
Arch Dams

Translated from the slides of

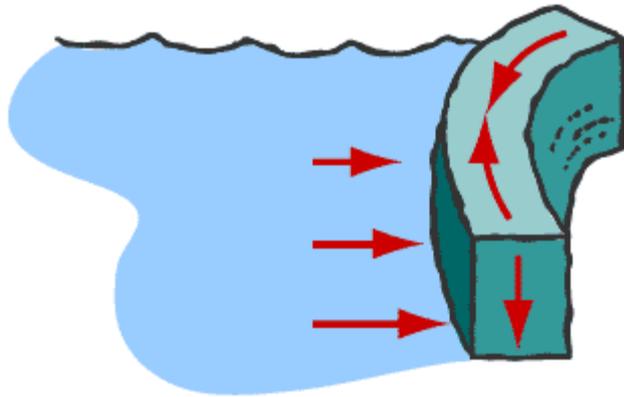
Prof. Dr. Recep YURTAL (Ç.Ü.)

by his kind courtesy

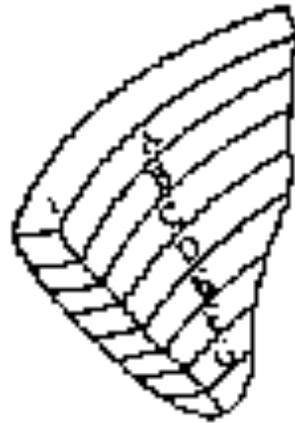
ercan kahya

Arch Dams

- Curved in plan and carry most of the water thrust horizontally to the side abutments by **arch action**.
- A certain percentage of water load is vertically transmitted to the foundation by **cantilever action**.



Arch Dams



(a) Series of horizontal arches



(b) Series of vertical cantilevers

Figure 2.10. Series of horizontal arches and vertical cantilevers

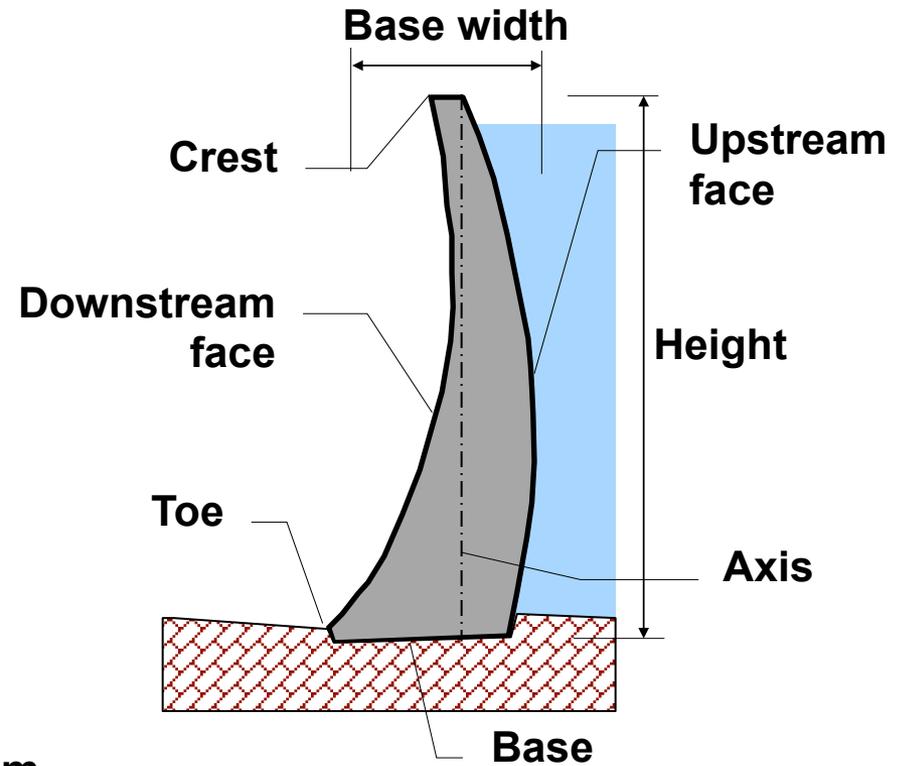
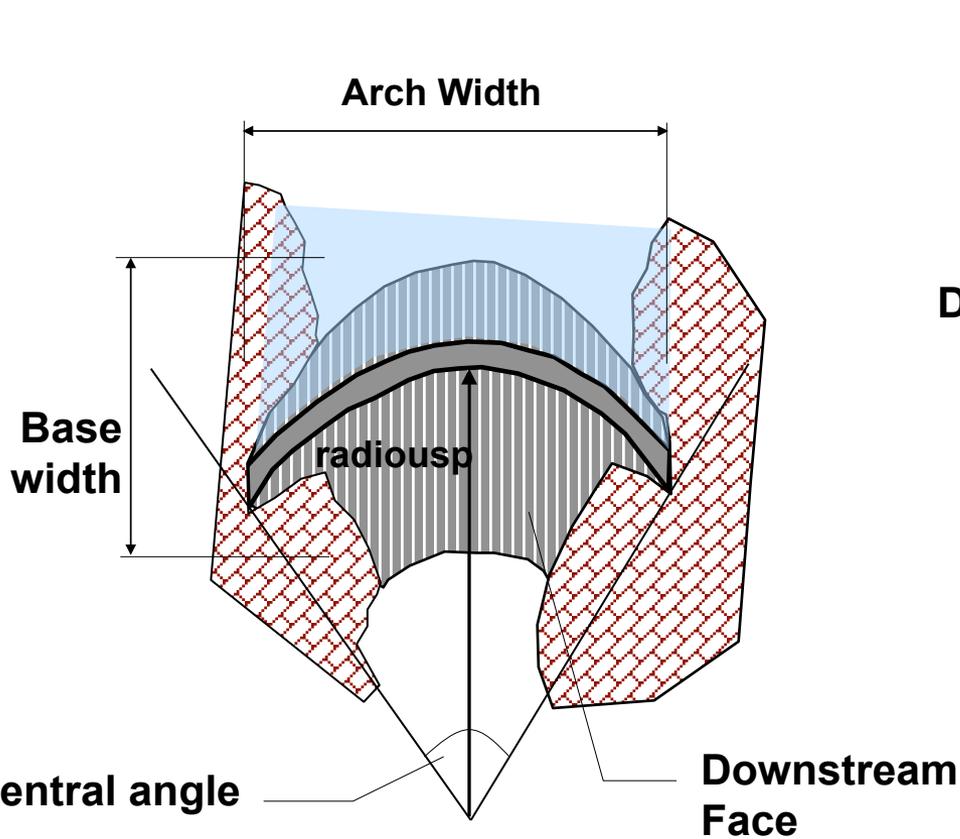




