

Novel High Precision Current-mode Multiplier/Divider

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INTRODUCTION

- In this paper, a method to reduce the second order effects on the circuit performances caused by the small sized MOS transistors is proposed and a squarer/divider circuit is designed using this method.

INTRODUCTION

- **Due to the decrease in dimensions of MOS transistor in IC fabrication technology**
- the MOS transistor voltage–current relationship deviates from square-law.
- second order effects like short channel effect cause more errors in the MOSFET performance.

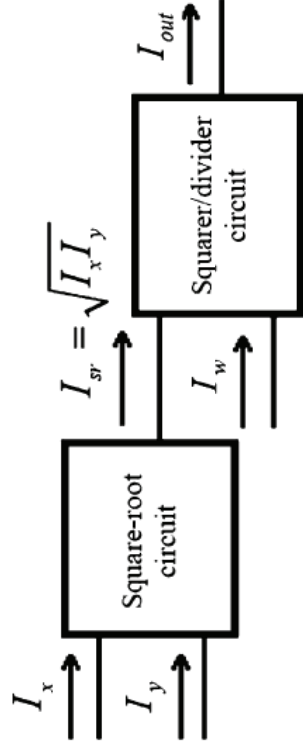
INTRODUCTION

- In this paper, a **method** is proposed to reduce the errors generated by the second order effects in the current-mode circuits with using MOS translinear loop.
- The output current function of the proposed circuit can be controlled by a control voltage.
- The proposed method enables the use of much smaller transistors and the circuits to be designed are smaller than their counterparts. Thus they may be operated at much higher frequencies.

INTRODUCTION

- **Where is the proposed circuit can be used?**
- filtering in square-root domain,
- fuzzy logic controllers,
- artificial neural networks,
- modulators,
- phase discriminators,
- adaptive filters,
- RMS-DC converters,
- sine/cosine synthesizers,
- cryptography systems, etc.

Current-mode multiplier/divider circuit



Since I_x and I_y are the input currents of the square-root circuit, the output function of the first circuit can be written as

$$I_{sr} = \sqrt{I_x I_y}$$

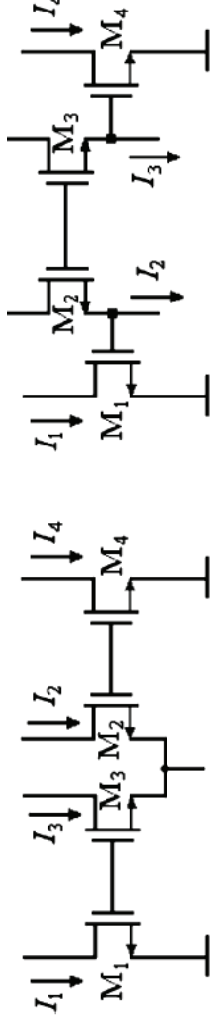
Figure 1. Simplified diagram of the multiplier/divider circuit

Assuming that this current is the one of the input currents and applying a second I_w to the input, the output current of the whole circuit can be expressed as

$$I_{out} = \frac{I_{in}^2}{I_w} = \frac{(\sqrt{I_x I_y})^2}{I_w} = \frac{I_x I_y}{I_w}$$

- In order to implement a multiplier/divider circuit, square-root and squarer/divider circuits must be designed

Current-mode multiplier/divider circuit



Both square root circuit and squarer/divider circuit can be obtained by using either the up-down or stacked voltage translinear (VTL) loops

Figure 2. a) Up-down VTL loop b) Stacked VTL loop

- Assuming that the aspect ratios of the transistors satisfy

$$\beta_1 = \beta_2 = \beta \text{ and } \beta_3 = \beta_4 = 2\beta$$

- using the VTL law $V_{GS1} + V_{GS2} = V_{GS3} + V_{GS4}$
- Assuming that the second order effects are negligible $I_D = \frac{\beta}{2}(V_{GS} - V_T)^2$

- Assuming that the V_{th} of MOSFETs are same $\sqrt{\frac{2I_1}{\beta}} + \sqrt{\frac{2I_2}{\beta}} = \sqrt{\frac{2I_3}{2\beta}} + \sqrt{\frac{2I_4}{2\beta}}$

