

TABLE: SELECTED DIMENSIONAL EQUIVALENTS

Length	<p>1 m = 3.280 ft 0.39.37 in                      1 cm = <math>10^{-2}</math> m = 0.394 in = 0.038 ft                      1 mm = <math>10^{-3}</math> m                      1 micron (m) = <math>10^{-10}</math> m                      1 Angstrom (<math>^{\circ}</math>A) <math>10^{-6}</math> m</p>
Time	<p>1 hr = 3600 sec = 60 min                      1 milisec = <math>10^{-3}</math> sec                      1 microsec (<math>\mu</math>sec) = <math>10^{-6}</math> sec                      1 nanosec (nsec) = <math>10^{-9}</math> sec</p>
Mass	<p>1 kg = 1000 gr = 2.2046 lbm = <math>6.8521 \times 10^{-2}</math> slugs                      1 slugs = 1 lbf.<math>\text{sec}^{-2}</math>/ft = 32.174 lbm                      1 amu = <math>1.66 \times 10^{-27}</math> kg</p>
Force	<p>1 newton = 1 kg.m/<math>\text{sec}^2</math>                      1 dyne = 1 gr.cm/<math>\text{sec}^2</math>                      1 lbf = <math>4.448 \times 10^5</math> dyne = 4.448 newtons</p>
Energy	<p>1 joule = 1 kg.m<sup>2</sup>/<math>\text{sec}^2</math> = 0.239 cal= 0.738 ft.lb = <math>2.78 \times 10^{-7}</math> kwh                      1 joule = <math>10^7</math> erg                      1 Btu = 778.18 ft.lbf= <math>1.055 \times 10^{15}</math> erg = 252 cal                      1 cal = 4.186 joule                      1 erg = 1 gr.cm<sup>2</sup>/<math>\text{sec}^2</math>                      1 eV = <math>1.602 \times 10^{-19}</math> joules = <math>160 \times 10^{-12}</math> erg</p>
Power	<p>1 Watt = 1 kg.m<sup>2</sup>/<math>\text{sec}^3</math> = 1 joule/sec                      1 hp = 550 ft.lbf/sec                      1 hp = 2545 Btu/hr = 746 Watts                      1 kWatt = 1000 Watts = 3413 Btu/hr</p>
Pressure	<p>1 atm = 14.696 lbf/in<sup>2</sup> = 760 torr                      1 mmHg = 0.01931 lbf/in<sup>2</sup> = 1 torr                      1 dyne/cm<sup>2</sup> = <math>145.04 \times 10^{-7}</math>                      1 bar = 14.504 lbf/in<sup>2</sup> = <math>10^6</math> dynes/cm<sup>2</sup>                      1 micron (<math>\mu</math>) = <math>10^{-6}</math> mHg = <math>10^{-3}</math> mmHg                      1 hPa = 1 mb                      1 hPa = 100 Pa</p>
Volume	<p>1 gal = 0.13368 ft<sup>3</sup>                      1 liter = 1000.028 cm<sup>3</sup></p>
Temperature	<p>1 <math>^{\circ}</math>K = 1 <math>^{\circ}</math>C = 1.8 <math>^{\circ}</math>F = 1.8 <math>^{\circ}</math>R                      0 <math>^{\circ}</math>C corresponds to 32 <math>^{\circ}</math>F, 273.16 <math>^{\circ}</math>K, and 491.69 <math>^{\circ}</math>R                      1 eV = 11600 <math>^{\circ}</math>K</p>
Magnetic Quantities	<p>1 Gauss = 1 g<sup>1/2</sup>/cm<sup>1/2</sup>.sec                      1 Gauss = <math>10^3</math> coul/m.sec for M                      1 Gauss = <math>(1/4\pi) \times 10^3</math> coul/m.sec for H                      1 Gauss = <math>10^{-4}</math> Tesla for B                      1 Tesla = 1 kg/coul.sec                      1 Tesla = 1 kg/A.<math>\text{sec}^2</math>                      1 nT = <math>10^{-9}</math> Tesla                      1 nT = <math>10^{-5}</math> Gauss                      1 gamma = 1 g = 1 nT</p> <p>Magnetic Flux: <math>\phi_B = \int B \cdot dA</math> , 1 Weber = 1 kg.m<sup>2</sup>/coul.sec</p> <p><math> \vec{B}  = \text{kg/sec.coul}</math></p>
Electrical Quantities	<p>E-potential: <math>\mathcal{E}, d\mathcal{E} = \vec{E} \cdot d\vec{l}</math> E, 1 volt = 1 kg.m<sup>2</sup>/coul.sec<sup>2</sup></p> <p><math> \vec{E}  = \text{kg.m/coul.sec}</math></p> <p>Current Density: coul/m<sup>2</sup>.sec                      Current: coul/sec                      Resistance (R): 1 ohm = 1 kg.m<sup>2</sup>/coul<sup>2</sup>.sec</p>