Arch Dams

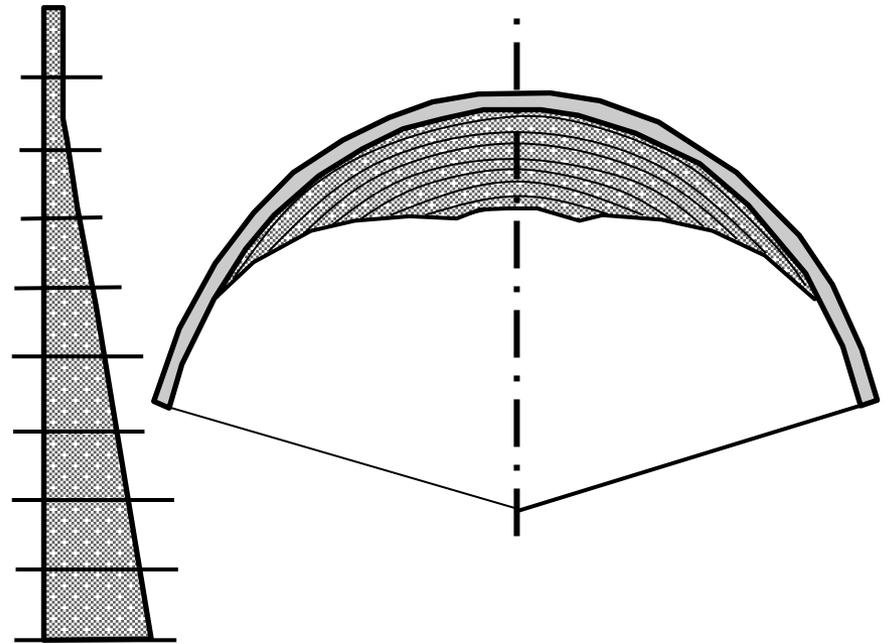
- Where & why we design it:
 - ❑ Appropriate when “Width / Height of valley” (B/H) < 6
 - ❑ Rocks at the base and hillsides should be strong enough with high bearing capacity.
 - ❑ To save in the volume of concrete.
 - ❑ Stresses are allowed to be as high as allowable stress of concrete.
 - ❑ Connection to the slope of hillsides should be 45° at least.

Arch Dams



Arch Dam Types

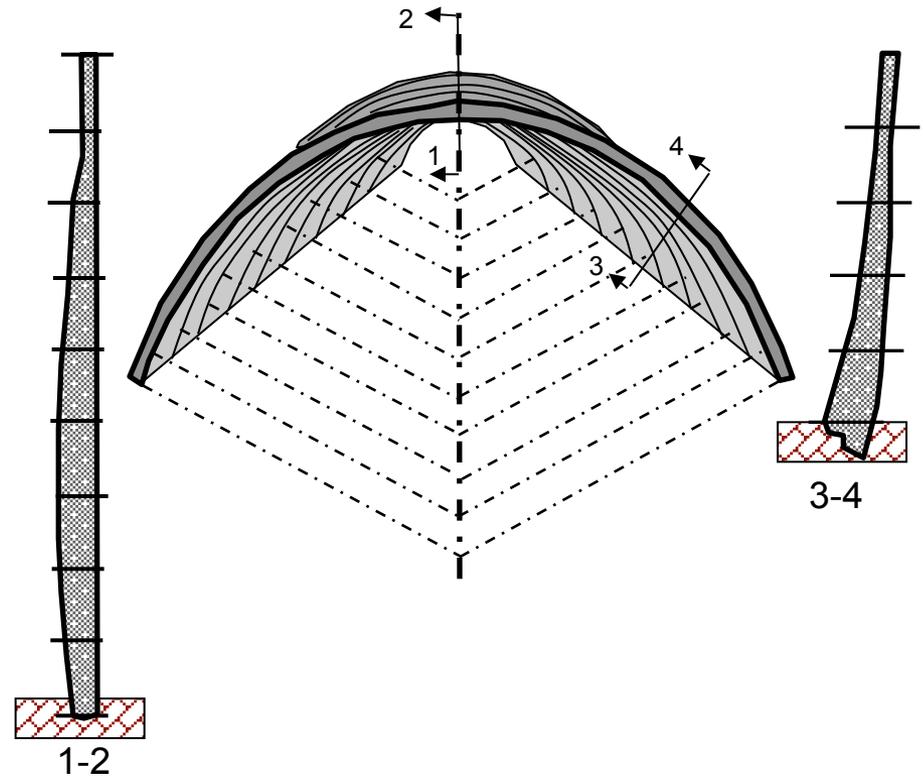
- **Constant Center Arch Dam (variable angle)**
 - Good for **U-shaped** valleys
 - Easy construction
 - Vertical upstream face
 - Appropriate for middle-high dams