Current-mode multiplier/divider circuit

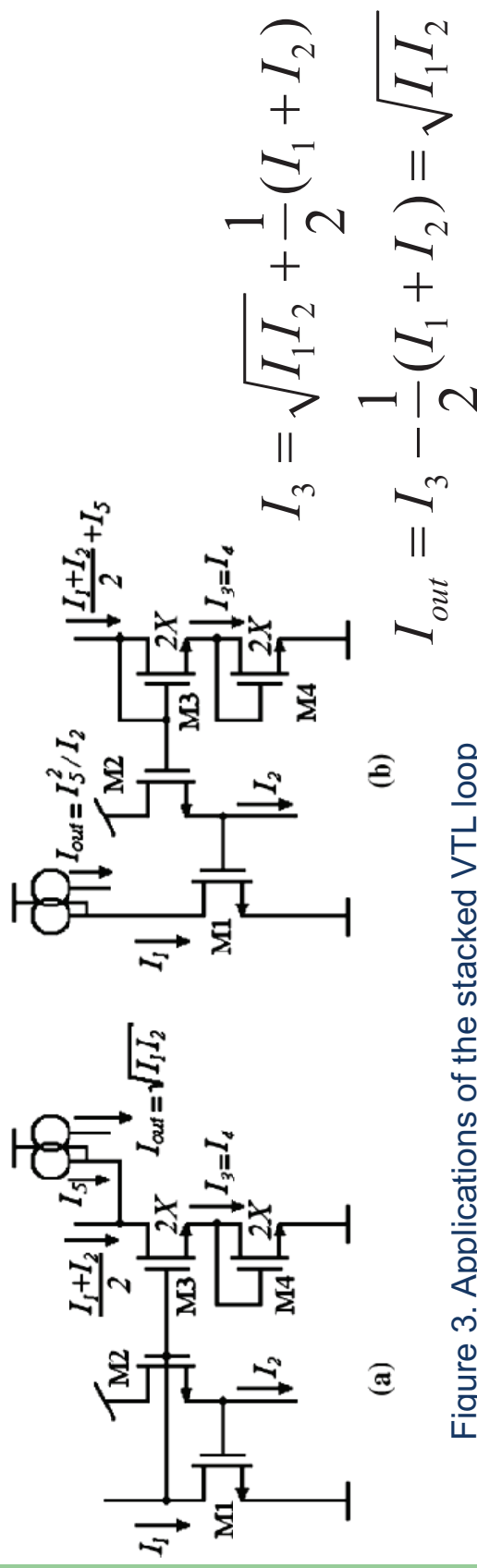
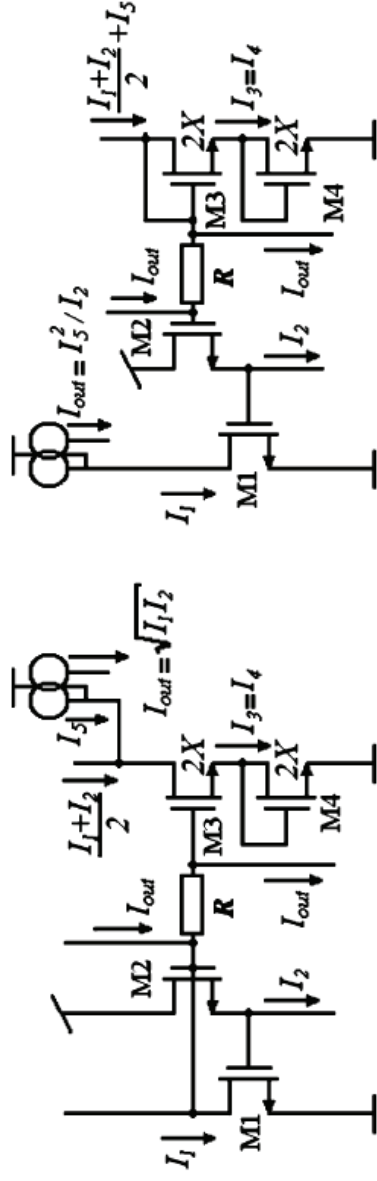


Figure 3. Applications of the stacked VTL loop
 (a) Square-root cell (b) Squarer/divider cell.

- a square-root circuit can be obtained as shown in (a) if I_1 and I_2 are the input currents and the output current is a copy of I_5 .
- a squarer/divider circuit can be obtained as shown in (b) if the output is a copy of either I_1 or I_2 and the inputs are the remaining two currents.

Proposed current-mode multiplier/divider circuit



(a) square-root cell (b) squarer/divider cell

- The error of the output current function can be reduced using the resistance R between the gates of the MOS transistors $M2$, $M3$ and letting the output current flow through this resistance. In this case, a new voltage term that is added to the VTL loop function which eliminates the error of the output current function.

Due to the second order effects small sized MOS transistors do not operate properly and therefore errors may occur in the output current function.

Proposed current-mode multiplier/divider circuit

- with using the VTL law at figure 4

$$V_{GS1} - V_{TH1} + V_{GS2} - V_{TH2} = I_{out} \cdot R + V_{GS3} - V_{TH3} + V_{GS4} - V_{TH4}$$

- If the mobility reduction is taken into consideration, the drain current of a MOS transistor operated in saturation is given by

$$I_D = \frac{\beta}{2} \frac{(V_{GS} - V_{TH})^2}{1 + \theta' (V_{GS} - V_{TH})} \quad V_{GS} - V_{TH} = \frac{I_D \theta'}{\beta} + \sqrt{\left(\frac{I_D \theta'}{\beta}\right)^2 + \frac{2I_D}{\beta}}$$

$$\left(\frac{I_D \theta'}{\beta}\right)^2 \square \frac{2I_D}{\beta} \quad V_{GS} - V_{TH} \approx \frac{I_D \theta'}{\beta} + \sqrt{\frac{2I_D}{\beta}}$$

$$\frac{I_1 \theta'}{\beta} + \sqrt{\frac{2I_1}{\beta}} + \frac{I_2 \theta'}{\beta} + \sqrt{\frac{2I_2}{\beta}} = I_{out} \cdot R + \frac{I_3 \theta'}{2\beta} + \sqrt{\frac{I_3}{\beta}} + \frac{I_4 \theta'}{2\beta} + \sqrt{\frac{I_4}{\beta}}$$

Proposed current-mode multiplier/divider circuit

- As shown in Figure 4, $I_3=I_4$:
$$\frac{I_1\theta'}{\beta} + \sqrt{\frac{2I_1}{\beta}} + \frac{I_2\theta'}{\beta} + \sqrt{\frac{2I_2}{\beta}} = I_{out} \cdot R + \frac{I_3\theta'}{\beta} + 2\sqrt{\frac{I_3}{\beta}}$$
- Using KCL equation at the output node of the modified square root cell
$$I_3 = \sqrt{I_1I_2} + \frac{1}{2}(I_1 + I_2) \Rightarrow I_3 = \frac{1}{2} \left[\sqrt{I_1} + \sqrt{I_2} \right]^2$$
- Multiplying $4/\beta$ each term and taking the square root on both sides,

$$\sqrt{\frac{2I_1}{\beta}} + \sqrt{\frac{2I_2}{\beta}} = 2\sqrt{\frac{I_3}{\beta}}$$
$$I_{out} \cdot R = \frac{\theta'}{\beta}(I_1 + I_2 - I_3) \quad R = \frac{\theta'}{\beta} \left[\frac{I_1 + I_2}{2\sqrt{I_1I_2}} - 1 \right]$$

Proposed current-mode multiplier/divider circuit

- Considering the mobility reduction effect, this equation indicated that the value of the resistance R to decrease the output current function error of the circuit.
- This equation can be expressed as

$$\sqrt{I_1 I_2} = (I_1 + I_2) \frac{\theta'}{2(\beta \cdot R + \theta')}$$

- E is defined as

$$E = \frac{\sqrt{I_1 I_2}}{I_1 + I_2} \frac{2(\beta \cdot R + \theta')}{\theta'}$$

