Cognitive Maps

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Introduction



- Cognitive mapping is the task of mapping a person's thinking about a problem or issue (Tolman, 1948).
- A cognitive map is the representation of thinking about a problem that follows from the process of mapping.
- **Cognition** can be used to refer to the mental models, or belief systems, that people use to perceive, contextualize, simplify, and make sense of otherwise complex problems.

Definition



- A cognitive map is an image of cognitive processes and an attempt to utilize expert(s) opinion and cognition about ill-structured social relationships (Axelrod, 1976; Lee *et al.*, 1992)
- Cognitive maps are *cause-effect networks*, with nodes representing concepts articulated by individuals, and directional linkages capturing causal dependencies (Srinivas and Shekar, 1997).

Why?



- Cognitive mapping is a tool which enables a group of experts and/or specialists to negotiate a definition of the problem that is visualized in the form of a model amenable to further elaboration and to the analysis of complexity (Eden, 1988)
- One of the practical aims of cognitive mapping is to attain an appropriate and powerful link between the qualitative aspects of a problem definition and the role of quantitative analysis (Eden et al., 1986)

Where?



- Cognitive maps have been studied in various fields of science, such as
 - psychology
 - planning
 - geography
 - management

Directed Graph



- The problem is represented by a **signed digraph** (directed graph) of basic elements where
 - A <u>concept variable</u> is symbolized as a <u>point</u>, and
 - The causal assertion (belief) of how one concept variable affects another (<u>relationship</u> between the variables) is symbolized as an <u>arrow</u>
 - A <u>plus sign</u> is attached to the arrows that show positive relationships (changes occur in the same direction)
 - A <u>minus sign</u> is attached to the arrows that show negative relationships (changes occur in the opposite direction)

Signed Digraph for Energy Demand





Deriving Cognitive Map



- There are three basic ways of deriving a cognitive map of the expert opinion (Hwang & Lin, 1987):
 - questionnaire survey,
 - documentary coding, and
 - interviews.
- A questionnaire survey can be divided into three phases (Roberts, 1976):
 - identifying potentially relevant variables,
 - limiting the number of variables by rating their importance, and
 - the choice of arrows and signs

Analysing Cognitive Map

- Decision Explorer software package (Banxia Software, 1996)
 - Domain analysis (centrality)
 - Head-Tail analysis"
 - Cluster analysis
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Centrality



- The total number of concept variables directly affected by concept *i* is
 outdegree of variable *i*
- The total number of concept variables directly affects concept *i* is indegree of variable *i*
- outdegree + indegree = total degree (centrality)

Heads and tails



- Typically a node which has no implication (outgoing arrows) is referred to as a "head", and a node which has no in-arrows is referred to as a "tail".
- The node which has the highest total of incoming and outgoing arrows is the most central element of the map.

Example head Contribution central to social improvement Damage on the Damage to inhabitants of the the historical surrounding area texture of the by crossing region Construction time Possibility of increasing employment through Suitability for the creating jobs transportation policy Cost of nationalization Facility in constructing (the topographic structure of the crossing area and the surrounding land, etc) Suitability for urban, regional and national Financial damage in progress plans tail case of accidents during operation

Heads and tails



- Heads will usually be "goal" type statements: expressions of desired or not-desired outcomes,
- Tails will be "options".
- When goals are expressed as not-desired outcomes, sometimes indicating disasters to be avoided at all costs, they are referred to as "negative-goals".
- Usually the map will contain more goal statements than those shown by heads, and more options than those shown by tails.

Structural properties

• When a cognitive map is pictured in graph form it is then relatively easy to see how each of the concepts and causal relationships relate to each other, and to see the overall structure of the whole set of portrayed assertions" (Axelrod, 1976).





Problem/issue complexity



- Both cognitive scientists and organizational scientists have been fond of simple analyses of cognitive maps.
- These analyses are supposed to indicate the central features of a directed graph.
 - The first of these simple analyses explores the total number of nodes and the total number of arrows;
 - The second is concerned with "cognitive centrality" of particular nodes.

The extent of the map



- The more nodes (or concepts) are there in a map, the more complex is the map and the issue.
- The map, as model, acts as a device for establishing a mutual understanding of the issue.
- The number of concepts elicited during an interview is dependent upon the length of the interview and the skills of the interviewer.

The complexity of the map as a network



- An alternative analysis of issue complexity is to determine the ratio of arrows to concepts. A higher ratio indicates a densely connected map and supposedly a higher level of complexity.
- Ratios of 1.15 to 1.20 is fine for maps elicited from interviews.

