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B+Trees

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- ▶ Maintaining a sequence set
- ▶ A simple prefix B+ Tree
- ▶ Simple Prefix B+ Tree Maintenance: Insertions and Deletions

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Motivation

- ▶ Some applications require two views of a file:

| Indexed view : | Sequential view : |
|------------------------------|--|
| Records are indexed by a key | Records can be sequentially accessed in order by key |
| Direct, indexed access | Sequential access (physically contiguous records) |
| Interactive, random access | Batch processing (Ex: co-sequential processing) |

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Example of Applications

- ▶ Student record system in a university
 - Indexed view: access to individual records
 - Sequential view: batch processing when posting grades or when fees are paid
- ▶ Credit card system
 - Indexed view: interactive check of accounts
 - Sequential view: batch processing of payment slips
- ▶ We will look at the following two aspect of the problem:
 1. Maintaining a sequence set: keeping records in sequential order
 2. Adding an index set to the sequence set

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Maintaining a Sequence Set

- ▶ Sorting and re-organizing after insertions and deletions is out of question
- ▶ We organize the sequence set in the following way
 - Records are grouped in **blocks**
 - Blocks should be **at least half full**
 - **Link fields** are used to point to the preceding block and the following block (similar to doubly linked list)
 - Changes (inserted/deletion) are localized into blocks by performing:
 1. **Block Splitting** when **insertion** causes overflow
 2. **Block Merging or Redistribution** when **deletion** causes underflow

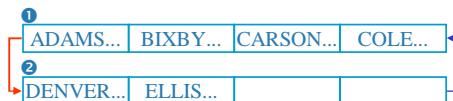
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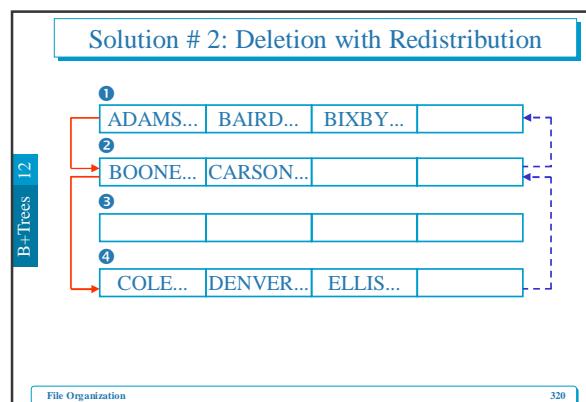
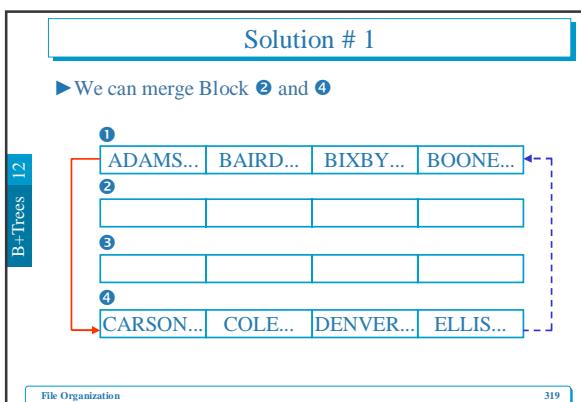
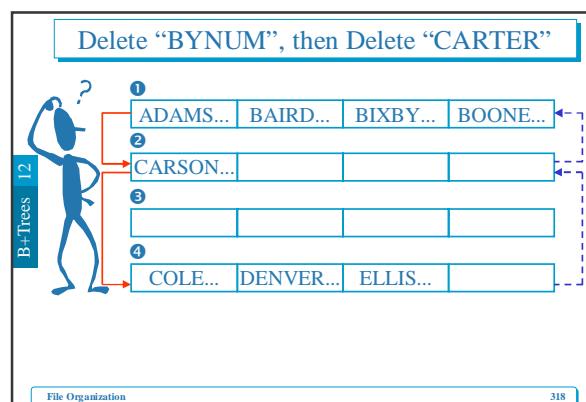
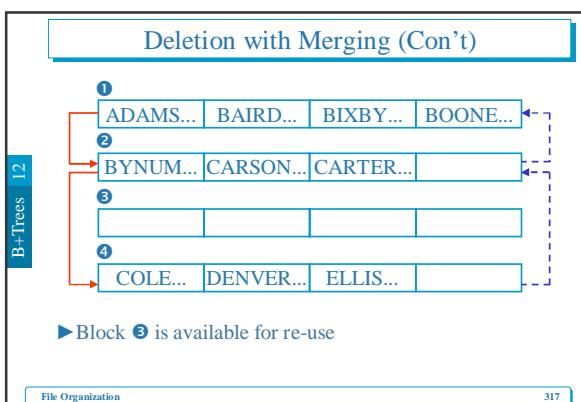
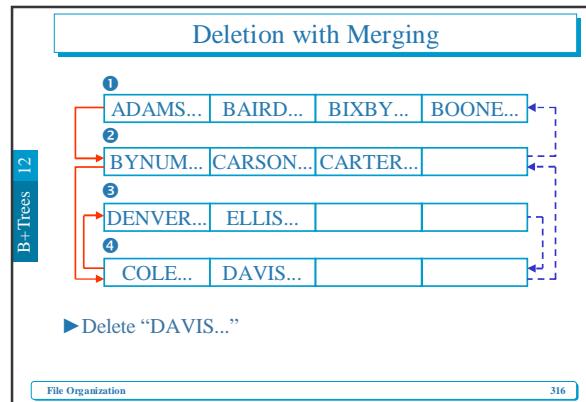
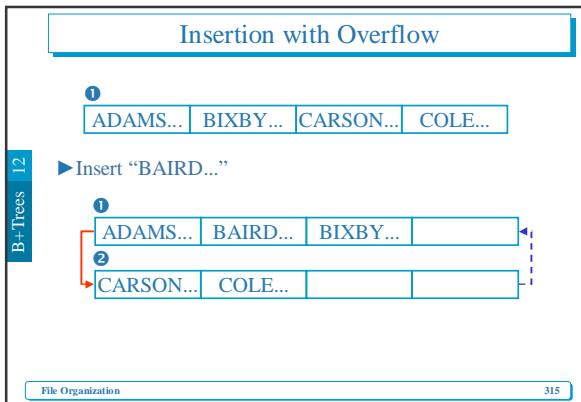
Example