Proposed current-mode multiplier/divider circuit

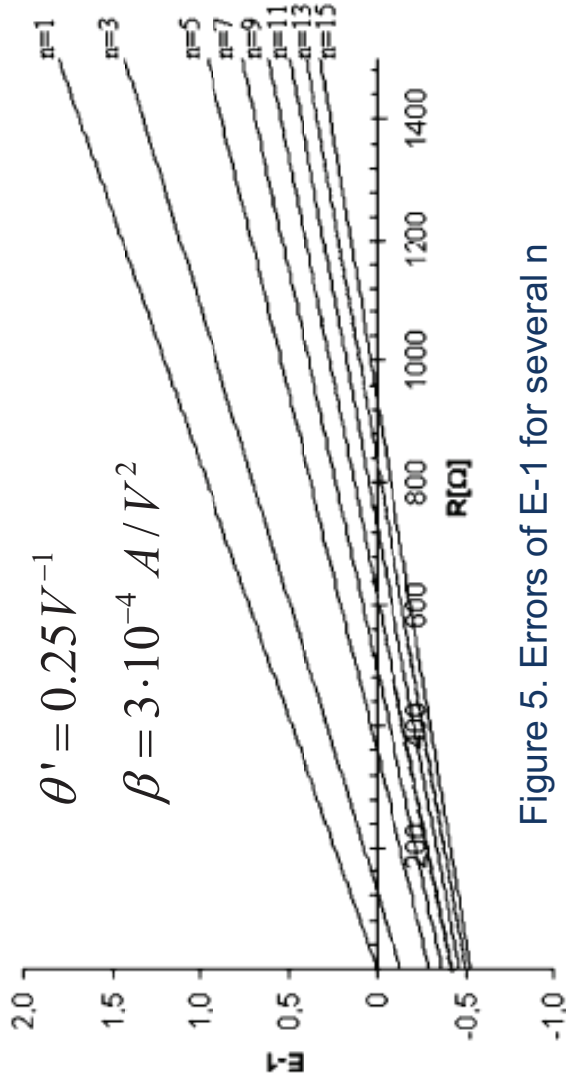


Figure 5. Errors of E-1 for several n

- If $I_2 = nI_1$, then the E-1 error function is drawn in Figure 5.
- When input currents, I_1 and I_2 are equal ($n = 1$) output current function error generated by mobility reduction will be zero. the resistance R value will be zero.
- As the difference between two input currents (I_1, I_2) increases, the value of the resistance R which will compensate for the error will also increase.

Proposed current-mode multiplier/divider circuit

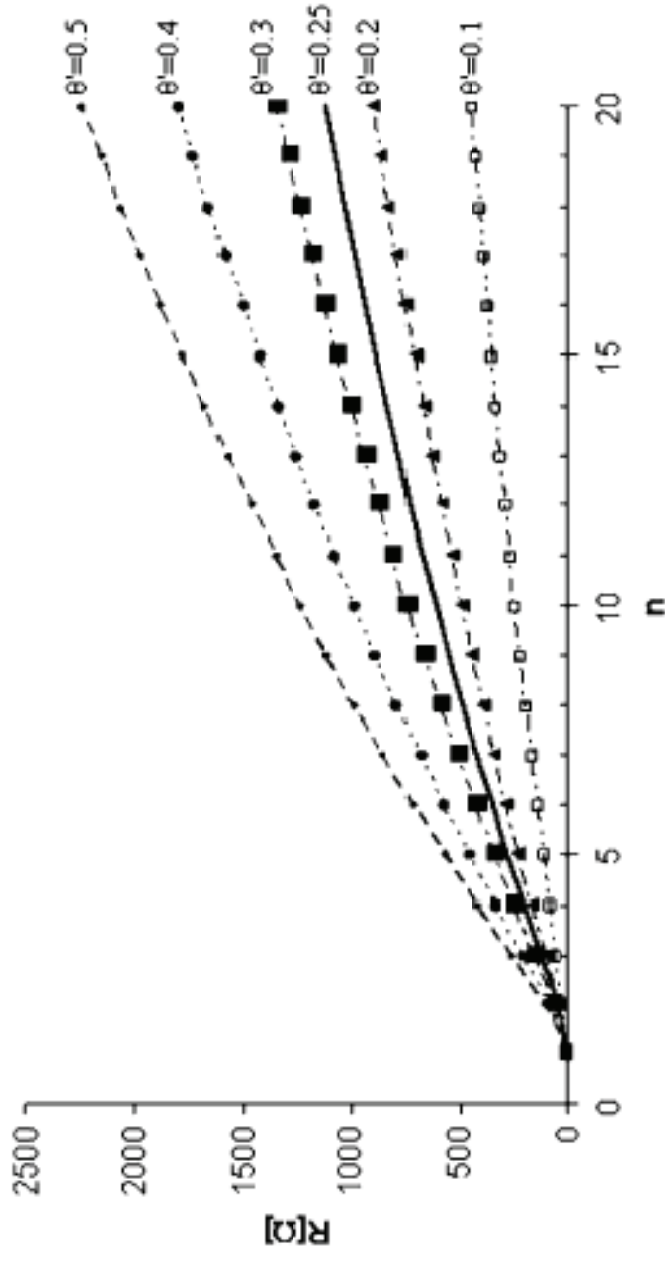


Figure 6. Variation in resistance R value with respect to n corresponding to different θ'

- As θ' increases, error generated by circuit increases as well as the value of the resistance which will compensate for it.