Arch Dam Types

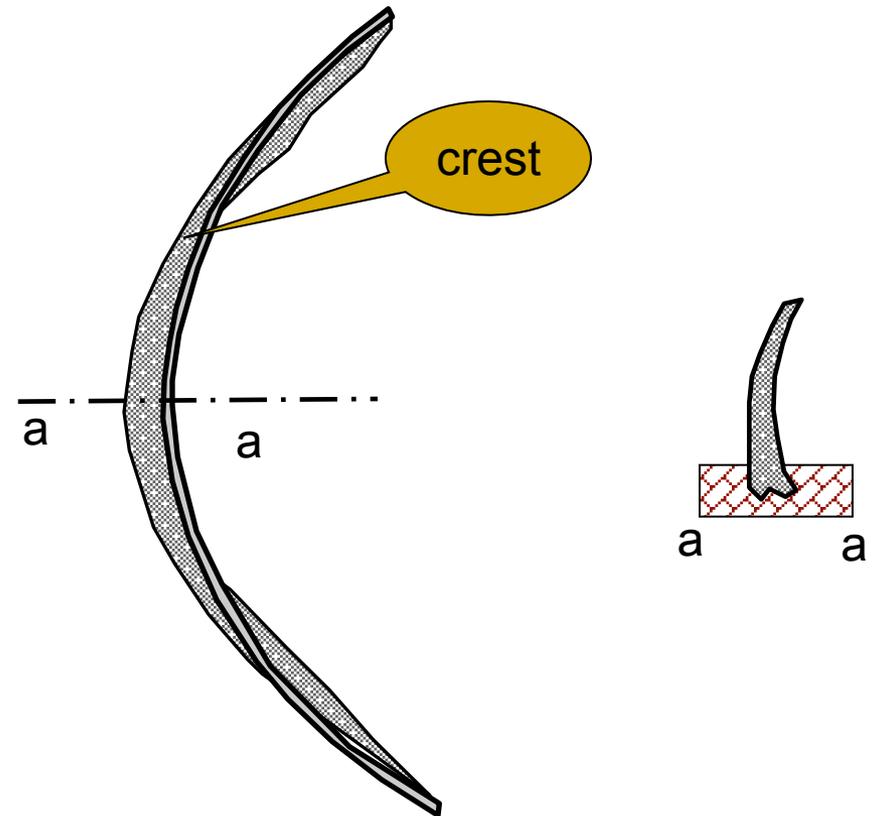
Variable Center Arch Dams (constant angle)

- Good for **V-shaped** valleys
- Limited to the ratio of $B/H=5$
- Best center angle: $133^{\circ} 34'$
- To obtain arch action at the bottom parts

