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## Chapter 13

## Gears - General

Mechanical Engineering Design

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Fig. 13.1 Spur gears have teeths parallel to the axis of rotation. They are used to transmit motion from one shaft to another, parallel, shaft.

Fig. 13.2 Helical gears have teeth inclined to the axis of rotation. Sometimes helical gears are used to transmit motion between nonparallel shafts.

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Fig. 13.3 Bevel gears have teeth formed on conical surfaces and are used mostly for transmitting motion between intersecting shafts.

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Fig. 13.4 Hypoid gears, worm gear are used to transmit motion between nonparallel, nonintersecting shafts.

## Nomenclature

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$$
\begin{aligned}
& P=N / d \\
& p=\pi d / N=\pi m \\
& m=d / N
\end{aligned}
$$

Fig. 13.5 Nomenclature. The circular pitch, p , is the distance, measured on the pitch circle, measured from a point on one tooth to a corresponding point on an adjacent point. The module, $m$, is the ratio of the pitch diameter to the number of teeth. The diametral pitch, P , is the ratio of the number of teeth on the gear to the pitch diameter. The addendum, $a$, is the radial distance between the top land and the pitch circle. The dedendum, b , is the radial distance from the bottom land to the pitch circle. The clerance circle is a circle that is tangent to the addendum circle of the mating gear.

Tooth Systems, Conjugate Action, Involute Properties
A tooth system is a standard which specifies the relationships involving addendum, dedendum, working depth, tooth thickness, and pressure angle.
When the tooth profiles are designed so as to produce a constant angular velocity ratio during meshing, these are said to have conjugate action. The involute profile is used to obtain the conjugate action.

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(a)

(b)

Fig. 13.7 (a) Generation of an involute;
(b) involute action

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Fig. 13.8 Construction of an involute curve

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Fig. 13.12 Tooth action.

## The Forming of Gear Teeth

There are a large number of ways of forming of the teeth of gears, such as sand casting, shell Molding, investment casting, permanent-mold casting, die casting, and centrifugal casting. Teeth can be formed by using the powder-metallurgy process; or by using extrusion. Gears which carry large loads in comparison with their size are usually made of steel and are cut with either form cutters or generating cutters.


Fig. 13.17 Generating a spur gear with a pinion cutter.


Fig. 13.18 Shaping teeth with a rack.


Fig. 13.19 Hobbing a worm gear.
The hob is simply a cutting tool which is shaped like a worm.

Choose an appropriate module, $m$ (use fatigue, fracture mechanics, strength of materials relations, and standard sizes).
Calculate addendum and dedendum ( $\mathrm{a}=1 . \mathrm{m} \quad \mathrm{b}=1.2 \sim 1.25 \mathrm{~m}$ )
Calculate the pitch diameter, d , and the diameters of addendum and dedendum circles, $\mathrm{d}_{\mathrm{a}}$ and $\mathrm{d}_{\mathrm{b}}$. ( $d=$ N.m $\quad d_{a}=d+2 . a \quad d_{b}=d-2.5 m$ )
Calculate the distance between the axes $\left((d P+d G) / 2=m\left(N_{P}+N_{G}\right) / 2\right)$.
Calculate the face width, $F=F_{w} \cdot p=F_{w} \cdot \pi . m$.

Straight Bevel Gears


Fig. 13.20 Terminology of bevel gears.

## Parallel Helical Gears



Fig. 13.22 Nomenclature of helical gears.

## Worm Gears

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$d_{G}=N_{G} p_{t} / \pi$
$L=p_{x} N_{W}$
$\tan \lambda=L / \pi d_{w}$
$C^{0.875 / 3 \leq d_{W} \leq} C^{0.875 / 1.7}$
$C$ : center distance

Fig. 13.24 Nomenclature of a singleenveloping worm gearset.

