

ADVANCED PROPULSION SYSTEM – MID-TERM EXAM

21/11/2008 - 13:30-14:15

Asses the quality of the wake given below according to the BMT's wake non-uniformity criteria (w_Δ , σ_{nl}) given in figure 1. **(15 Points)**

Given:

$$D = 4800 \text{ mm (propeller diameter)}$$

$$N = 120 \text{ (number of propeller revolution per minute - RPM)}$$

$$Z = 4 \text{ (number of blades)}$$

$$Z_p = 2700 \text{ mm (shaft height from the base line)}$$

$$T_a = 7.70 \text{ m (Draft at the aft perpendicular)}$$

$$P_a = 100000 \text{ Pa (Atmospheric Pressure)}$$

$$P_v = 1700 \text{ Pa (Vapour Pressure)}$$

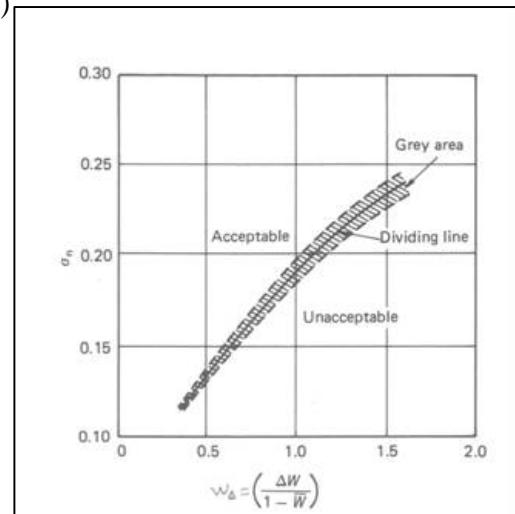
$$\rho = 1025 \text{ kg/m}^3 \text{ (Density of sea water)}$$

$$g = 9.80665 \text{ m/sn}^2 \text{ (Acceleration of gravity)}$$

$$\sigma_{nl} = \frac{P_a - P_v + P_H}{\frac{1}{2} \rho (\pi n D)^2}$$

$$P_H = \text{Hydrostatic pressure at the propeller tip}$$

$$w_\Delta = \left(\frac{\Delta w}{1 - \bar{w}} \right)_{1.0R}$$



The wake is given in the following table.

| ANGLE | Wake Velocity Ratios – V_x/V_s | | | | | | | |
|-------|----------------------------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| | 0 | 0.053 | 0.158 | 0.110 | 0.122 | 0.216 | 0.240 | 0.267 |
| 10 | 0.075 | 0.139 | 0.113 | 0.122 | 0.201 | 0.293 | 0.361 | 0.422 |
| 20 | 0.093 | 0.126 | 0.107 | 0.136 | 0.214 | 0.310 | 0.389 | 0.471 |
| 30 | 0.108 | 0.123 | 0.102 | 0.158 | 0.238 | 0.333 | 0.443 | 0.565 |
| 40 | 0.114 | 0.125 | 0.105 | 0.175 | 0.268 | 0.381 | 0.495 | 0.590 |
| 50 | 0.114 | 0.124 | 0.121 | 0.212 | 0.337 | 0.492 | 0.596 | 0.658 |
| 60 | 0.111 | 0.119 | 0.161 | 0.308 | 0.438 | 0.584 | 0.655 | 0.685 |
| 70 | 0.109 | 0.119 | 0.216 | 0.421 | 0.520 | 0.619 | 0.682 | 0.726 |
| 80 | 0.109 | 0.136 | 0.272 | 0.508 | 0.603 | 0.669 | 0.733 | 0.808 |
| 90 | 0.112 | 0.173 | 0.328 | 0.572 | 0.691 | 0.720 | 0.771 | 0.898 |
| 100 | 0.116 | 0.215 | 0.392 | 0.618 | 0.736 | 0.763 | 0.800 | 0.916 |
| 110 | 0.121 | 0.238 | 0.447 | 0.666 | 0.757 | 0.805 | 0.837 | 0.938 |
| 120 | 0.123 | 0.239 | 0.479 | 0.730 | 0.803 | 0.866 | 0.884 | 0.947 |
| 130 | 0.123 | 0.228 | 0.494 | 0.773 | 0.853 | 0.922 | 0.940 | 0.951 |
| 140 | 0.122 | 0.214 | 0.503 | 0.789 | 0.899 | 0.956 | 0.974 | 0.988 |
| 150 | 0.119 | 0.196 | 0.494 | 0.775 | 0.925 | 0.974 | 0.986 | 0.994 |
| 160 | 0.109 | 0.179 | 0.460 | 0.727 | 0.924 | 0.977 | 0.988 | 0.992 |
| 170 | 0.091 | 0.170 | 0.399 | 0.639 | 0.896 | 0.965 | 0.990 | 0.999 |
| 180 | 0.067 | 0.168 | 0.329 | 0.536 | 0.850 | 0.928 | 0.971 | 0.996 |
| r/R | 0.146 | 0.292 | 0.438 | 0.583 | 0.729 | 0.875 | 1.021 | 1.167 |