Proposed Circuit

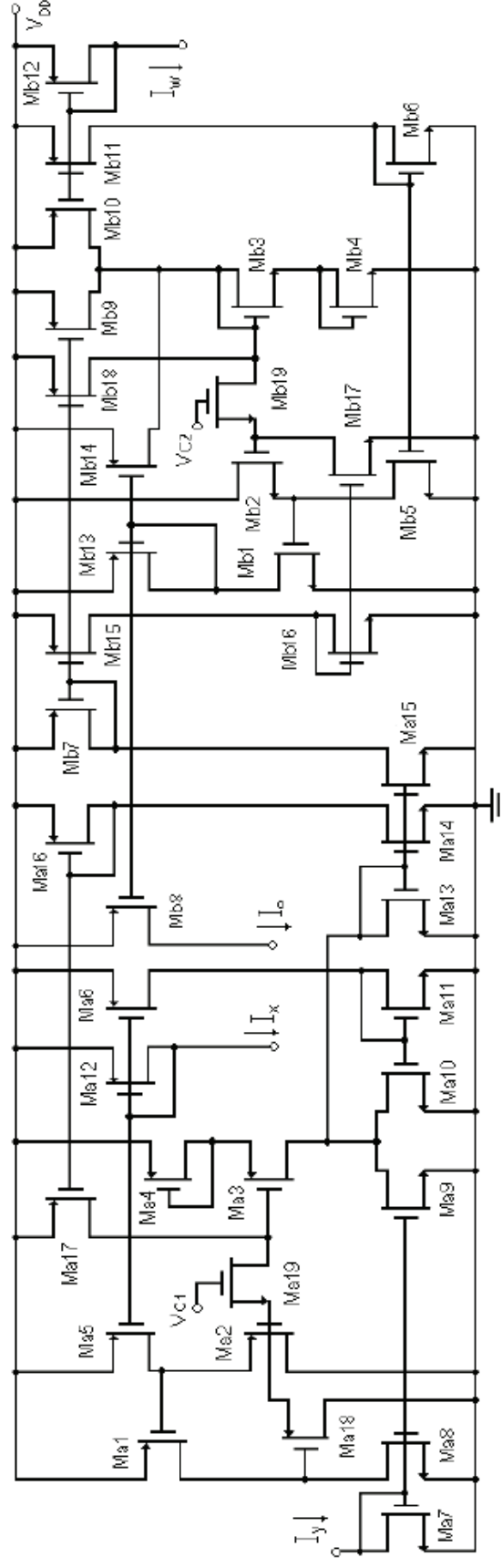


Figure 7. Proposed current-mode multiplier/divider circuit

- Resistances are realized with the transistors in Figure 7 and their value can be controlled by the VC control voltages. By this way output current function of the circuit can be controlled and the function errors of the current can be eliminated.

Proposed Circuit

- The output current function error of the square-root circuit that forms the left part of the circuit is reduced by the current flowing over the resistor R1. This process is carried out by flowing output current over the transistors Ma14, Ma16, Ma17, Ma18.
- The output current function error of the squarer/divider circuit that forms the right part of the circuit is reduced by the current flowing over the resistor R2. Mb15, Mb16, Mb17, Mb18 are used to provide the correction current flowing over the R2 resistor.

Simulation results

Table 1. Transistor dimensions

	W/L (μm)	Ma11 Ma12 Ma13 Ma14 Ma15 Ma16 Ma17 Ma18 Ma19 Ma10	W/L (μm)	Mb1 Mb2 Mb3 Mb4 Mb5 Mb6 Mb7 Mb8 Mb9 Mb10	W/L (μm)	Mb11 Mb12 Mb13 Mb14 Mb15 Mb16 Mb17 Mb18 Mb19	W/L (μm)
Ma1	6/7		12/7		12/7		12/7
Ma2	6/7		12/7		12/7		12/7
Ma3	12/7		12/7		24/7		12/7
Ma4	12/7		12/7		24/7		6/7
Ma5	12/7		12/7		12/7		12/7
Ma6	12/7		12/7		12/7		12/7
Ma7	12/7		12/7		12/7		12/7
Ma8	12/7		12/7		12/7		12/7
Ma9	6/7		10/7		12/7		80/7
Ma10	6/7				6/7		

- SPICE simulations were performed using TSMC 0.35 μm LEVEL 3 CMOS process parameters.
- The power supply voltage is 3V.

