

## MOS AKTİF DİRENÇ

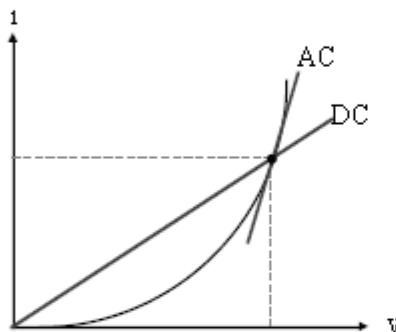
### Gerçekleştirme



**DS kısadevre, eleman  
doymada**

$$\begin{aligned} v_{DS} &\geq v_{GS} - V_T \\ v_D - v_S &\geq v_G - v_S - V_T \\ \therefore v_{DG} &\geq -V_T \text{ where } V_T > 0 \end{aligned}$$

### I-V Karakteristiği



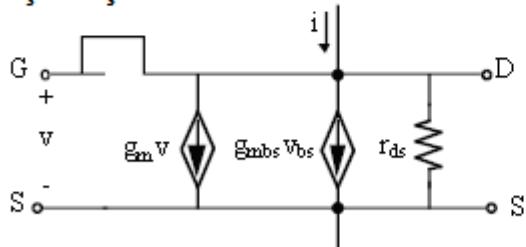
### Büyük İşaret Davranışı

$$\begin{aligned} i &= i_D = \left( \frac{K'W}{2L} \right) [v_{GS} - V_T]^2 \\ &= \frac{\beta}{2} (v_{GS} - V_T)^2, \quad \lambda \text{ ihmali} \end{aligned}$$

veya

$$v = v_{DS} = v_{GS} = V_T + \sqrt{\frac{2i_D}{\beta}}$$

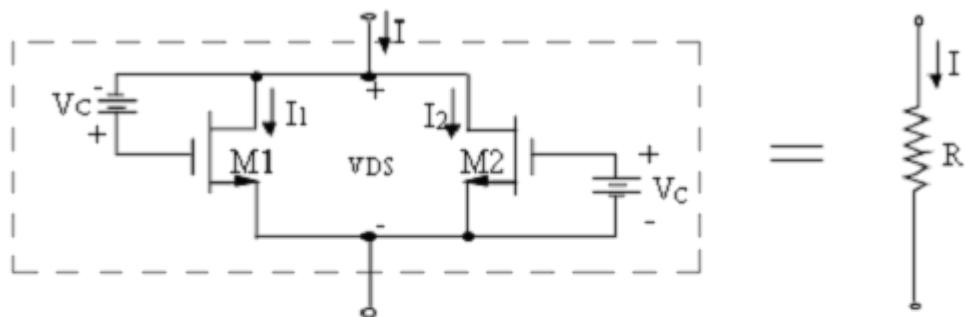
### Küçük İşaret



$$\begin{aligned} V_{BS} &= 0, \quad R_{OUT} = \frac{v}{i} = \frac{1}{g_M + g_{DS}} \approx \frac{1}{g_M} \\ V_{BS} &\neq 0? \end{aligned}$$

**genel olarak**  $g_m \approx 10$   $g_{mbs} \approx 100$   $g_{ds}$

## Aktif Direncin Dinamik Aralığının Genişletilmesi



**Her iki elemanın doymasız bölgede çalıştığı kabul edilirse**

$$I_1 = \beta_1 \left[ (v_{DS} + V_C - V_T)v_{DS} - \frac{v_{DS}^2}{2} \right]$$

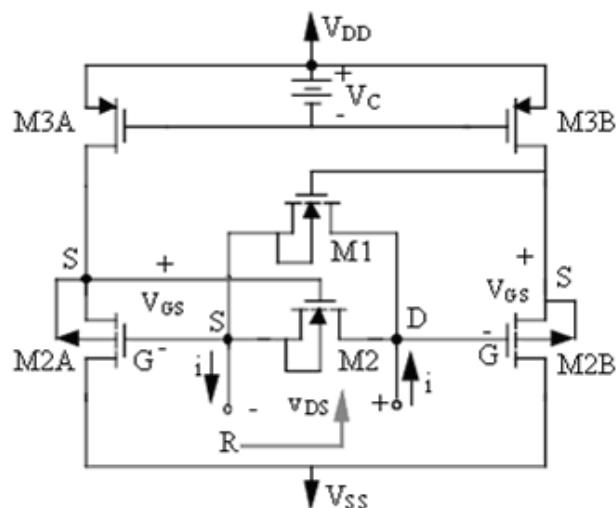
$$I_2 = \beta_2 \left[ (V_C - V_T)v_{DS} - \frac{v_{DS}^2}{2} \right]$$