Here 0° – Top dead centre – 180° – bottom death centre

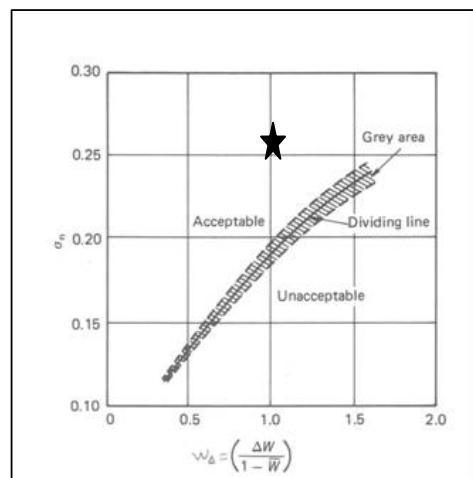
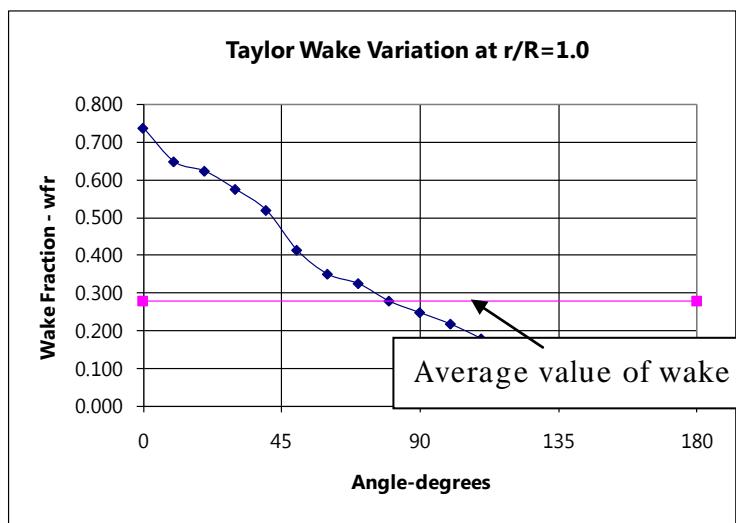
SOLUTION

First calculate the cavitation parameter σ_{NI} ,

$$\sigma_{nl} = \frac{100000 - 1700 + 9.80665 \times 1025 \times \left(7.70 - \frac{4.8}{2} - 2.7 \right)}{\frac{1}{2} \times 1025 \times \left(\pi \times \frac{120}{60} \times 4.8 \right)^2} = \frac{124434.7223}{466161.1551} = 0.267$$

Second calculate the wake parameter

$$w_\Delta = \left(\frac{\Delta w}{1 - \bar{w}} \right)_{1.0R} = \left(\frac{0.737 - 0.011}{1 - 0.277} \right)_{1.0R} = \frac{0.726}{0.723} = 1.004$$



| ANGLE | w(1.0r) | SM | Mult. |
|-------|---------|--------|--------|
| 0 | 0.737 | 1 | 0.737 |
| 10 | 0.648 | 4 | 2.591 |
| 20 | 0.623 | 2 | 1.246 |
| 30 | 0.575 | 4 | 2.298 |
| 40 | 0.519 | 2 | 1.037 |
| 50 | 0.413 | 4 | 1.652 |
| 60 | 0.349 | 2 | 0.699 |
| 70 | 0.324 | 4 | 1.297 |
| 80 | 0.278 | 2 | 0.556 |
| 90 | 0.247 | 4 | 0.989 |
| 100 | 0.217 | 2 | 0.433 |
| 110 | 0.178 | 4 | 0.710 |
| 120 | 0.125 | 2 | 0.250 |
| 130 | 0.062 | 4 | 0.246 |
| 140 | 0.028 | 2 | 0.056 |
| 150 | 0.015 | 4 | 0.061 |
| 160 | 0.013 | 2 | 0.025 |
| 170 | 0.011 | 4 | 0.045 |
| 180 | 0.033 | 1 | 0.033 |
| | | Sum= | 14.961 |
| | | Area= | 0.870 |
| | | Mean = | 0.277 |