Representation



- Graph
 - Helps to see the causal relationships between variables better
- Matrix
 - Allows mathematical analysis in en effective way.

Example: How can we motivate employees?

- Variables
 - Motivation
 - Salaries
 - Problems in the work environment
 - Good attitude of the employer
 - Good attitude of the colleagues
 - Career possibilities



Causal relationships between the variables



• positive (+)

salary → motivation

negative (-)

problems in the work environment $\xrightarrow{-}$ motivation

• no relationship

attitude of colleagues salary



How can we motivate employees?

	mtv.	sal.	env.	emp.	col.	car.
mtv.	0	0	0	0	0	0
sal.	+	0	0	0	0	0
env.	-	0	0	0	0	0
emp.	+	0	-	0	0	+
col.	+	0	0	0	0	0
car.	+	0	0	0	0	0

Motivation; Salaries; Problems in the work environment; Good attitude of the employer; Good attitude of the colleagues; Career possibilities



How can we motivate employees?



Matrix Algebra

- Valency Matrix
- Centrality
- Reachability Matrix



Valency Matrix



- The adjacency matrix
- V is a square matrix of n*n, where n is the total number of concept variables
- Entry displays the <u>direct</u> effect of the column variable on the row variable



 The valency matrix indicates only direct relations between concept variables, that is, concept linkage paths of length 1

Centrality



- The row sum of the absolute values of the elements of V for row *i* gives the <u>outdegree</u> (od) of variable *i*.
- The column sum of the absolute values of the elements of V for column *i* gives the *indegree* (id) of variable *i*.
- The sum of od_i and id_i gives the <u>total degree</u> of *i* (td_i) which is a useful operational measure of that variable's <u>cognitive centrality</u> in the opinion structure of the experts

Indirect effect

V_{ij}^{n} : for the path of length *n*, indirect effect of variable *i* on variable *j*





Indirect effect

Reachability of variable *i* on variable *j*



For the path of length 2, the cumulative indirect effects of variable *i* on variable *j* $V_{i,i}^2 = +3$ (Three paths +)

 $V_{i,j}^2 = +1$ (Two paths +, one path -)

 $V_{i,j}^2 = -1$ (Two paths -, one path +)

$$V_{i,i}^2 = -3$$
 (Three paths -)



Reachability Matrix



- R reflects the existence of indirect relations
- If the adjacency matrix contains no feedback loops, the cumulative indirect effects (R) are calculated as: R = V + V² ... + Vⁿ⁻¹
- The sum of the absolute values for row *i* of R shows the total number of variables reachable from variable *i*
- The sum of the absolute values for column *i* of R shows the total number of variables reaching variable *i*

Example





				1			1		-										
		sf	r	k	pp	t	sh	kar											
	sf	0	0	0	-1	0	0	0	1										
	r	0	0	0	1	0	0	0	1										
	k	0	0	0	0	1	0	0	1										
V	pp	0	0	0	0	0	1	0	1										
	t	0	0	0	0	0	1	0	1										
	sh	0	0	0	0	0	0	1	1										
	kar	0	0	0	0	0	0	0	0										
		0	0	0	2	1	2	1	6										
		sf	r	k	pp	t	sh	kar				sf	r	k	pp	t	sh	kar	
	sf	0	0	0	0	0	-1	0			sf	0	0	0	0	0	0	0	
	r	0	0	0	0	0	1	0			r	0	0	0	0	0	0	0	
	k	0	0	0	0	0	1	0			k	0	0	0	0	0	0	0	
\mathbf{V}^2	pp	0	0	0	0	0	0	1		V^4	pp	0	0	0	0	0	0	0	
	t	0	0	0	0	0	0	1		•	t	0	0	0	0	0	0	0	
	sh	0	0	0	0	0	0	0			sh	0	0	0	0	0	0	0	
	kar	0	0	0	0	0	0	0			kar	0	0	0	0	0	0	0	
				•••••••	^														
		sf	r	k	pp	t	sh	kar				sf	r	k	pp	t	sh	kar	
	sf	0	0	0	0	0	0	-1			sf	0	0	0	-1	0	-1	-1	3
	r	0	0	0	0	0	0	1			r	0	0	0	1	0	1	1	3
	k	0	0	0	0	0	0	1			k	0	0	0	0	1	1	1	3
V^3	pp	0	0	0	0	0	0	0		R	pp	0	0	0	0	0	1	1	2
-	t	0	0	0	0	0	0	0			t	0	0	0	0	0	1	1	2
	sh	0	0	0	0	0	0	0			sh	0	0	0	0	0	0	1	1
	kar	0	0	0	0	0	0	0			kar	0	0	0	0	0	0	0	0
			·				·					0	0	0	2	1	5	6	14