PHYSICAL CONSTANTS

Avogadro's Number	$N = 6.025 \times 10^{23}$ /g.mole
Bolzman's Constant	$k = 1.38 \times 10^{-23}$ joule / <sup>o</sup> K
Stefan Boltzmann Constant	$\sigma = 5.7 \times 10^{-5}$ erg/cm <sup>2</sup> .sec. <sup>o</sup> K <sup>4</sup> $\sigma = 5.67 \times 10^{-8}$ joule/m <sup>2</sup> .sec. <sup>o</sup> K <sup>4</sup>
Gas Constant	$R = 1545.33$ ft.lbf/lb.mole. <sup>o</sup> R $R = 8.317$ joule/g-mole. <sup>o</sup> K $R = 8317$ joule/kg-mole. <sup>o</sup> K $R = 1.986$ Btu/lb.mole. <sup>o</sup> R $R = 1.986$ cal/g.mole. <sup>o</sup> K
Planck's Constant	$h = 6.625 \times 10^{-34}$ joule.sec
Biot-Savart Constant	$1/4\pi\epsilon_0 = 8.987 \times 10^9$ kg.m <sup>3</sup> /coul <sup>2</sup> .sec <sup>2</sup> $\mu_0/4\pi = 1.000 \times 10^{-7}$ kg.m/coul <sup>2</sup>
Electronic Charge	$e = -1.6021 \times 10^{-19}$ coul
Proton Mass	$m_p = 1.67 \times 10^{-27}$ kg
Electron Mass	$m_e = 9.1 \times 10^{-31}$ kg
Speed of Light	$c = 2.998 \times 10^8$ m/sec
Newton's Constant	$g_c = 32.174$ ft.lbm/lbf.sec <sup>2</sup>
Gravitational Constant	$k_G = 6.67 \times 10^{-11}$ m <sup>3</sup> /kg.sec <sup>2</sup>
Wienn's Constant	$c = 0.28$ cm. <sup>o</sup> K
Sun-Earth Distance	1 AU = $1.5 \times 10^8$ km
Solar Constant for Earth	$I_o = 1.94$ cal/cm <sup>2</sup> min $I_o = 1370$ Watt/m <sup>2</sup>
Sun's Radius	$R_{sun} = 7 \times 10^5$ km
Sun's Mass	$M_{sun} = 2 \times 10^{30}$ kg
Sun's Surface Temperature	$T = 6000$ <sup>o</sup> K
Sun's Luminosity	$L = 4 \times 10^{26}$ Watt
Earth's Radius	$R_{Earth} = 6378$ km
Earth's Albedo	A or $\alpha = \% 33$ or 0.33
Magnetic Field at the Earth's Equator	$B_o = 0.36$ Gauss (CGS) $B_o = 0.3 \times 10^{-4}$ Tesla (MKS)
$\mu_0$	$\mu_0 = 4\pi \times 10^{-7}$ (MKS, Henry/m, or kg.m/coul <sup>2</sup> , Henry = kg.m <sup>2</sup> /coul <sup>2</sup> )
<p>R : Universal Gas Constant  <math>R^*</math> : Specific Gas Constant  <math>R^* = (R \times 10^3) / M</math>, M = 29 amu for Air  <math>R^* = (8.317 \times 10^3) / 29 = 286</math> (MKS)  P = <math>\rho R^* T</math> or PV=RT</p>	