$$I = I_1 + I_2 = \beta \left[ v_{DS}^2 + (V_C - V_T)v_{DS} - \frac{v_{DS}^2}{2} + (V_C - V_T)v_{DS} - \frac{v_{DS}^2}{2} \right]$$

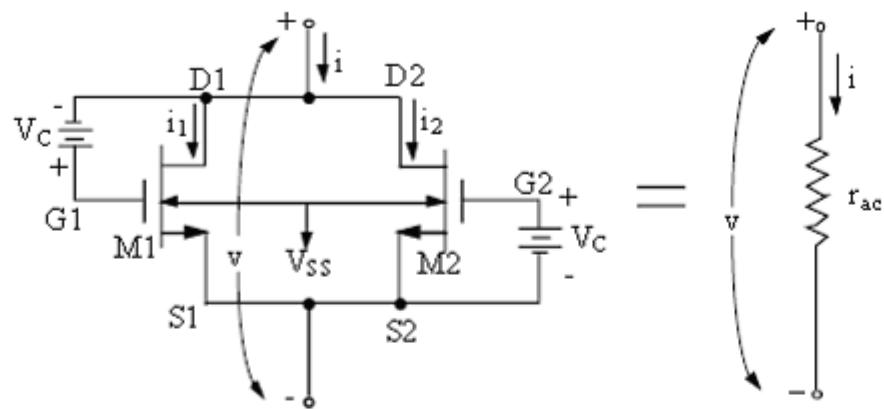
$$I = 2\beta(V_C - V_T)v_{DS}$$

$$R = \frac{1}{2\beta(V_C - V_T)}$$

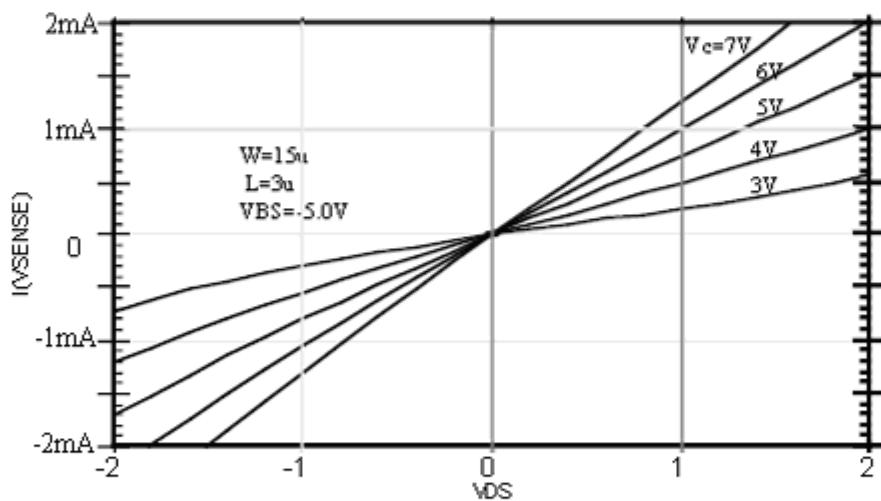
## Gerçekleştirme



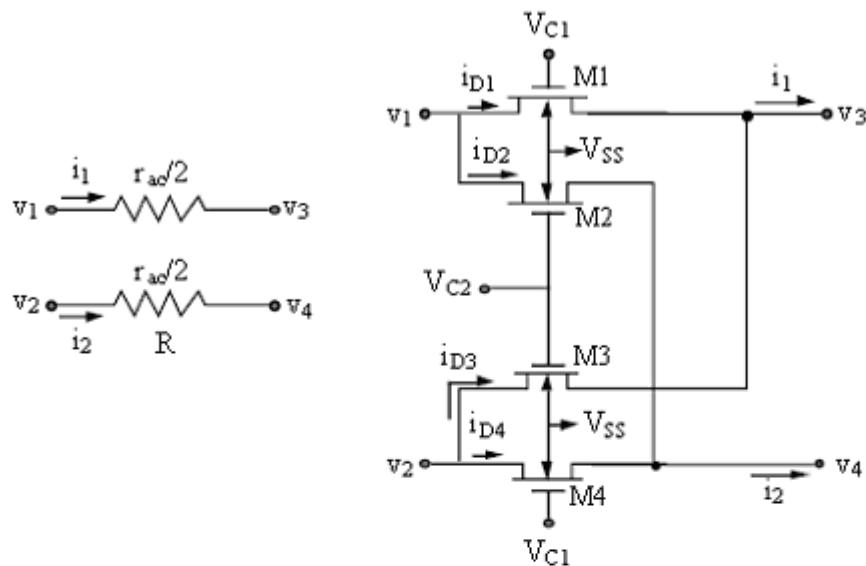
## NMOS paralel tranzistorlarla gerçekleştirme