Example



		sis	sg	m	sf	hs	by	çmy				sis	sg	m	sf	hs	by	çmy
	sis	0	0	1	0	0	0	1	2		sis	0	0	1	0	-1	0	1
	sg	1	0	0	0	0	0	0	1		sg	1	0	0	0	0	-1	0
	m	0	1	0	1	0	0	0	2		m	1	1	1	1	0	1	1
V	sf	0	0	0	0	-1	-1	0	2	V^4	sf	0	1	1	1	0	1	1
	hs	-1	0	0	0	0	0	0	1		hs	-1	0	0	0	0	1	0
	by	0	0	0	0	1	0	0	1		by	0	-1	0	-1	0	-1	0
	çmy	0	0	0	0	0	1	0	1		çmy	0	0	-1	0	0	0	-1
		2	1	1	1	2	2	1										
	ļ			ļ	ļ	ļ		ļ										
		sis	sg	m	sf	hs	by	çmy				sis	sg	m	sf	hs	by	çmy
	sis	0	1	0	1	0	1	0			sis	1	1	0	1	0	1	0
	sg	0	0	1	0	0	0	1			sg	0	0	1	0	-1	0	1
	m	1	0	0	0	-1	-1	0			m	1	1	1	1	0	0	1
\mathbf{V}^2	sf	1	0	0	0	-1	0	0		\mathbf{V}^{5}	sf	1	1	0	1	0	0	0
	hs	0	0	-1	0	0	0	-1			hs	0	0	-1	0	1	0	-1
	by	-1	0	0	0	0	0	0			by	-1	0	0	0	0	1	0
	çmy	0	0	0	0	1	0	0			çmy	0	-1	0	-1	0	-1	0
				ļ	ļ	ļ												ļ
		sis	sg	m	sf	hs	by	çmy				sis	sg	m	sf	hs	by	çmy
	sis	1	0	0	0	0	-1	0			sis	1	0	1	0	0	-1	1
	sg	0	1	0	1	0	1	0			sg	1	1	0	1	0	1	0
	m	1	0	1	0	-1	0	1			m	1	1	1	1	-1	0	1
V^3	sf	1	0	1	0	0	0	1		 V ⁶	sf	1	0	1	0	-1	-1	1
	hs	0	-1	0	-1	0	-1	0			hs	-1	-1	0	-1	0	-1	0
	by	0	0	-1	0	0	0	-1			by	0	0	-1	0	1	0	-1
	çmy	-1	0	0	0	0	0	0			çmy	-1	0	0	0	0	1	0

Construction of the Group Cognitive Map



- Gathering a list of related concepts about the issue on hand from different persons
- Preparing a collective list of concepts
- Persons' judgments to reveal the relationships between the concepts
- Construction of personal cognitive maps
- Aggregating personal cognitive maps
 - Single number of experts
 - Taking experts' opinions again about the doubtful relations

• Size

• Over 100 nodes on the map



Hierarchy of decisions



- The most fundamental decisions are
 - Definition of customer service (1)
 - Forecasts of demand (8)
 - Product routing (14)
 - Information to be provided with the product (32)
- The rest of the decisions cannot be taken unless these 4 decisions are given

Definition of customer service The 'view' of the part of the cognitive map showing the fundamental decision 'definition of customer service' 42 Stock location 23 Transportation modes 9 Inventory management strategy 18 Procurement type 15 Facilities lavout 6 C&I network strategy 12 Desired inventory level A PF network strategy 7 40 Warehousing 3 Degree of vertical mission and integration and functions outsourcing 2 Customer service objectives 1 Definition of 34

customer service



Domain Analysis (Centrality)

Centrality score	Decision
11	2 Customer service objectives
9	5 PF network design
8	41 Warehouse layout
	12 Desired inventory level
	20 Suppliers
7	36 Unit loads
	37 Types of material handling equipment
	47 Order picking procedures
	6 C&I network strategy
	9 Inventory management strategy
	17 Production scheduling
6	23 Transportation modes
	35 Packaing design
	43 Receiving/shipping dock design

Cluster Analysis



- Islands of themes
 - without accounting for hierarchy
- Nodes in each cluster \rightarrow tightly linked
- Bridges with other clusters \rightarrow minimized



Hierarchical Clusters



Potent Options







Cluster Analysis (Cluster I)





Cluster Analysis (Cluster II)