Symbol	MKS (SI)	CGS (Gaussian System)
Length	1 m	$10^2$ cm
Mass	1 kg	$10^3$ g
Time	1 s, 1 sec	1 s, 1 sec
Force	1 N	$10^5$ dynes
Work or Energy	1 J	$10^7$ erg
Power	1 W	$10^7$ ergs/s
Charge	1 C	$3 \times 10^9$ statcoul
Current	1 A	$3 \times 10^9$ statamp
Electric Field Strength	1 V/m	$(1/3) \times 10^{-4}$ statvolt/cm
Electric Potential	1 V	(1/300) statvolt
Electric Polarization	1 C/m <sup>2</sup>	$3 \times 10^5$ statcoul/cm <sup>2</sup>
Electric Displacement	1 C/m <sup>2</sup>	$12\pi \times 10^5$ statvolt/cm <sup>2</sup>
Resistance	1 $\Omega$	$(1/9) \times 10^{-11}$ s/cm
Capacitance	1 F	$9 \times 10^{11}$ cm
Magnetic Flux	1 Wb	$10^8$ Maxwells
Magnetic Induction	1 T	$10^4$ Gauss
Magnetic Field Strength	1 A-turn/m	$4\pi \times 10^3$ Gauss

To convert to	Multiply by
kilo	$10^3$
mega	$10^6$
giga	$10^9$
centri	$10^{-2}$
mili	$10^{-3}$
micro	$10^{-6}$
nano	$10^{-9}$
pico	$10^{-12}$
ppmv = one per million	$10^{-6}$
ppbv = one per billion	$10^{-9}$
pptv = one per trillion	$10^{-12}$

## LENGTH

- 1 kilometer (km) = 1000 meters (m)  
= 3281 feet (ft)  
= 0.62 mile (mi)
- 1 mile (mi) = 5280 feet (ft)  
= 1609 meters (m)  
= 1.61 kilometers (km)
- 1 centimeter (cm) = 0.39 inch (in.)  
= 0.01 meter (m)
- 1 inch (in.) = 2.54 cm  
= 0.08 ft
- 1 meter (m) = 100 cm  
= 3.28 ft  
= 39.37 in.
- 1 micrometer ( $\mu\text{m}$ ) = 0.0001 cm  
= 0.000001 m

## AREA

- 1 square centimeter ( $\text{cm}^2$ ) = 0.15 in.<sup>2</sup>  
1 square inch (in.<sup>2</sup>) = 6.45 cm<sup>2</sup>  
1 square meter (m<sup>2</sup>) = 10.76 ft<sup>2</sup>  
1 square foot (ft<sup>2</sup>) = 0.09 m<sup>2</sup>

## VOLUME

- 1 cubic centimeter ( $\text{cm}^3$ ) = 0.06 in.<sup>3</sup>  
1 cubic inch (in.<sup>3</sup>) = 16.39 cm<sup>3</sup>  
1 liter (l) = 1000 cm<sup>3</sup>

## SPEED

- 1 knot = 1.15 mph  
= 0.51 mps  
= 1.85 kph
- 1 mile per hour (mph) = 0.87 knot  
= 0.45 mps  
= 1.61 kph
- 1 kilometer per hour (kph) = 0.54 knot  
= 0.62 mph  
= 0.28 mps
- 1 meter per second (mps) = 1.9 knots  
= 2.2 mph  
= 3.6 kph

# A

## UNITS, CONVERSIONS, AND ABBREVIATIONS

## MASS

- 1 gram (g) = 0.035 ounce  
= 0.002 lb
- 1 kilogram (kg) = 1000 g  
= 2.2 lb

## ENERGY

- 1 joule (J) = 0.239 cal  
1 calorie (cal) = 4.187 J

## PRESSURE

- 1 millibar (mb) = 1000 dynes/cm<sup>2</sup>  
= 0.75 millimeter of mercury  
= 0.03 inch of mercury  
= 0.01 pound per square  
inch (psi)  
= 100 pascals (Pa)
- 1 standard atmosphere = 1013.25 mb  
= 760 millimeters of  
mercury  
= 29.92 inches of  
mercury  
= 14.7 psi