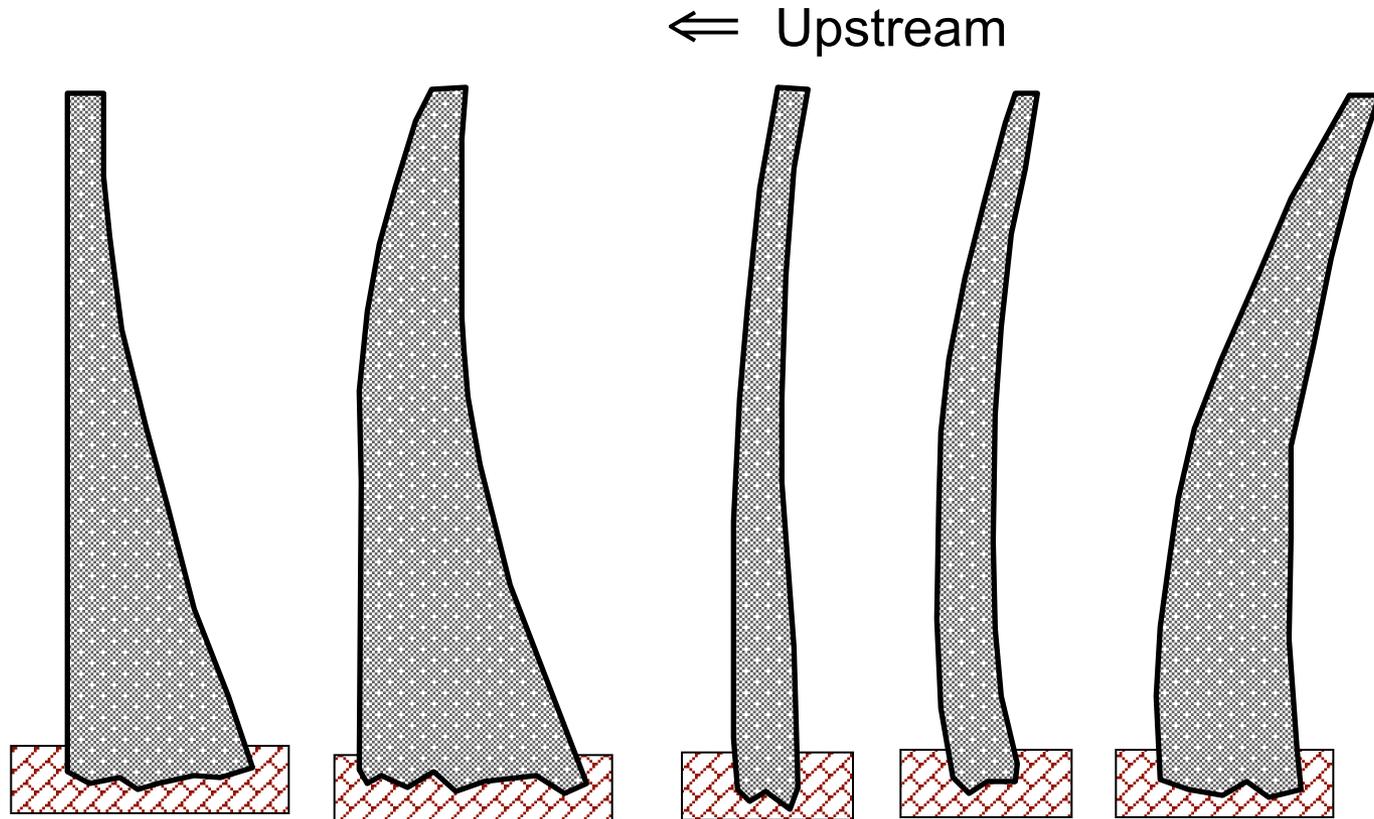


Arch Dam Types

- Variable Center – Variable Angle Arch Dams
 - Combination of the two above.
 - Its calculation based on shell theory applied to arch dams



Arch Dam Types



Arch Dams

■ 3.6.2 DESIGN OF ARCH DAMS

Structural Design: → Load distribution in the dam body
& beyond scope of this course

- ❑ Independent ring method
- ❑ Trial load method
- ❑ Elasticity theory
- ❑ Shell theory