Simulation results

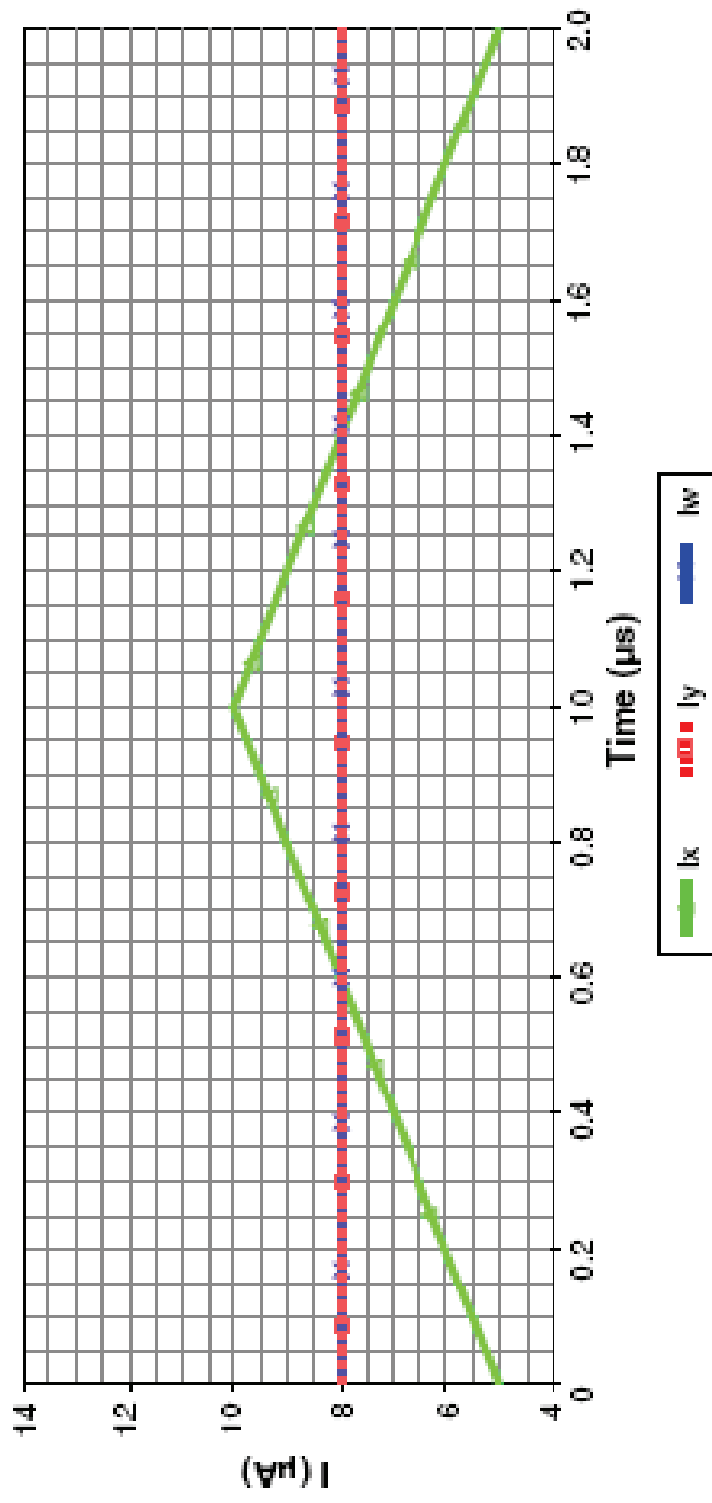
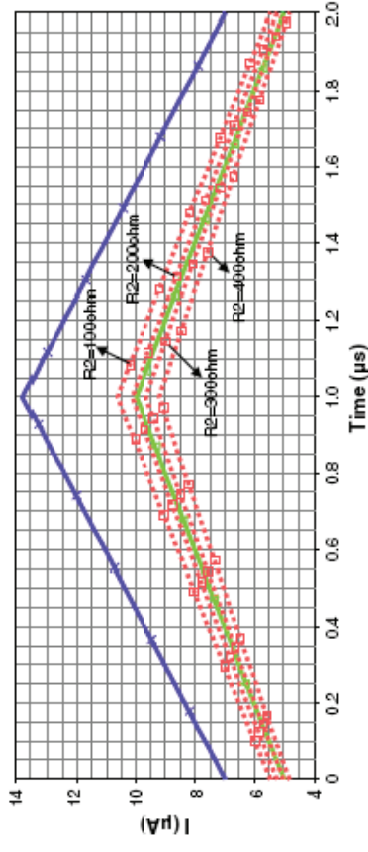
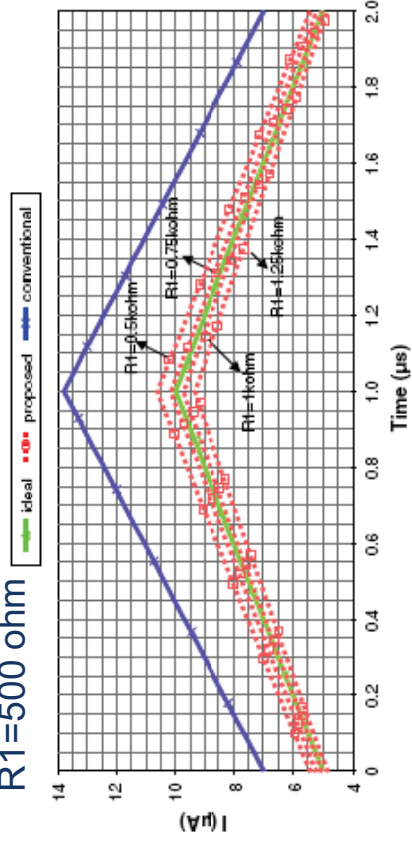


Figure 8. Input currents i_x , i_y and i_w of the proposed multiplier/divider

Simulation results



$R_1 = 500 \text{ ohm}$



$R_2 = 50 \text{ ohm}$

- As expected, for different values of the resistances R_1 and R_2 the output current function varies around the ideal curve.
- Because of the second order effects the output current function of the conventional circuit is different from the ideal curve.
- It is apparent that the error of the output current function can be reduced by choosing appropriate resistance values.

