Lecture Slides

Chapter 9

Welding, Bonding, and the Design of Permanent Joints

Shigley's Mechanical Engineering Design Ninth Edition Richard G. Budynas and J. Keith Nisbett

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Chapter Outline

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Welding Symbols

- Welding symbol standardized by American Welding Society
- Specifies details of weld on machine drawings

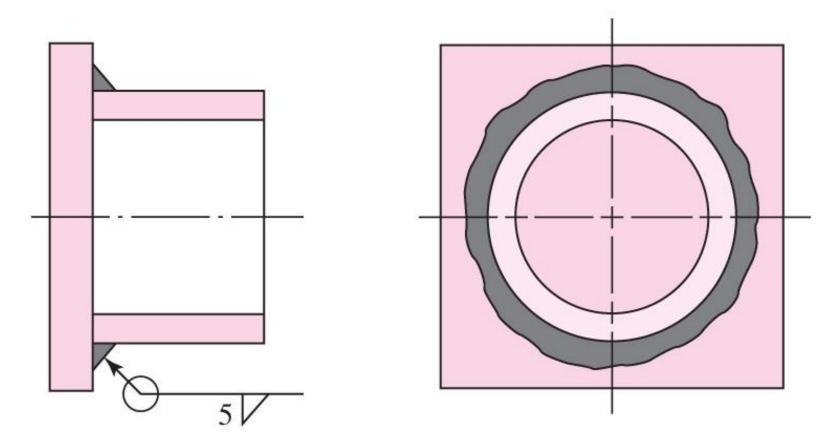
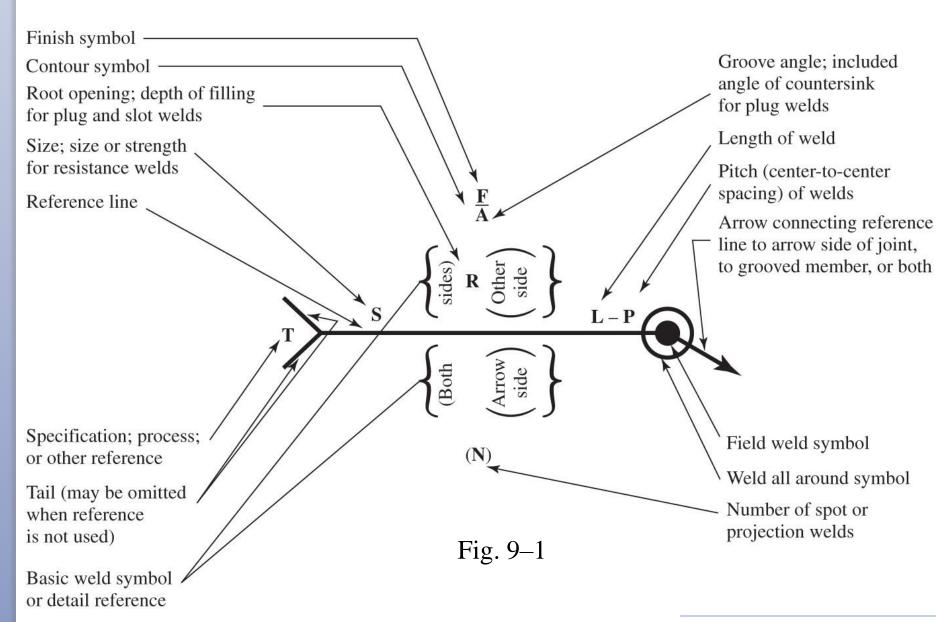


Fig. 9–4

Welding Symbols



Welding Symbols

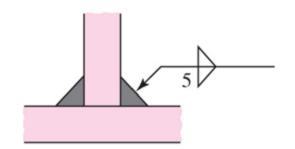
- Arrow side of a joint is the line, side, area, or near member to which the arrow points
- The side opposite the arrow side is the *other side*
- Shape of weld is shown with the symbols below

Type of weld							
Bead	Fillet	Plug	Groove				
	Fillet	or slot	Square	V	Bevel	U	J
				\	V	5	V