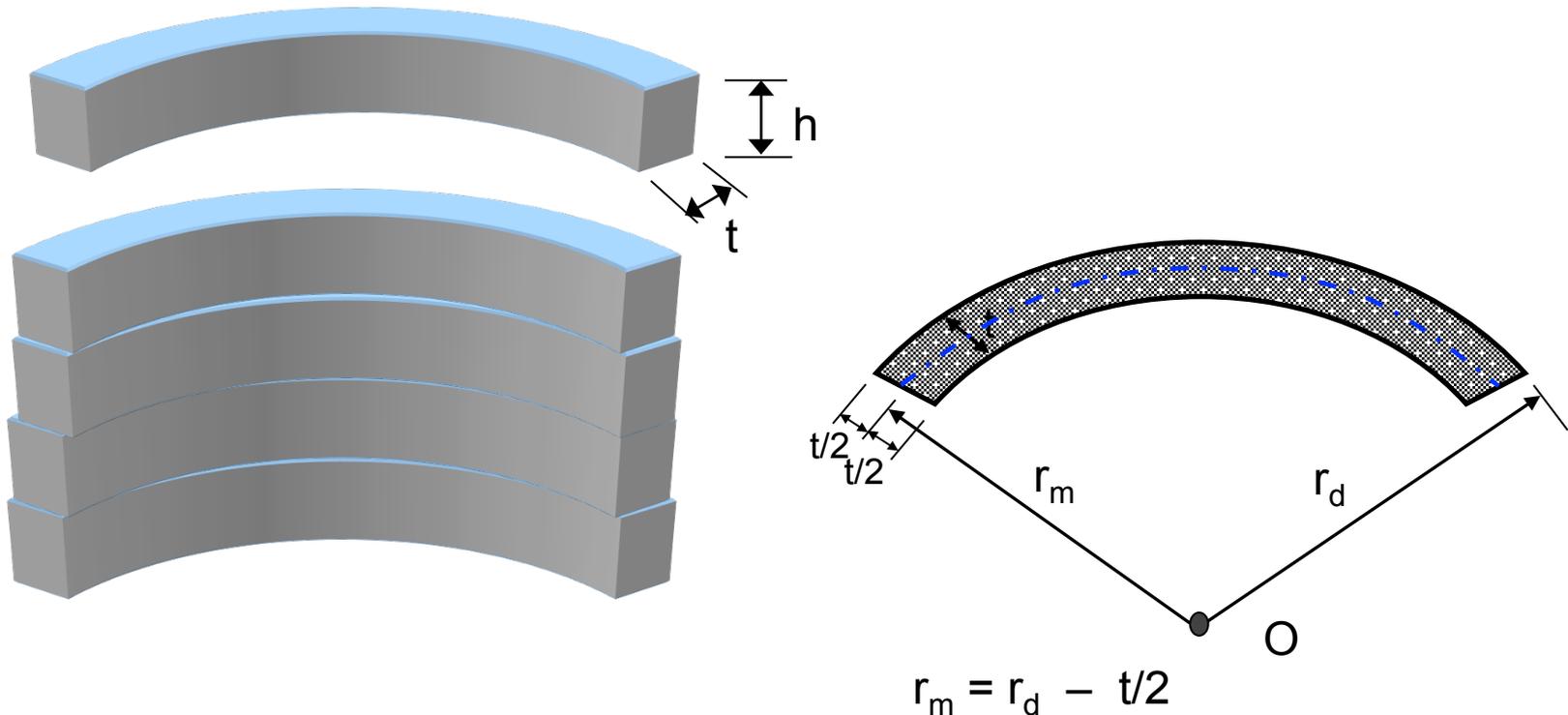
Arch Dams

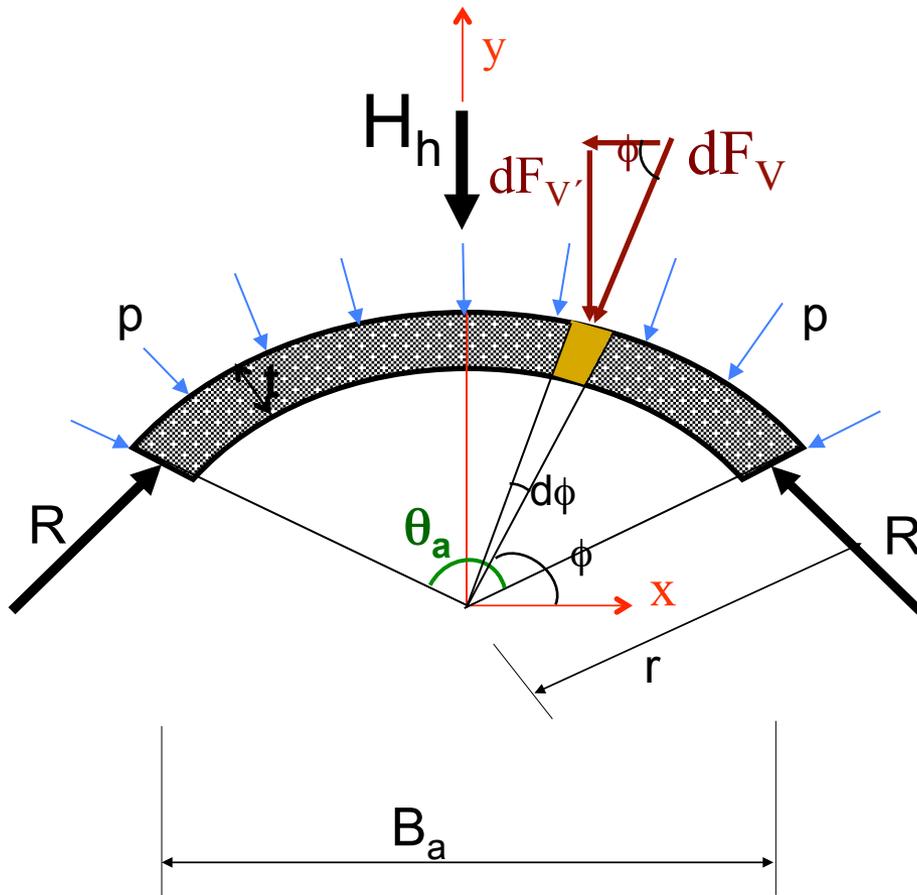
■ Hydraulic Design

- ✧ Determination of thickness at any elevation
 - ✧ Effect of uplift force – ignored
 - ✧ Stresses due to ice & temp changes-important
 - ✧ Arch action - near the crest of dam
 - ✧ Cantilever action - near the bottom of dam
 - ✧ Horizontal hydrostatic pressure is assumed to be taken by arch action
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Arch Dams (design principles)

- Independent Ring method:





Differential force for infinitely small elemental piece with center angle of $d\phi$:

$$dF_V = p \cdot r \cdot d\phi$$

Vertical component:

$$dF_V' = p \cdot r \cdot d\phi \cdot \sin\phi$$

Arch Dams (design principles)