- ▶ Block Size = 4
 - ▶ Key = Last Name
- Forward Pointer
← Backward Pointer



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Advantages and Disadvantages of Sequence Set

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- Advantages
 - No need to re-organize the whole file after insertions/deletions
- Disadvantages
 - File takes more space than unblocked files (since blocks may be half full)
 - The order of the records is not necessarily **physically** sequential (we only guarantee physical sequentiality within a block)

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Choosing Block Size

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- Main memory constraints (must hold at least 2 blocks)
- Avoid seeking within a block (e.g., in sector formatted disks choose block size equal to cluster size).

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Adding an Index Set to the Sequential Set

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- Index will contain SEPARATORS instead of KEYS

| | | | | | |
|---|----------|-------|-------|-----------|-------|
| ① | ADAMS... | | | BERNE... | BO |
| ② | BOLEN... | | | CAGE... | CAM |
| ③ | CAMP... | | | DUTTON... | E |
| ④ | EMBRY... | | | EVANS... | F |
| ⑤ | FABER... | | | FOLK... | FOLKS |
| ⑥ | FOLKS... | | | GADDIS... | |

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The Simple Prefix B+ Tree

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- The **simple prefix B+ tree** consists of
 - **Sequence Set**
 - **Index Set:** similar to a B-tree index, but storing the shortest separators for the sequence set.

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Example: Order of the index set is 3

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Search in a Simple Prefix B+ Tree

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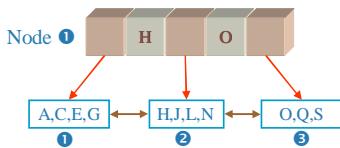
- Search for "EMBRY"
 - Retrieve Node ① (Root)
 - Since "EMBRY">>"E", so go right, and retrieve Node ②.
 - Since "EMBRY"<"F", so go left, and Block # ④
 - Look for the record with key "EMBRY" in Block # ④

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Simple Prefix B+ Tree Maintenance

► Example:

- Sequence set has blocking factor 4
- Index set is a B tree of order 3



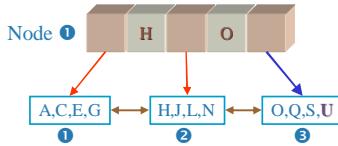
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Example (Cont'd)

1. Changes which are local to single blocks in the sequence set

- Insert "U"
- Go to the root
- Go to the right of "O"
- Insert "U" to Block 3



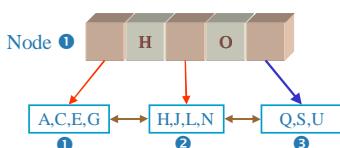
-There is no change in the index set

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Example (Cont'd)

- Delete "O"
- Go to the root
- Go to the right of "O"
- Delete "O" from Block 3



-There is no change in the index set: "O" is still a perfect separator for Blocks 2 and 3

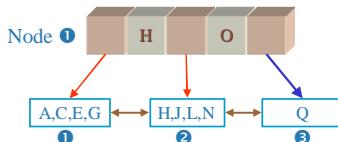
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Example (Cont'd)

2. Changes involving multiple blocks in the sequence set

- Delete "S" and "U"



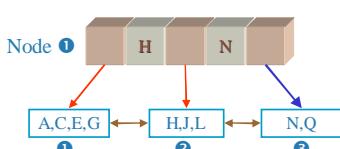
-Now Block 3 becomes less than ½ full (UNDERFLOW)

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Example (Cont'd)

- Since Block 2 is full, the only position is re-distribution bringing a key from Block 2 to Block 3
- We must update the separator "O" to "N"