## Gear Trains

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Fig. 13.27 Gear trains. Gear 3 is an idler. 2,3,5 are drivers. 3,4,6 are driven members.
$n_{3}=/ N_{2} / N_{3} / n_{2=} / d_{2} / d_{3} / n_{2}$
$n_{6}=\left(N_{2} / N_{3}\right)\left(N_{3} / N_{4}\right)\left(N_{5} / N_{6}\right) n_{2}$
$e=$ product of driving tooth numbers / product of driven tooth numbers, $n_{L}=e n_{F}$


(b)

(d)

Left hand
Fig. 13.26 Thrust, rotation, and hand relations for crossed helical gears.


Fig. 13.28 Planetary, or epicyclic, gear trains. Some of the gear axes rotate about others. $e=\left(n_{L}-n_{A}\right) /\left(n_{F}-n_{A}\right)$

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Fig. 13.35


Force analysis
$\mathrm{W}_{\mathrm{t}}=\mathrm{T} / \mathrm{r}_{\mathrm{av}}$
$\mathrm{W}_{\mathrm{r}}=\mathrm{W}_{\mathrm{t}} \tan \Phi \cos \gamma$
$\mathrm{W}_{\mathrm{a}}=\mathrm{W}_{\mathrm{t}} \tan \Phi \sin \gamma$

Fig. 13.37

$T_{1}=W_{t} d_{1} / 2$
Spur gears
$W_{r}=W \cdot \sin \Phi_{t}$
$W_{t}=W \cdot \cos \Phi_{t}$
Helical gears
$W_{r}=W \cdot \sin \Phi_{n}$
$W_{t}=W \cdot \cos \Phi_{n} \cdot \cos \psi$
$W_{a}=W \cdot \cos \Phi_{n} \cdot \sin \psi$

$W^{x}=W \cos \Phi_{n} \sin \lambda$
$\mathrm{W}_{\mathrm{Wt}}=-\mathrm{W}_{\mathrm{Ga}}=\mathrm{W}^{\mathrm{x}}$
$W^{y}=W \sin \Phi_{n}$
$W^{z}=W \cos \Phi_{n} \cos \lambda$
$W_{W_{r}}=-W_{G r}=W^{y}$
$\mathrm{W}_{\mathrm{Wa}}=-\mathrm{W}_{\mathrm{Gt}}=\mathrm{W}^{\mathrm{z}}$

Efficiency

Fig. 13.42
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## Chapter 13, Problem 2.

A 15-tooth spur pinion has a module of 3 mm and runs at a speed of $1600 \mathrm{rev} / \mathrm{min}$. The driven gear has 60 teeth. Find the speed of the driven gear, the circular pitch, and the theoretical center-to-center distance.

## Chapter 13, Problem 13.

A parallel-shaft gearset consists of an 18-tooth helical pinion driving a 32-tooth gear. The pinion has a left-hand helix angle of $25^{\circ}$, a normal pressure angle of $20^{\circ}$, and a normal module of 3 mm . Find:
(a) The normal, transverse, and axial circular pitches
(b) The transverse module and the transverse pressure angle
(c) The pitch diameters of the two gears

## Chapter 13, Problem 16.

The mechanism train shown consists of an assortment of gears and pulleys to drive gear 9 . Pulley 2 rotates at $1200 \mathrm{rev} / \mathrm{min}$ in the direction shown. Determine the speed and direction of rotation of gear 9 .


Figure P13-16

## Chapter 13, Problem 21 (Chapter 13, Problem 21).

Tooth numbers for the gear train shown in the figure are $N 2=12, N 3=16$, and $N 4=12$. How many teeth must internal gear 5 have? Suppose gear 5 is fixed. What is the speed of the arm if shaft a rotates counterclockwise at $320 \mathrm{rev} / \mathrm{min}$ ?