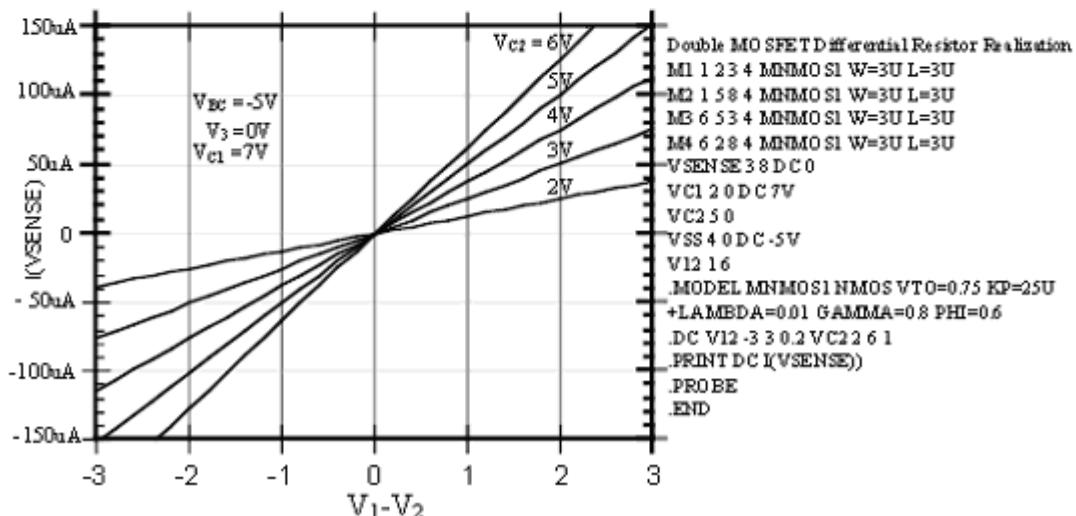
## Gerilim-Akım Karakteristiği



## Çift MOSFET ile Farksal Direnç Gerçekleştirme



### Gerilim-Akım Karakteristiği

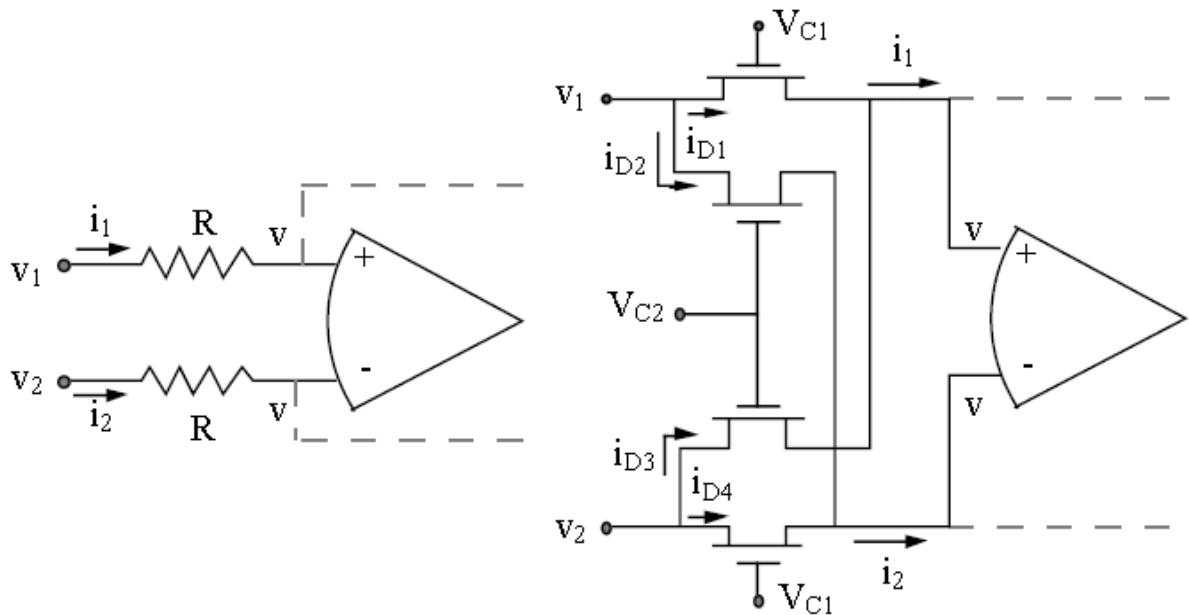


\*

$$R_{in} = \frac{v_1 - v_2}{i_1 - i_2} = \frac{v_1 - v_2}{\beta(V_{C1} - V_{C2})(v_1 - v_2)} = \frac{1}{\frac{Kw}{L}(V_{C1} - V_{C2})}$$

$R_{in} = \frac{1}{\frac{Kw}{L}(V_{C1} - V_{C2})}$

$v_1, v_2 \leq \min [(V_{C1} - V_T), (V_{C2} - V_T)]$



$$i_{D1} = \beta \left[ (V_{C1} - v - V_T)(v_1 - v) - \frac{1}{2}(v_1 - v)^2 \right]$$

$$i_{D2} = \beta \left[ (V_{C2} - v - V_T)(v_1 - v) - \frac{1}{2}(v_1 - v)^2 \right]$$

$$i_{D3} = \beta \left[ (V_{C1} - v - V_T)(v_2 - v) - \frac{1}{2}(v_2 - v)^2 \right]$$

$$i_{D4} = \beta \left[ (V_{C2} - v - V_T)(v_2 - v) - \frac{1}{2}(v_2 - v)^2 \right]$$

$$i_1 = i_{D1} + i_{D3} = \beta \left[ (V_{C1} - v - V_T)(v_1 - v) - \frac{1}{2}(v_1 - v)^2 + (V_{C2} - v - V_T)(v_2 - v) - \frac{1}{2}(v_2 - v)^2 \right]$$