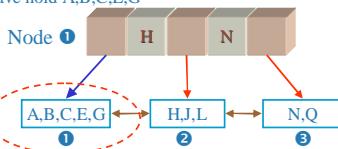


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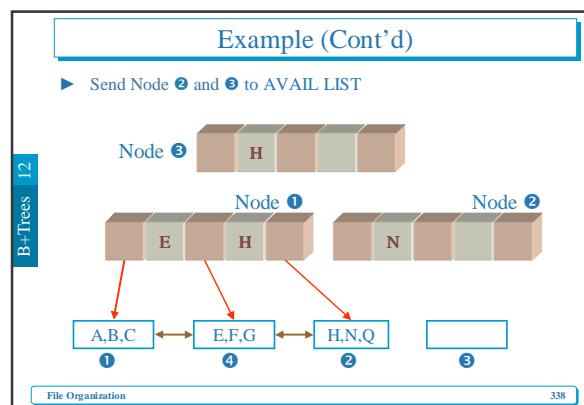
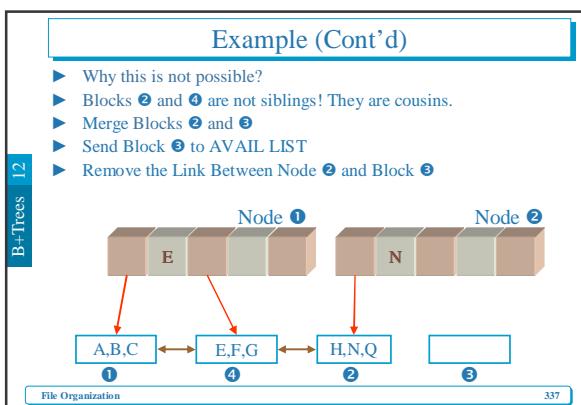
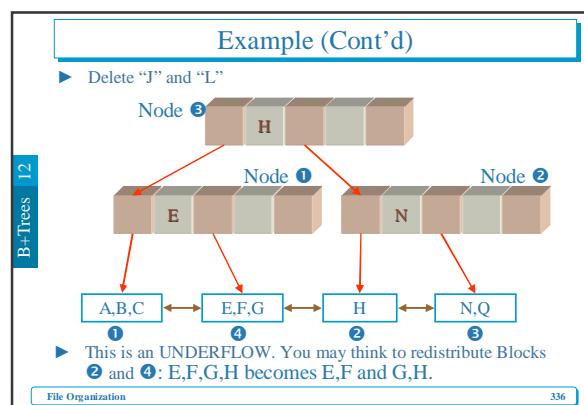
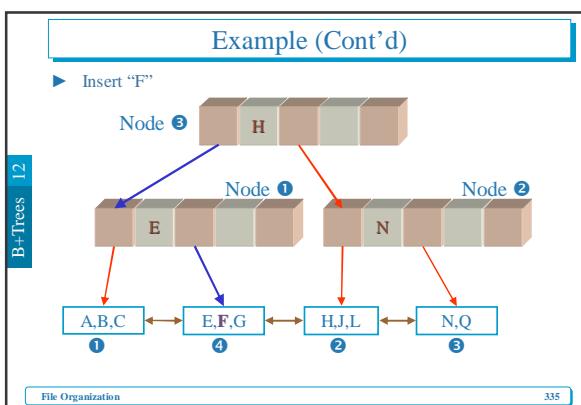
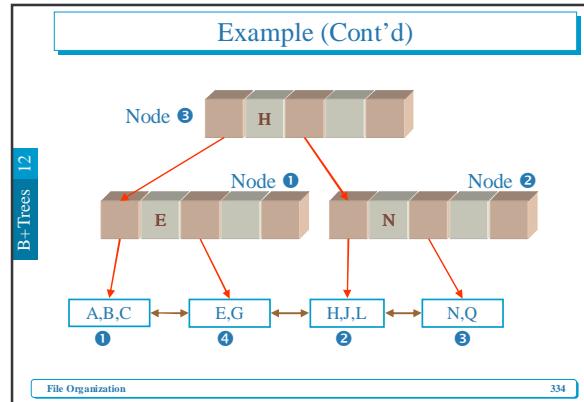
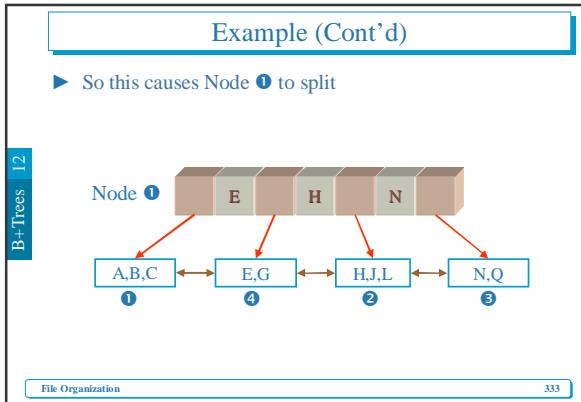
Example (Cont'd)

- Insert "B"
- Go to the root
- Go to the left of "H" to Block 1
- Block 1 would hold A,B,C,E,G
- Block 1 is split



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Example (Cont'd)

- Blocks were reunited as a big happy family again ☺