Figure P13-21

## Chapter 13, Problem 24 (Chapter 13, Problem 25).

The epicycle train shown in the figure has the arm attached to shaft $a$, and sun gear 2 to shaft $b$. Gear 5 , with 111 teeth, is an internal gear and is part of the frame. The two planets, gears 3 and 4, are both fixed to the same planet shaft. If this train is used as an in-line speed reducer, which is the input shaft, $a$ or $b$ ? Will both shafts then rotate in the same or in the opposite directions?

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Figure P13-24

Choosing module (m) according to failure criteria

- Pitting is a surface fatigue failure due to many repetitions of high contact stresses

$$
m_{n}=0.9 \sqrt[3]{\frac{K_{A} \cdot K_{V} \cdot T_{1} \cdot E \cdot(e+1) \cos ^{4} \psi}{N_{1}^{2} \cdot P_{e m}^{2}-e \cdot \varepsilon_{\alpha} F_{W}}}(\mathrm{~mm})
$$

- Fracture of a tooth

$$
m_{n}=0.6 \cdot \sqrt[3]{\frac{K_{A} \cdot K_{v} \cdot T_{1} \cdot \gamma \cdot \cos \psi}{N_{1} \cdot \sigma_{e m} \cdot \varepsilon_{\alpha} \cdot F_{w}}}(\mathrm{~mm})
$$

$\varepsilon_{\alpha}$ : profile ratio
$K_{A}$ : Impact or contact load factor
E: Young's modulus ( $\mathrm{N} / \mathrm{mm}^{2}$ )
Kv: Dynamic load factor
$T_{1}$ : Torque on pinion (Nim)
Fem: Tensile (bending) strength ( $\mathrm{N} / \mathrm{mm}^{2}$ )
$N_{1}$ : Number of teeth of pinion
Pen: Hertz pressure
$\gamma$ : Form factor

$$
e=\frac{w_{1}}{w_{2}}=\frac{N_{2}}{N_{1}}
$$

$\mathrm{K}_{\mathrm{A}}: 1-2.25$ (depending on the impact loads during the operation of machine)
$\mathrm{K}_{\mathrm{v}}$ : It is chosen based on the Table 1.
Table 1. Dynamic load factor

| Tangential velocity $(\mathrm{m} / \mathrm{s})$ | 2 | 4 | 12 | 20 | 40 | 60 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| High quality | 1 | 1 | 1.1 | 1.15 | 1.2 | 1.25 |
| Normal quality | 1 | 1.1 | 1.25 | 1.3 | - | - |
| Pure quality (casting) | 1.5 | 2.0 | - | - | - | - |

Table 2. Form factor $(\gamma)$ for $\left(\phi_{n}=20^{\circ}\right)$.

| $\mathrm{N}^{\prime}$ | 13 | 14 | 15 | 16 | 18 | 20 | 30 | 50 | 100 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\gamma$ | 9.5 | 9.3 | 9.0 | 8.8 | 8.4 | 8.1 | 7.5 | 6.8 | 6.3 |

Table 3. Profile ratio $\left(\varepsilon_{\alpha}\right)$

| $\psi=0$ | $15^{\circ}$ | $30^{\circ}$ | $45^{\circ}$ |
| :--- | :--- | :--- | :--- |
| 1.73 | 1.65 | 1.41 | 1.05 |

Table 4. Width ratio $\left(\mathrm{F}_{\mathrm{w}}=\mathrm{b} / \mathrm{p}_{\mathrm{n}}\right)$

| Gears made of cast materials | 2 |
| :--- | :--- |
| Pure quality gears | $3 \ldots 4$ |
| High quality gears | $5 \ldots 8$ |
| Very high quality gears | $9 \ldots 14$ |


