## Sample Problems - 1

Problem 1: Determine the angle $\theta$ at which a particle in Jupiter's circular orbit experiences equal attractions from the sun and from Jupiter.


Problem 2: The motion of pin $P$ is controlled by the two moving slots $A$ and $B$ in which the pin slides.
(a) If $B$ has a velocity $v_{B}=3 \mathrm{~m} / \mathrm{s}$ to the right while $A$ has an upward velocity $v_{A}=2 \mathrm{~m} / \mathrm{s}$, determine the magnitude of the velocity of the pin.
(b) If $A$ has a downward velocity $v_{A}=1 \mathrm{~m} / \mathrm{s}$ and the velocity of the pin $P$ is also $1 \mathrm{~m} / \mathrm{s}$ downwards determine $v_{B}$.

Problem 3: In a design test of the actuating mechanism for a telescoping antenna on a spacecraft, the supporting shaft rotates about the fixed $z$-axis with an angular rate. Determine the $R$-, $\theta$-, and $\phi$-components of the acceleration $\vec{a}$ of the end of the antenna at the instant when $L=1.2 \mathrm{~m}$, and $\beta=45^{\circ}$, if the rates $\dot{\theta}=2$ $\mathrm{rad} / \mathrm{s}, \dot{\beta}=\frac{3}{2} \mathrm{rad} / \mathrm{s}$, and $\dot{L}=0.9 \mathrm{~m} / \mathrm{s}$ are constant during the motion.

## Problem 4:



The slotted arm $O A$ forces the small pin to move in the fixed spiral guide defined by $r=K \theta$. Arm $O A$ starts from rest at $\theta=\pi / 4$ and has a constant counterclockwise angular acceleration $\ddot{\theta}=\alpha$. Determine the magnitude of the acceleration of the $\operatorname{pin} P$ when $\theta=3 \pi / 4$.


Problem 5: In the design of an amusement-park ride, the cars are attached to arms of length $R$ which are hinged to a central rotating collar which drives the assembly about the vertical axis with a constant angular rate $\omega=\dot{\theta}$. The cars rise and fall with the track according to the relation $z=(h / 2)(1-2 \cos 2 \theta)$. Find the $R$-, $\theta$-, and $\phi$-components of the velocity $\vec{v}$ of each car as it passes the position $\theta=\frac{\pi}{4} \mathrm{rad}$.

Problem 6: The object of the pinball-type game is to project the particle so that it enters the hole at $E$. When the spring is compressed and suddenly released, the particle is projected along the track, which is smooth except for the rough portion between points $B$ and $C$, where the coefficient of kinetic friction is $\mu_{k}$ The particle becomes a projectile at oint $D$. Determine the correct spring
 compression $\delta$ so that the particle enters the hole at $E$. State any necessary conditions relating the lengths $d$ and $\rho$.

## Problem 7:

The inclined block $A$ is given a constant rightward acceleration $a$. Determine the range of values of $\theta$ for which block $B$ will not slip relative to block $A$, regardless of how large the acceleration $a$ is. The coefficient of static friction between the blocks is $\mu_{s}$.


## Problem 8:

The $10-\mathrm{kg}$ steel sphere is suspended from the $15-\mathrm{kg}$ frame which slides down the $20^{\circ}$ incline. If the coefficient of kinetic friction between the frame and incline is 0.15 , compute the tension in each of the supporting wires $A$ and $B$.


## Problem 9:

The bowl-shaped device rotates about a vertical axis with a constant angular velocity $\omega$. If the particle is observed to approach a steady-state position $\theta=40^{\circ}$ in the presence of a very small amount of friction, determine $\omega$. The value of $r$ is 0.2 m .


Problem 10: The chain of length $L$ and mass $\rho$ per unit length is released from rest on the smooth horizontal surface with a negligibly small overhang $x$ to initiate motion. Determine

(a) the acceleration $a$ as a function of $x$,
(b) the tension $T$ in the chain at the smooth corner as a function of $x$, and
(c) the velocity $v$ of the last link $A$ as it reaches the corner.

Problem 11: The system is released from rest while in the position shown. If $m_{1}=0.5 \mathrm{~kg}, m_{2}=4 \mathrm{~kg}, d=0.5 \mathrm{~m}$, and $\theta=20^{\circ}$, determine the speeds of both bodies just after the block leaves incline (before striking the horizontal surface). Neglect all friction.


Problem 12: The two bodies have the masses and initial velocities shown in the figure. The coefficient of restitution for the collision is $e=0.3$, and friction is negligible. If the time duration of the collision is 0.025 s , determine the average impact force which is exerted on the $3-\mathrm{kg}$ body. Also determine loss of total kinetic energy of the system during the collision.

Problem 13: If the system is released from rest, determine the speeds of both masses after $B$ has moved 1 m . Neglect friction and the masses of the pulleys.


Problem 14: The disk rotates about a fixed axis through $O$ with angular velocity $\omega=5 \mathrm{rad} / \mathrm{s}$ and angular acceleration $a=3 \mathrm{rad} / \mathrm{s}^{2}$ in the directions shown at a certain instant. The small sphere $A$ moves in the circular slot, and at the same instant, $\beta=30^{\circ}$ and $\dot{\beta}=-4 \mathrm{rad} / \mathrm{s}^{2}$. Determine the absolute velocity and acceleration of $A$ at this instant.


## Problem 15:

A slender rod bent into the shape shown rotates about the fixed line $C D$ at a constant angular rate $\omega$. Determine the velocity and acceleration of point $A$.


## Problem 16:

The robot shown has five degrees of rotational freedom. The $x-y-z$ axes are attached to the base ring, which rotates about the $z$-axis at the rate $\omega_{1}$. The $\operatorname{arm} O_{1} O_{2}$ rotates about the $x$-axis at the rate $\omega_{2}=\dot{\theta}$. The control arm $O_{2} \mathrm{~A}$ rotates about axis $\mathrm{O}_{1}-\mathrm{O}_{2}$ at the rate $\omega_{3}$ and about a perpendicular axis through $O_{2}$ which is momentarily parallel to the $x$-axis at the rate $\omega_{4}=\dot{\beta}$. Finally, the jaws rotate about axis $O_{2}-A$ at the rate $\omega_{5}$. The magnitudes of all angular rates are constant. For the configuration shown, determine the magnitude $\omega$ of the total angular velocity of the jaws for $\theta=60^{\circ}$ and $\beta=45^{\circ}$ if $\omega_{1}=2 \mathrm{rad} / \mathrm{s}, \dot{\theta}=1.5 \mathrm{rad} / \mathrm{s}$, and $\omega_{3}=\omega_{4}=\omega_{5}=0$. Also express the angular acceleration $\boldsymbol{\alpha}$ of arm $O_{1} O_{2}$ as a vector.