- **Total horizontal force:**

$$H_h = 2\gamma \cdot h \cdot r \cdot \sin \frac{\theta_a}{2}$$

h : height of arch lib from the reservoir surface

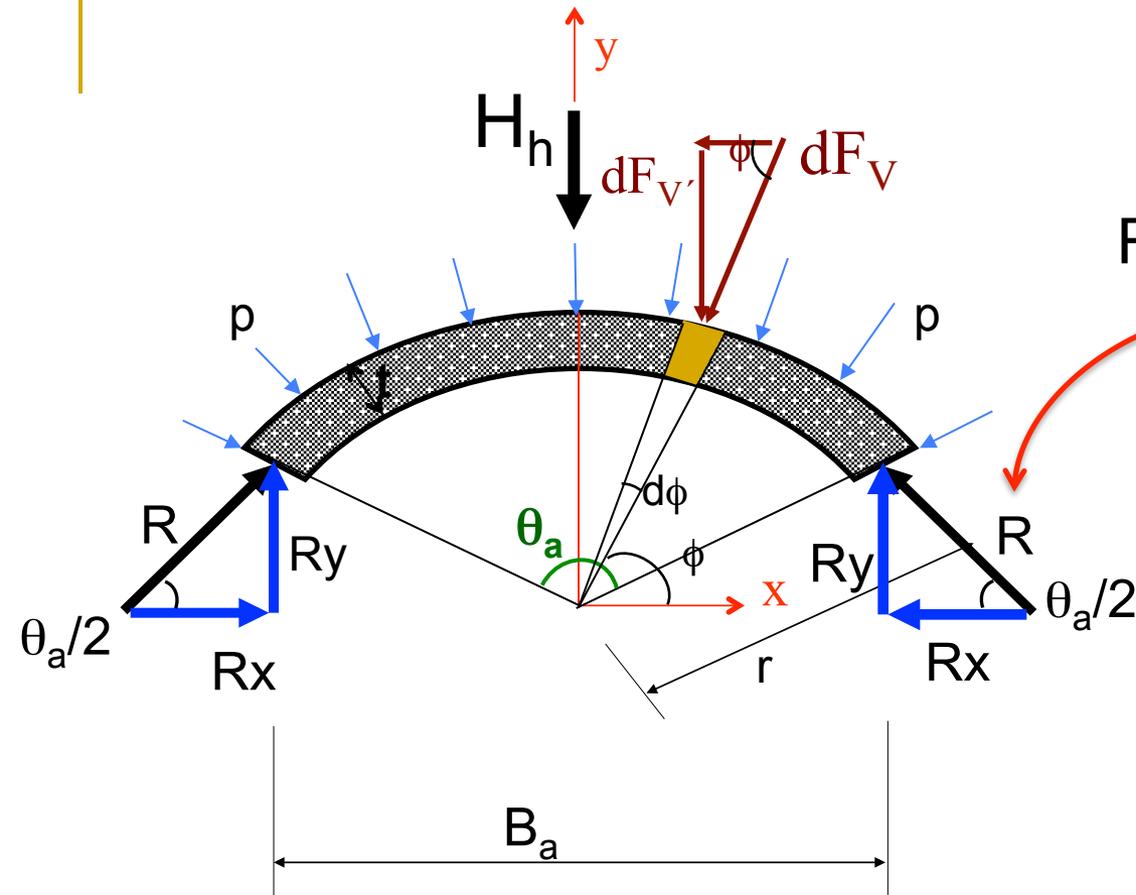
r : radius of arch

θ_a : central angle

- Equilibrium of forces in the flow direction (y):

$$H_h = 2 R_y$$

R_y : reaction force at the sides in y direction [= $R \sin (\theta_a/2)$]



Reaction of the sides (R):

$$R = \gamma \cdot h \cdot r$$

The required thickness of the rib (t) when $t \ll r$:

$$\sigma \approx R / t$$

$$t = \frac{\gamma \cdot h \cdot r}{\sigma_{all}}$$

σ_{all} : allowable working stress
for concrete in compression

Arch Dams (design principles)

The **volume of concrete** for unit height for a single arch:

$$V = L t$$

L: arch length ($L = r \theta_a$) (note that θ_a is in radians)

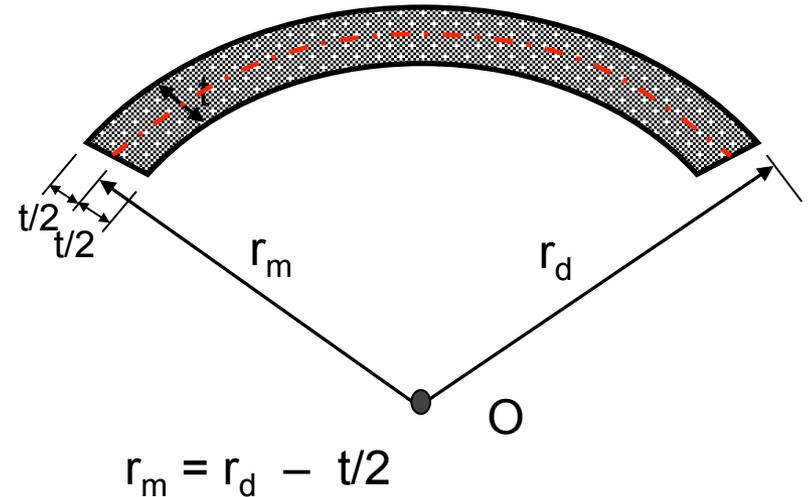
$$V = \frac{\gamma \cdot h}{\sigma_{all}} r^2 \theta_a$$

Arch Dams (design principles)

The required thickness of the rib (t):

- Pressure $p = \gamma \times h$:

$$t = \frac{p \times r_d}{\sigma_{all}}$$



Reduction factor for base pressure at arch dams is zero ($m=0$)

Arch Dams (design principles)

- The **optimum** θ_a for minimum volume of arch rib:

$$dV / d\theta = 0 \quad \rightarrow \quad \theta_a = 133^\circ 34'$$

- ▶ This is the reason why the constant-angle dams require **less concrete** than the constant-center dams
- ▶ Formwork is more difficult
- ▶ In practice; $100^\circ < \theta_a < 140^\circ$ for the constant-angle dams

Arch Dams (design principles)

■ Displacement in an arch ring:

