## SOLUTIONS TO MIDTERM EXAM 2 QUESTIONS

1.a. ( 15 pts.$)$

| Party A | 182,679 | 182,679 | 91,340 | 91,340 | 91,340 | 60,893 | 60,893 | 2 |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :--- |
| Party B | 42,033 | 42,033 | 42,033 | 42,033 | 42,033 | 42,033 | 42,033 | - |
| Party C | 43,648 | 43,648 | 43,648 | 43,648 | 43,648 | 43,648 | 43,648 | - |
| Party D | 264,842 | 132,421 | 132,421 | 88,281 | 88,281 | 88,281 | 66,211 | 4 |
| Party E | 106,862 | 106,862 | 106,862 | 106,862 | 53,431 | 53,431 | 53,431 | 1 |
| $\max$ | 264,842 | 182,679 | 132,421 | 106,862 | 91,340 | 88,281 | 66,211 |  |

4 seats are allocated to Party D, 2 seats are allocated to Party A, and 1 seat is allocated to Party E.
1.b. (15 pts.)

Total number of votes: 640,064
Electoral coefficient: 91,437.71

| Party A | 1.9979 | 1 | 91,241 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Party B | 0.4597 | - | 42,033 |  | - |
| Party C | 0.4774 | - | 43,648 | 1 | 1 |
| Party D | 2.8964 | 2 | 81,967 | 1 | 3 |
| Party E | 1.1687 | 1 | 15,424 |  | 1 |

3 seats are allocated to Party D, 2 seats are allocated to Party A, and 1 seat each is allocated to Party C and Party E.

## 2. ( 35 pts .)

| M | a | b | c |
| :---: | :---: | :---: | :---: |
| a | 0 | 4 | 5 |
| b | 6 | 0 | 7 |
| c | 5 | 3 | 0 |
|  |  |  |  |
| E | a | b | c |
| a | 0 | -2 | 0 |
| b | 2 | 0 | 4 |
| c | 0 | -4 | 0 |


| $\mathrm{M}^{\text {T }}$ | a | b | c |
| :---: | :---: | :---: | :---: |
| a | 0 | 6 | 5 |
| b | 4 | 0 | 3 |
| c | 5 | 7 | 0 |


| 'a PbPc' | L | a | b | c | $\mathrm{f}_{\mathrm{k}}=4$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | a | 0 | 1 | 1 |  |
|  | b | -1 | 0 | 1 | $\mathrm{f}_{\mathrm{k}}=-12$ |
|  | c | -1 | -1 | 0 |  |
|  | L | a | b | c |  |
|  | a | 0 | 1 | 1 |  |
|  | b | -1 | 0 | -1 |  |
|  | c | -1 | 1 | 0 |  |


| 'b P a P c' | L | a | b | c | $\mathrm{f}_{\mathrm{k}}=12$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | a | 0 | -1 | 1 |  |
|  | b | 1 | 0 | 1 |  |
|  | c | -1 | -1 | 0 |  |



Best rankings are 'b $\mathrm{Pa} \operatorname{Pc}$ c and 'b Pcea'
3. $(35 \mathrm{pts}$ )

UNWEIGHTED MATRIX

|  |  | I |  | II |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | A | B | C | D | E |
| I | A | 1 | 0 | 0.75 | 0.8 | 1 |
|  | B | 0 | 1 | 0.25 | 0.2 | 0 |
| II | C | 0.75 | 0.5 | 1 | 0 | 0 |
|  | D | 0.25 | 0 | 0 | 1 | 0 |
|  | E | 0 | 0.5 | 0 | 0 | 1 |

## WEIGHTED MATRIX

|  |  | I |  | II |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | A | B | C | D | E |
| I | A | 0.5 | 0 | 0.375 | 0.4 | 0.5 |
|  | B | 0 | 0.5 | 0.125 | 0.1 | 0 |
| I II | C | 0.375 | 0.25 | 0.5 | 0 | 0 |
|  | D | 0.125 | 0 | 0 | 0.5 | 0 |
|  | E | 0 | 0.25 | 0 | 0 | 0.5 |

## LIMIT MATRIX

|  |  | I |  | II |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | A | B | C | D | E |
| I | A | 0.3933 | 0.3933 | 0.3933 | 0.3933 | 0.3933 |
|  | B | 0.1067 | 0.1067 | 0.1067 | 0.1067 | 0.1067 |
| I II | C | 0.3483 | 0.3483 | 0.3483 | 0.3483 | 0.3483 |
|  | D | 0.0983 | 0.0983 | 0.0983 | 0.0983 | 0.0983 |
|  | E | 0.0534 | 0.0534 | 0.0534 | 0.0534 | 0.0534 |