Figure 9. Comparison of the output currents and the ideal curve

Simulation results

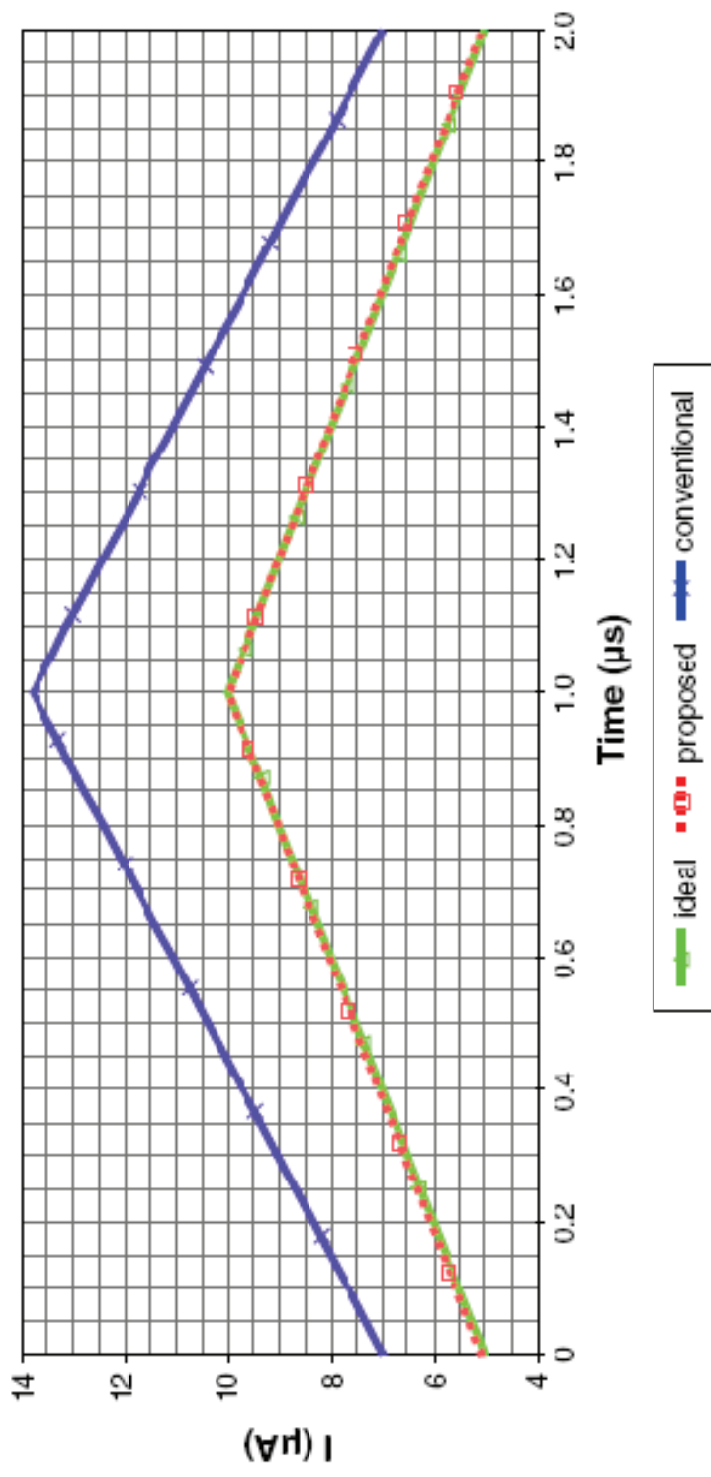
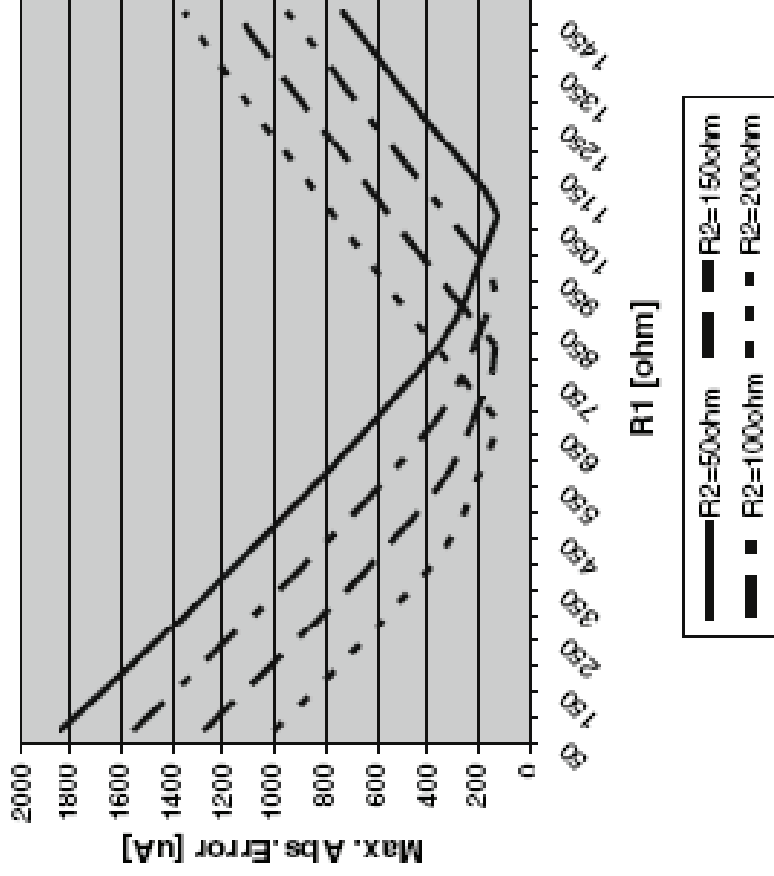


Figure 10. Comparison of the output currents and the ideal curve

- V_{C1} and V_{C2} are taken 2.09 V and 5 V.

Simulation results



- In Figure 11, it can be easily seen that the output current function error is reduced by changing the values of the resistances R_1 and R_2 .