## Appendix A

### Conversion to SI Units

Physical quantity	Unit	SI (MKS) equivalent
Length	ft	0.305 m
	$\mu\text{m}$	$10^{-6}$ m
	nm	$10^{-9}$ m
Time	day	$8.64 \times 10^4$ s
Mass	lb	0.454 kg
Temperature	$^{\circ}\text{F}$	$273 + (^{\circ}\text{F} - 32)/1.8$ K
Volume	liter	$10^{-3}$ m <sup>3</sup>
Velocity	mph	$0.447$ m s <sup>-1</sup>
	knots	$0.515$ m s <sup>-1</sup>
	km hr <sup>-1</sup>	$0.278$ m s <sup>-1</sup>
	fps	$0.305$ m s <sup>-1</sup>
Force	kg m s <sup>-2</sup>	1 N
	lb	0.138 N
	dyne	$10^{-5}$ N
Pressure	N m <sup>-2</sup>	1 Pa
	bar	$10^5$ Pa
	mb	$10^2$ Pa = 1 hPa
Energy	kg m <sup>2</sup> s <sup>-2</sup>	1 J
	Nm	1 J
	erg	$10^{-7}$ J
	cal	4.187 J
Power	kg m <sup>-2</sup> s <sup>-3</sup>	1 W
	J s <sup>-1</sup>	1 W
	Langley day <sup>-1</sup>	$4.84 \times 10^{-1}$ W m <sup>-2</sup>
Specific heat	cal gm <sup>-1</sup>	$4.184 \times 10^3$ J kg <sup>-1</sup>
Energy flux	cal cm <sup>-2</sup> min <sup>-1</sup>	$6.97 \times 10^2$ W m <sup>-2</sup>

## Appendix B

### Thermodynamic Properties of Air and Water

#### Dry Air

Mean molecular weight	$M_d = 28.96 \text{ g mol}^{-1}$
Specific gas constant	$R = 287.05 \text{ J kg}^{-1} \text{ K}^{-1}$
Density	$\rho = 1.293 \text{ kg m}^{-3}$ (at STP*)
Number density (Loschmidt number)	$n = 2.687 \times 10^{25} \text{ m}^{-3}$ (at STP)
Isobaric specific heat capacity	$c_p = 1.005 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Isochoric specific heat capacity	$c_v = 7.19 \times 10^2 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Ratio of specific heats	$\gamma = c_p/c_v = 1.4$
	$\kappa = (\gamma - 1)/\gamma = R/c_p = 0.286$
Coefficient of viscosity	$\mu = 1.73 \times 10^{-5} \text{ kg m}^{-1} \text{ s}^{-1}$ (at STP)
Kinematic viscosity	$\nu = 1.34 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$ (at STP)
Coefficient of thermal conductivity	$k = 2.40 \times 10^{-2} \text{ W m}^{-1} \text{ K}^{-1}$ (at STP)
Sound speed	$c_s = 331 \text{ m s}^{-1}$ (at 273 K)

#### Water

Mean molecular weight	$M_v = 18.015 \text{ g mol}^{-1}$
	$\epsilon = M_v/M_d = 0.622$
Specific gas constant	$R = 461.51 \text{ J kg}^{-1} \text{ K}^{-1}$
Density (liquid water)	$\rho = 10^3 \text{ kg m}^{-3}$ (at STP)
Density (ice)	$\rho = 9.17 \times 10^2 \text{ kg m}^{-3}$ (at STP)
Isobaric specific heat capacity (vapor)	$c_p = 1.85 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Isochoric specific heat capacity (vapor)	$c_v = 1.39 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Ratio of specific heats (vapor)	$\gamma = c_p/c_v = 1.33$
Specific heat capacity (liquid water)	$c = 4.218 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Specific heat capacity (ice)	$c = 2.106 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Specific latent heat of fusion	$l_f = 3.34 \times 10^5 \text{ J kg}^{-1}$
Specific latent heat of vaporization	$l_v = 2.50 \times 10^6 \text{ J kg}^{-1}$
Specific latent heat of sublimation	$l_s = l_f + l_v$

\*Standard temperature and pressure (STP) = 1013 mb and 273 K.