$$i_2 = i_{D2} + i_{D4} = \beta \left[ (V_{C2} - v - V_T)(v_1 - v) - \frac{1}{2}(v_1 - v)^2 + (V_{C1} - v - V_T)(v_2 - v) - \frac{1}{2}(v_2 - v)^2 \right]$$

$$i_1 - i_2 = \beta [ (V_{C1} - v - V_T)(v_1 - v) + (V_{C2} - v - V_T)(v_2 - v) - (V_{C2} - v - V_T)(v_1 - v) - (V_{C1} - v - V_T)(v_2 - v) ]$$

$$= \beta [ v_1(V_{C1} - V_{C2}) + v_2(V_{C2} - V_{C1}) ] = \beta (V_{C1} - V_{C2})(v_1 - v_2)$$

$$R_{in} = \frac{v_1 - v_2}{i_1 - i_2} = \frac{v_1 - v_2}{\beta (V_{C1} - V_{C2})(v_1 - v_2)} = \frac{1}{\frac{KW}{L}(V_{C1} - V_{C2})}$$

$$R_{in} = \frac{V_1 - V_2}{I_1 - I_2} = \frac{V_1 - V_2}{\beta(V_{C1} - V_{C2})(V_1 - V_2)} = \frac{1}{\frac{KW}{L}(V_{C1} - V_{C2})}$$

$$\boxed{R_{in} = \frac{1}{\frac{KW}{L}(V_{C1} - V_{C2})}} \quad V_1, V_2 \leq \min [ (V_{C1} - V_T), (V_{C2} - V_T) ]$$

### **Kaynaklar:**

P.E. Allen and D.R. Holberg, CMOS analog circuit design (Second Edition), Oxford University Press, New York Oxford, 2002.