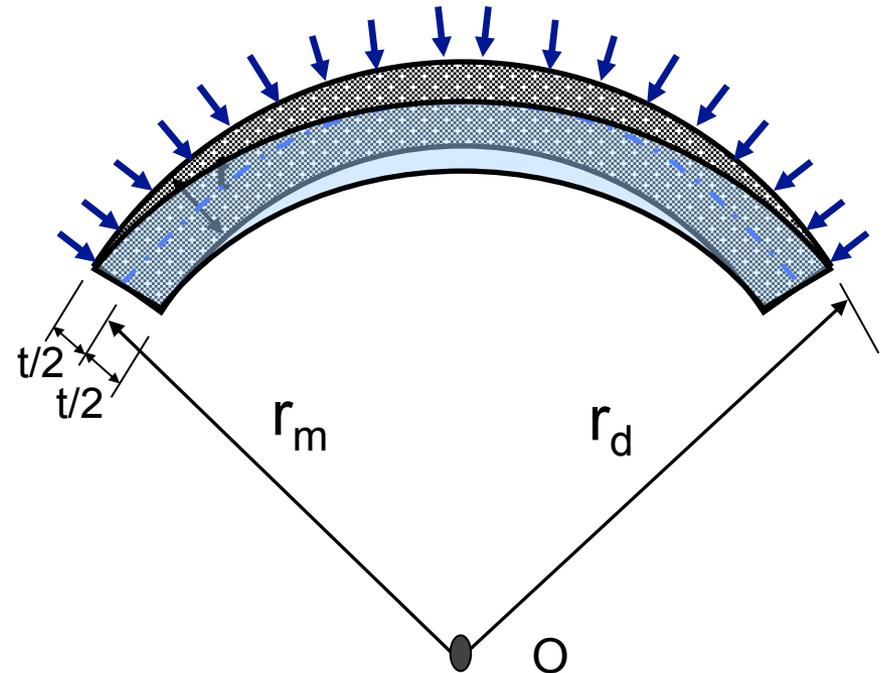
$$\delta = \sigma_{all} \frac{r_m}{E}$$

E = Concrete elasticity modulus

r_m = Radius from ring axis

For the relation between center angle (2ϕ), beam length (L) & arch radius (r):

$$r = \frac{L}{2 \times \sin \phi}$$



$$r_m = r_d - t/2$$

Örnek

- Yüksekliği **120 m** olan bir barajın ağırlık ve kemer-ağırlık türünde yapılması halleri için taban genişliklerini ve birim kalınlıktaki hacimlerini karşılaştırınız. Barajda taban su basıncı küçültme faktörü **0.8** dir. $\gamma_b = 2.4 \text{ t/m}^3$

Çözüm: Ağırlık baraj için:

$$\gamma' = \frac{\gamma_b}{\gamma_w} \quad \gamma' = \frac{2.4}{1.0} = 2.4$$

$$\frac{b}{h} = \sqrt{\frac{1}{\gamma' - m}} \quad \frac{b}{120} = \sqrt{\frac{1}{2.4 - 0.8}} \quad b = 120 \times \sqrt{\frac{1}{2.4 - 0.8}} \quad b = 95 \text{ m.}$$

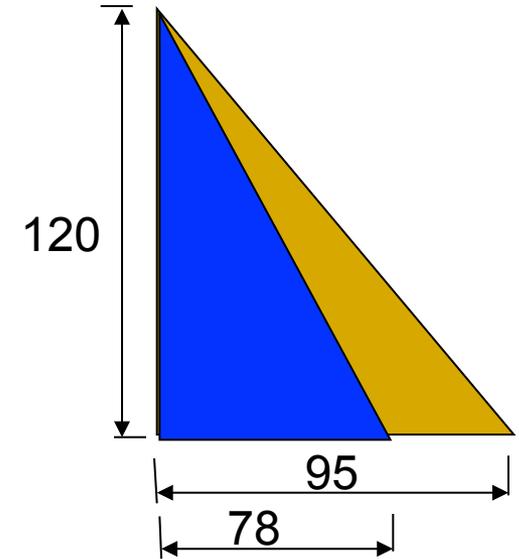
$$\text{Hacim} = 120 \times 95 \times \frac{1}{2} = 5700 \text{ m}^3$$

- Kemer-Ağırlık baraj için:

$$m = 0 \quad \frac{b'}{h} = \sqrt{\frac{1}{\gamma'}} \quad b' = 120 \times \sqrt{\frac{1}{2.4}} = 78 \text{ m}$$

$$\text{Hacim} = 120 \times 78 \times \frac{1}{2} = 4680 \text{ m}^3$$

$$\text{Hacim azalması} : \frac{5700 - 4680}{5700} = \% 18$$



Ağırlık yerine kemer-ağırlık seçmeyle beton hacminde **%18** azalma olacaktır.
Bu seçim ancak yamaçlar yeterince sağlam olduğunda yapılabilir.

Örnek

- Yüksekliği **80 m** olacak bir sabit yarıçaplı (silindirik) kemer barajda tabandaki maksimum kemer kalınlığının, en fazla baraj yüksekliğinin $\frac{1}{4}$ üne eşit olması istendiğine göre kemer yarıçapını hesaplayınız. Kemer halkalarının emniyet gerilmesi **220 t/m^2** , betonun elastisite modülü **$2 \times 10^6 \text{ t/m}^2$** olduğuna göre tepede anahtar noktasında ortaya çıkacak sehimi bulunuz.

Çözüm

$$r_d = t \times \frac{\sigma_h}{p}$$

$t = h/4$ alalım $t = 80 / 4 = 20 \text{ m}$:

$$p = \gamma \times h \quad r_d = \left(\frac{h}{4} \right) \times \frac{\sigma_h}{(\gamma \times h)} \quad r_d = \frac{1}{4} \times \frac{\sigma_h}{\gamma} = \frac{1}{4} \times \frac{220}{1} = 55 \text{ m}$$

$$r_m = r_d - \frac{t}{2} = 55 - \frac{20}{2} = 45 \text{ m} \quad \delta = \sigma_h \frac{r_m}{E} \quad \delta = 220 \times \frac{45}{2 \times 10^6} = 0.005 \text{ m}$$