| Material |  | $\sigma_{\text {өm }}\left[\mathrm{N} / \mathrm{mm}^{2}\right]$ | $\mathrm{P}_{\text {em }}\left[\mathrm{N} / \mathrm{mm}^{2}\right]$ |
| :---: | :---: | :---: | :---: |
| Cast Iron | GG20 | 35-45 | 220 |
|  | GG25 | 48-55 | 270 |
|  | GG30 | 60 | 330 |
| Nodular Cast Iron | Ferritik | 145 | 300 |
|  | Perlitik | 145 | 400 |
| Cast Steel | GS45 | 80 | 250 |
|  | GS52 | 90 | 310 |
|  | GS60 | 100 | 390 |
| Tool Steel | St42 | 90-100 | 280-340 |
|  | St50 | 110-125 | 340-400 |
|  | St60 | 125-140 | 380-500 |
|  | St70 | 140-160 | 440-570 |
| Tempered Steel | C22 | 120 | 330 |
|  | C45 | 135-150 | 450 |
|  | C60 | 150-165 | 500 |
|  | 34 Cr 4 | 180-200 | 600 |
|  | 37MnSi5 | 190-200 | 550 |
|  | 42CrMo4 | 200 | 630 |
|  | 35NiCr18 | 200 | 900 |
| Case Hardening Steel | C10 | 100-115 | 1350 |
|  | C15 | 110-125 | 1500 |
|  | 16 MnCr 5 | 190-210 | 1500 |
|  | 20 MnCr 5 | 210-230 | 1500 |
|  | 13Ni6 | 150 | 1350 |
|  | 15 CrNi 6 | 200-220 | 1500 |
|  | 13 NiCr 18 | 220 | 1400 |
|  | 18 CrNi 8 | 210-230 | 1500 |
| Hardened Steel | C60 | 160 | 1050 |
|  | Ck45 | 180 | 1350 |
|  | Ck53 | 220 | 1400 |
|  | 37MnSi5 | 200 | 1250 |
|  | $53 \mathrm{MnSi4}$ | 200 | 1400 |
|  | 41 Cr 4 | 200 | 1300 |
|  | 50 CrV 4 | 240 | 1400 |
|  | $42 \mathrm{CrMo4}$ | 210 | 1500 |
| Cyanide Hardening Steel | 41 Cr 4 | 190 | 1350 |
|  | $37 \mathrm{MnSi5}$ | 200 | 1250 |
|  | 35NiCr18 | 220 | 1350 |
|  | 34 Cr 4 | 210 | 1200 |
|  | $42 \mathrm{CrMo4}$ | 240 | 1200 |
| Nitrogen Hardening <br> Steel | C45 | 160 | 750 |
|  | 16 MnCr 5 | 170 | 720 |
|  | 42CrMo4 | 290 | 850 |
|  | 16 MnCr 5 | 210 | 880 |


| Tabble 13-6 <br> Moxinum Tooh Numbers | Number of Pinion | Number of Gear reeth, $N_{6}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Halix angle, ${ }^{\text {y }}$, deg |  |  |  |  |
| on Geors to Avoid | Teath, $\mathrm{N}_{\mathrm{p}}$ | 0 | 5 | 10 | $15 \quad 20 \quad 25$ | 3035 |
| Intereerce. Numbers | 8 |  |  |  |  | 12 |
| Are bosed on o Normal | 9 |  |  |  |  |  |
| Pressure Angle of | 10 |  |  |  | 12 | $26 \infty$ |
| $\phi_{n}=w^{\circ}$ ard Full $\mathrm{Depeph}^{\text {a }}$ | 11 |  |  |  | $13 \quad 23$ | 93 |
| Teeth. For Sour Geors, | $\begin{aligned} & 12 \\ & 13 \end{aligned}$ | 16 | 17 | 12 20 | $\begin{array}{ccc} 16 & 24 & 57 \\ 27 & 50 & 1385 \end{array}$ | $\infty$ |
| $\psi=0$ | 14 |  | 27 |  |  |  |
| Sarce lipe 'Aoding | 15 |  | 49 | 69 | $181 \times$ |  |
| Desion id 31 ro. 1,1982 <br> 012 |  | 101 1309 |  | $\begin{aligned} & 287 \\ & 0 \end{aligned}$ | $\infty$ |  |
|  |  |  |  |  |  |  |