## Appendix C

### Physical Constants

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Avogadro's number	$N_A = 6.022 \times 10^{26} \text{ mol}^{-1}$
Universal gas constant	$R^* = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$
Boltzmann constant	$k = 1.381 \times 10^{-23} \text{ J K}^{-1}$
Planck constant	$h = 6.6261 \times 10^{-34} \text{ J s}^{-1}$
Stefan-Boltzmann constant	$\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$
Speed of light	$c = 2.998 \times 10^8 \text{ m s}^{-1}$
Solar constant	$F_s = 1.372 \times 10^3 \text{ W m}^{-2}$
Radius of the earth	$a = 6.371 \times 10^3 \text{ km}$
Standard gravity	$g_0 = 9.806 \text{ m s}^{-2}$
Earth's angular velocity	$\Omega = 7.292 \times 10^{-5} \text{ s}^{-1}$

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## Appendix D

### Vector Identities

$$\mathbf{A} \times (\mathbf{B} \times \mathbf{C}) = (\mathbf{A} \cdot \mathbf{C})\mathbf{B} - (\mathbf{A} \cdot \mathbf{B})\mathbf{C} \quad (\text{D.1})$$

$$\mathbf{A} \cdot (\mathbf{B} \times \mathbf{C}) = (\mathbf{A} \times \mathbf{B}) \cdot \mathbf{C} = \mathbf{B} \cdot (\mathbf{C} \times \mathbf{A}) \quad (\text{D.2})$$

$$(\mathbf{A} \times \mathbf{B}) \cdot (\mathbf{C} \times \mathbf{D}) = (\mathbf{A} \cdot \mathbf{C})(\mathbf{B} \cdot \mathbf{D}) - (\mathbf{A} \cdot \mathbf{D})(\mathbf{B} \cdot \mathbf{C}) \quad (\text{D.3})$$

$$\nabla(fg) = f\nabla g + g\nabla f \quad (\text{D.4})$$

$$\nabla \cdot (f\mathbf{A}) = \nabla f \cdot \mathbf{A} + f\nabla \cdot \mathbf{A} \quad (\text{D.5})$$

$$\nabla \times (f\mathbf{A}) = \nabla f \times \mathbf{A} + f\nabla \times \mathbf{A} \quad (\text{D.6})$$

$$\nabla \cdot (\mathbf{A} \times \mathbf{B}) = \mathbf{B} \cdot (\nabla \times \mathbf{A}) - \mathbf{A} \cdot (\nabla \times \mathbf{B}) \quad (\text{D.7})$$

$$\nabla \cdot \nabla \times \mathbf{A} = 0 \quad (\text{D.8})$$

$$\nabla \times \nabla f = 0 \quad (\text{D.9})$$

$$\nabla \cdot \nabla f = \nabla^2 f \quad (\text{D.10})$$

$$\nabla \times \nabla \times f = \nabla(\nabla \cdot f) - \nabla^2 f \quad (\text{D.11})$$

$$\nabla(\mathbf{A} \cdot \mathbf{B}) = \mathbf{A} \cdot \nabla \mathbf{B} + \mathbf{B} \cdot \nabla \mathbf{A} + \mathbf{A} \times \nabla \mathbf{B} + \mathbf{B} \times \nabla \times \mathbf{A} \quad (\text{D.12})$$

$$\nabla(\mathbf{A} \times \mathbf{B}) = \mathbf{B} \cdot \nabla \mathbf{A} - \mathbf{A} \cdot \nabla \mathbf{B} + \mathbf{A}(\nabla \cdot \mathbf{B}) - \mathbf{B}(\nabla \cdot \mathbf{A}) \quad (\text{D.13})$$

$$\mathbf{A} \cdot \nabla \mathbf{A} = \frac{1}{2} \nabla(\mathbf{A} \cdot \mathbf{A}) - \mathbf{A} \times (\nabla \times \mathbf{A}) \quad (\text{D.14})$$



## Appendix E

### Curvilinear Coordinates

Spherical Coordinates  $(\lambda, \phi, r)$

$$\nabla\psi = \frac{1}{r \cos \phi} \frac{\partial\psi}{\partial\lambda} \mathbf{e}_\lambda + \frac{1}{r} \frac{\partial\psi}{\partial\phi} \mathbf{e}_\phi + \frac{\partial\psi}{\partial r} \mathbf{e}_r$$

$$\nabla \cdot \mathbf{A} = \frac{1}{r \cos \phi} \frac{\partial A_\lambda}{\partial \lambda} + \frac{1}{r \cos \phi} \frac{\partial}{\partial \phi} (\cos \phi A_\phi) + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 A_r)$$