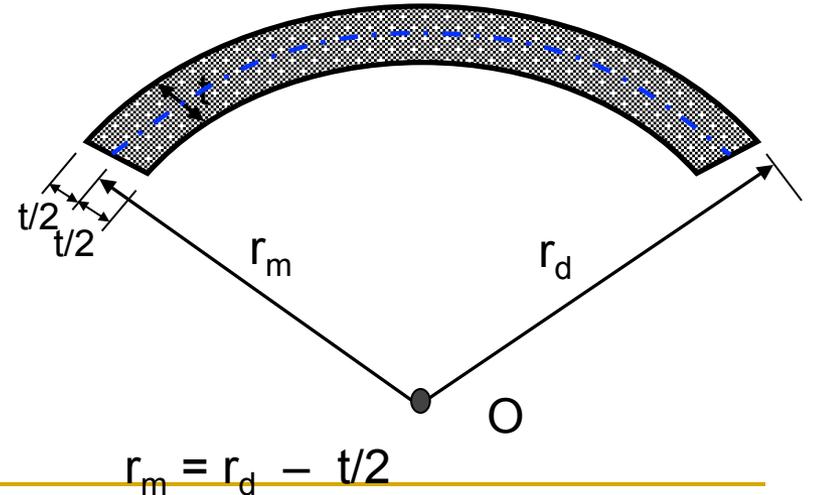
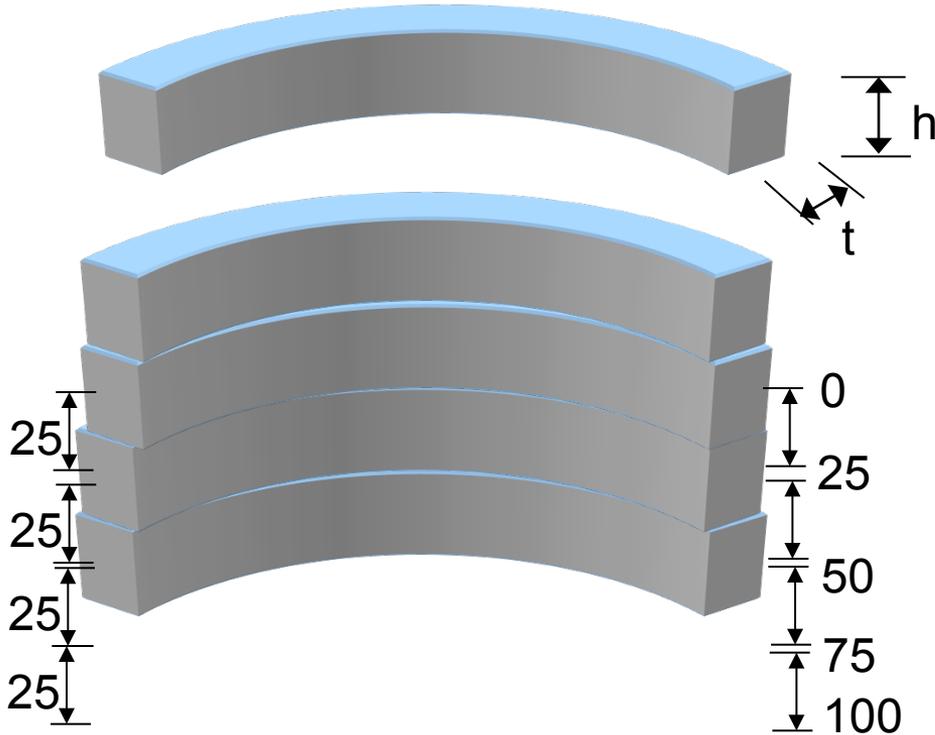
0.5 cm sehîm oluşur.

Örnek

- Yüksekliği **100 m** ve tepe genişliği **5 m** olacak bir kemer barajın tepeden itibaren **0, 25, 50, 75** ve **100 m** derinliklerdeki eksen yarıçapları sıra ile **95, 80, 63, 58, 50 m** dir. Betonun emniyet gerilmesi 300 t/m^2 ve elastisite modülü $2 \times 10^6 \text{ t/m}^2$ dir. Her seviyede kemer halkasının kalınlık ve sehimini bulunuz.

Kemer Barajlar (Hesap Esasları)

■ Bağımsız Halkalar Yöntemi



Çözüm

$$\sigma_h = \frac{2}{3} \sigma_{b_{em}} = \frac{2}{3} \times 300 = 200 \text{ t/m}^2$$

$$r_d = r_m + \frac{t}{2} \quad t = \frac{p \times r_d}{\sigma_h} \quad t = \frac{\overbrace{(\gamma \times h)}^p \times \overbrace{\left(r_m + \frac{t}{2}\right)}^{r_d}}{\sigma_h} = \frac{\overbrace{(\gamma \times h)}^p \times (r_m + 0.5 \times t)}{\sigma_h}$$

$$t = \frac{\gamma \times h \times r_m + \gamma \times h \times 0.5 \times t}{\sigma_h} \quad t = \frac{\gamma \times h \times r_m}{(\sigma_h - \gamma \times h \times 0.5)}$$

$$\gamma = 1 \text{ t/m}^3, \sigma_h = 200 \text{ t/m}^2 \text{ için: } t = \frac{h \times r_m}{(200 - h \times 0.5)} \quad \text{bulunur.}$$

$$\text{Sehim: } \delta = \sigma_h \frac{r_m}{E}$$

$$t = \frac{h \times r_m}{(200 - h \times 0.5)}$$

$$\delta = \sigma_h \frac{r_m}{E}$$

Sıra No	Baraj tepesinden itibaren derinlik h (m)	Eksen yarıçapı r _m (m)	Kemer kalınlığı t (m)	Sehim δ (cm)
1	0	95	0,00	0,95
2	25	80	10,67	0,80
3	50	63	18,00	0,63
4	75	58	26,77	0,58
5	100	50	33,33	0,50