Figure 11. Maximum absolute errors for different values of R1 and R2

Simulation results

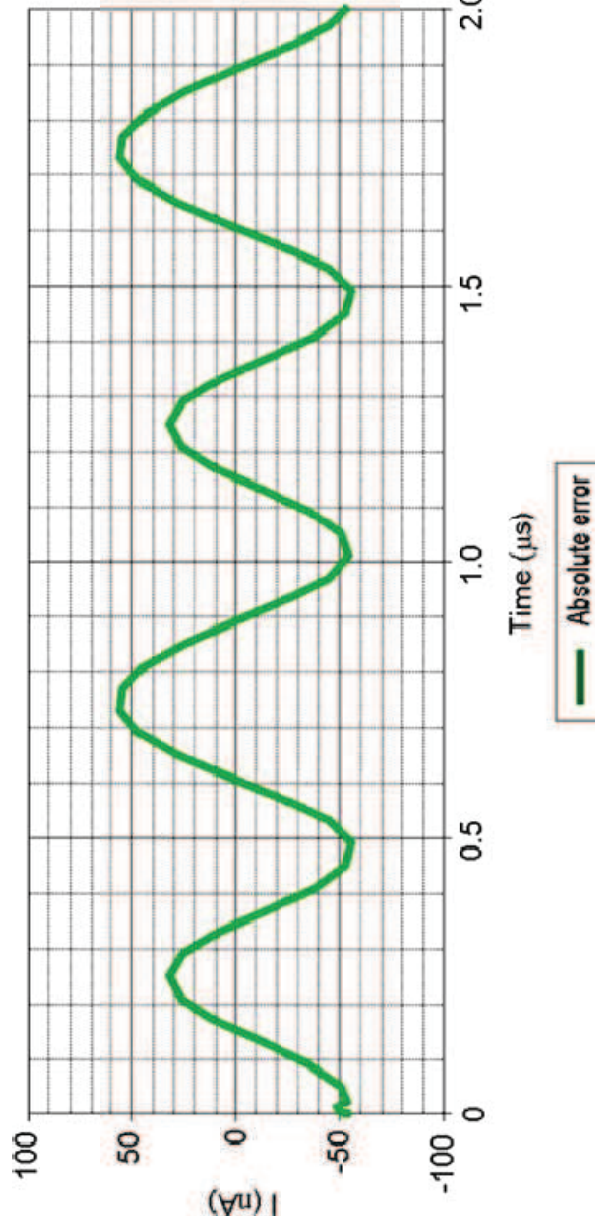
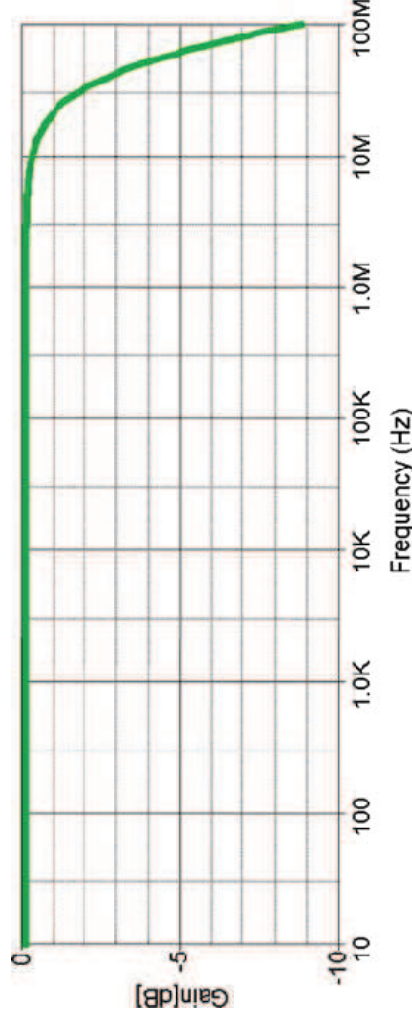


Figure 12. Simulated absolute error of the proposed multiplier/divider

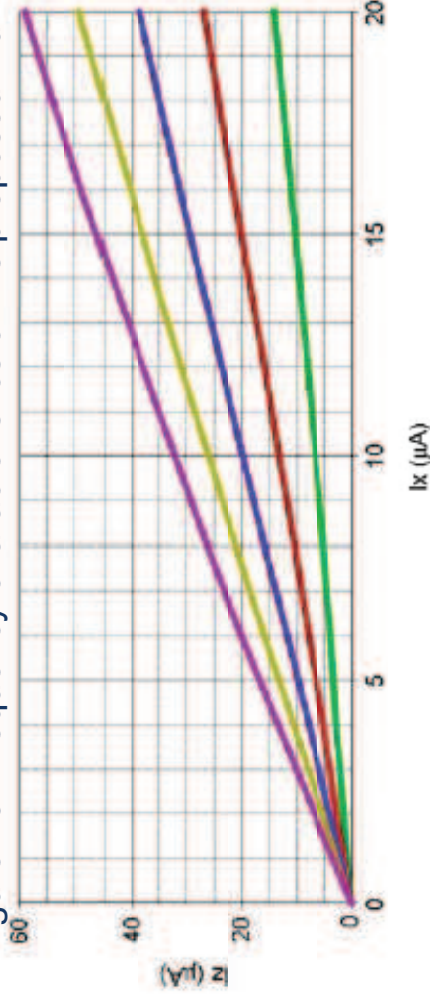
- The absolute error of the simulated output, i.e., $(I_x \cdot I_y / I_w) - I_z$, where the input currents are $I_x = I_y = I_w = 5(2 + \sin 2\pi ft)$ μA with $f = 1 \text{ MHz}$.
- The simulated absolute error is less than $0.055 \mu\text{A}$, thus confirming the high precision of the proposed multiplier/divider circuit.

Simulation results



- The small-signal bandwidth measured from the input I_x to the output (with $I_y = I_w = 15 \mu\text{A}$) is 44MHz

Figure 13. Frequency characteristics of the proposed multiplier/divider



- Input currents were $I_w = 3 \mu\text{A}$, I_y values ranging from 2 μA to 10 μA in 2 μA steps and I_x swept from 0 to 20 μA .