$$\begin{aligned} \nabla \times \mathbf{A} = & \frac{1}{(r^2 \cos \phi)} \left\{ r \cos \phi \left[ \frac{\partial A_r}{\partial \phi} - \frac{\partial (r A_\phi)}{\partial r} \right] \mathbf{e}_\lambda \right. \\ & + r \left[ \frac{\partial}{\partial r} (r \cos \phi A_\lambda) - \frac{\partial A_r}{\partial \lambda} \right] \mathbf{e}_\phi \\ & \left. + \left[ \frac{\partial (r A_\phi)}{\partial \lambda} - \frac{\partial}{\partial \phi} (r \cos \phi A_\lambda) \right] \mathbf{e}_r \right\} \end{aligned}$$

$$\nabla^2 \psi = \frac{1}{r^2 \cos^2 \phi} \frac{\partial^2 \psi}{\partial \lambda^2} + \frac{1}{r^2 \cos \phi} \frac{\partial}{\partial \phi} \left( \cos \phi \frac{\partial \psi}{\partial \phi} \right) + \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \frac{\partial \psi}{\partial r} \right)$$

$$\begin{aligned} \nabla^2 \mathbf{A} = & \left[ \nabla^2 A_\lambda - \frac{A_\lambda}{r^2 \cos^2 \phi} + \frac{2}{r^2 \cos \phi} \frac{\partial A_r}{\partial \lambda} + \frac{2 \sin \phi}{r^2 \cos^2 \phi} \frac{\partial A_\phi}{\partial \lambda} \right] \mathbf{e}_\lambda \\ & + \left[ \nabla^2 A_\phi - \frac{A_\phi}{r^2 \cos^2 \phi} + \frac{2}{r^2} \frac{\partial A_r}{\partial \phi} - \frac{2 \sin \phi}{r^2 \cos^2 \phi} \frac{\partial A_\lambda}{\partial \lambda} \right] \mathbf{e}_\phi \\ & + \left[ \nabla^2 A_r - \frac{2}{r^2} A_r - \frac{2}{r^2 \cos \phi} \frac{\partial}{\partial \phi} (\sin \phi A_\phi) - \frac{2}{r^2 \cos \phi} \frac{\partial A_\lambda}{\partial \lambda} \right] \mathbf{e}_r \end{aligned}$$

Cylindrical Coordinates ( $r, \phi, z$ )

$$\nabla\psi = \frac{\partial\psi}{\partial r}\mathbf{e}_r + \frac{1}{r}\frac{\partial\psi}{\partial\phi}\mathbf{e}_\phi + \frac{\partial\psi}{\partial z}\mathbf{e}_z \quad (\text{E.6})$$

$$\nabla \cdot \mathbf{A} = \frac{1}{r}\frac{\partial}{\partial r}(rA_r) + \frac{1}{r}\frac{\partial A_\phi}{\partial\phi} + \frac{\partial A_z}{\partial z} \quad (\text{E.7})$$

$$\begin{aligned} \nabla \times \mathbf{A} = & \left[ \frac{1}{r}\frac{\partial A_z}{\partial\phi} - \frac{\partial A_\phi}{\partial z} \right] \mathbf{e}_r + \left[ \frac{\partial A_r}{\partial z} - \frac{\partial A_z}{\partial r} \right] \mathbf{e}_\phi \\ & + \left[ \frac{1}{r}\frac{\partial(rA_\phi)}{\partial r} - \frac{1}{r}\frac{\partial A_r}{\partial\phi} \right] \mathbf{e}_z \end{aligned} \quad (\text{E.8})$$

$$\nabla^2\psi = \frac{1}{r}\frac{\partial}{\partial r}\left(r\frac{\partial\psi}{\partial r}\right) + \frac{1}{r^2}\frac{\partial^2\psi}{\partial\phi^2} + \frac{\partial^2\psi}{\partial z^2} \quad (\text{E.9})$$

$$\begin{aligned} \nabla^2\mathbf{A} = & \left[ \nabla^2 A_r - \frac{A_r}{r^2} - \frac{2}{r^2}\frac{\partial A_\phi}{\partial\phi} \right] \mathbf{e}_r + \left[ \nabla^2 A_\phi - \frac{A_\phi}{r^2} + \frac{2}{r^2}\frac{\partial A_r}{\partial\phi} \right] \mathbf{e}_\phi \\ & + \nabla^2 A_z \mathbf{e}_z \end{aligned} \quad (\text{E.10})$$