Figure 14. Simulated DC transfer characteristics of the multiplier/ divider

Using of the proposed circuit as an analog amplitude modulator

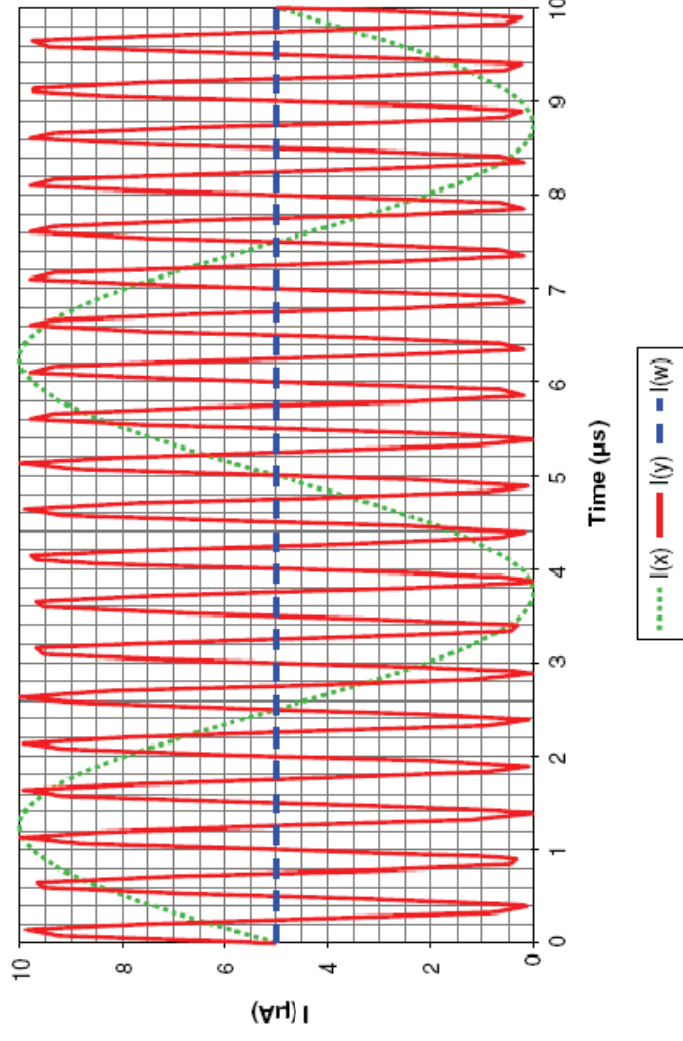


Figure 15. Input currents of the multiplier/divider as an amplitude modulator

- Input currents are taken as $I_x = 5(1 + \sin 2\pi f t)$ μA with $f = 0.2\text{MHz}$, $I_y = 5(1 + \sin 2\pi f t)$ μA with $f = 2\text{MHz}$ and I_w is taken as a fix current of $5\mu\text{A}$ as shown in Fig. 15.

Using of the proposed circuit as an analog amplitude modulator

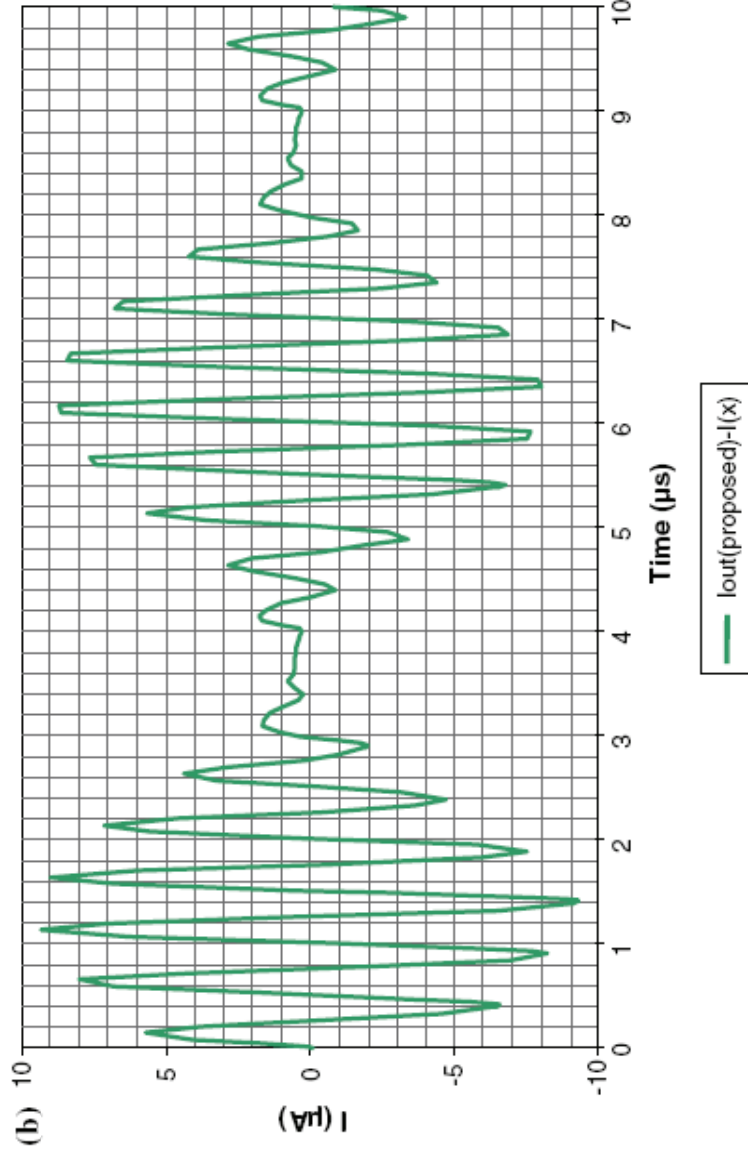


Figure 16. Modulated ac output current of the multiplier/divider as an amplitude modulator

Using of the proposed circuit as an analog amplitude modulator

Table 2. Performance parameters of the multiplier/divider

Parameter	Value	
	Proposed	Cruz-Blas et al. [2]
Technology	0.35 μm CMOS	0.8 μm CMOS
Supply voltage	3 V	1.5 V
THD	0.14% (input: 10 μA_{pp} at 1 MHz)	0.90% (input: 24 μA_{pp} at 1 kHz)
BW (simulated)	44 MHz	5.5 MHz
Area	0.01 mm^2	0.10 mm^2
		Oliveira and Oki [3]
		0.35 μm CMOS
		1.5 V
		0.83% (input: 20 μA_{pp} at 10 MHz)
		140 MHz
		0.02 mm^2

- The circuit proposed provides to the IC designers advantages such as smaller chip size and lower distortion.

CONCLUSION

- This paper proposes a method to reduce the errors generated by the second order effects in the current-mode circuits employing MOS translinear loop. In addition, a high-precision multiplier/divider circuit is also designed using the introduced method.

The main advantages of the proposed circuit can be summarized as,

- a smaller area on the chip
- operation at higher frequencies
- power efficiency
- High precision
- possibility of controlling the output current with the control voltage
- reduced errors of the output current function which is caused by secondary effects

Reference

- [1] S. Menekay, R.C. Tarcan, H. Kuntman, 'Novel high-precision current mode multiplier/divider', *Analog Integrated Circuits and Signal Processing*, Vol.60, No.3, 237-248, 2009.
- [2] C. A. De La Cruz-Blas, A. J. Lopez-Martin and A. Carlosena, "1.5 V four-quadrant CMOS current multiplier/divider." *Electronics Letters*, 39(5), 434-436. doi:10.1049/el:20030298, 2003.
- [3] V. J. S. Oliveira and N. Oki, "Low voltage four-quadrant current multiplier: An improved topology for n-well CMOS process." In *Design & technology of integrated systems in nanoscale era*, DTIS. International conference (pp. 52-55), 2007.