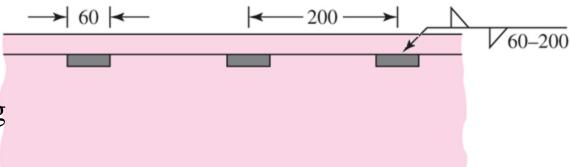
Fig. 9–2

Welding Symbol Examples

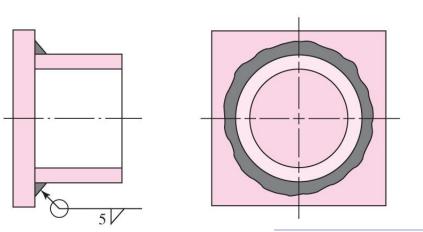
- Weld leg size of 5 mm
- Fillet weld
- Both sides



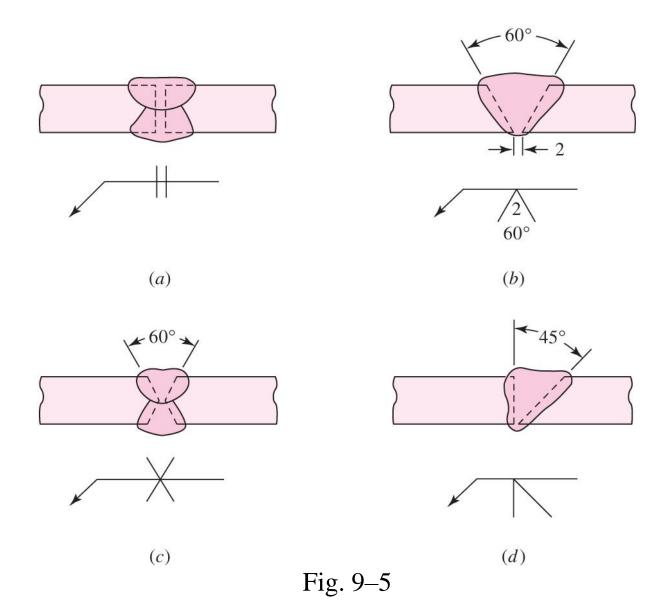
 Intermittent and staggered 60 mm along on 200 mm centers



- Leg size of 5 mm
- On one side only (outside)
- Circle indicates all the way around



Welding Symbol Examples



Welding Symbol Examples

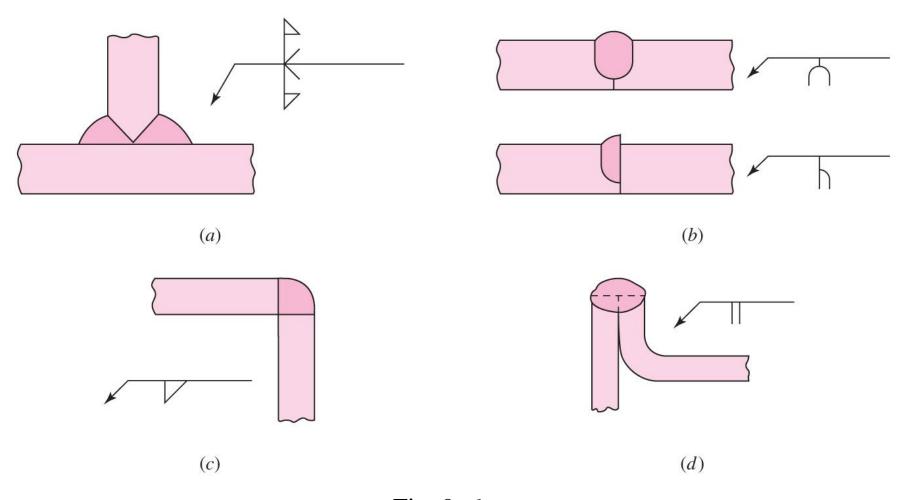


Fig. 9–6

Tensile Butt Joint

- Simple butt joint loaded in tension or compression
- Stress is normal stress

$$\sigma = \frac{F}{hI} \tag{9-1}$$

- Throat *h* does not include extra reinforcement
- Reinforcement adds some strength for static loaded joints
- Reinforcement adds stress concentration and should be ground off for fatigue loaded joints

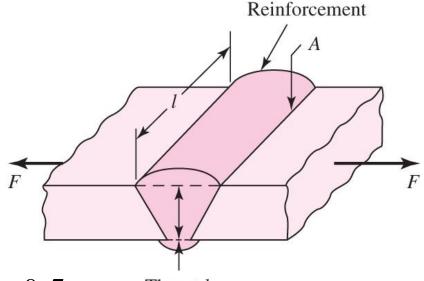


Fig. 9–7*a*

Shear Butt Joint

- Simple butt joint loaded in shear
- Average shear stress

$$\tau = \frac{F}{hI} \tag{9-2}$$

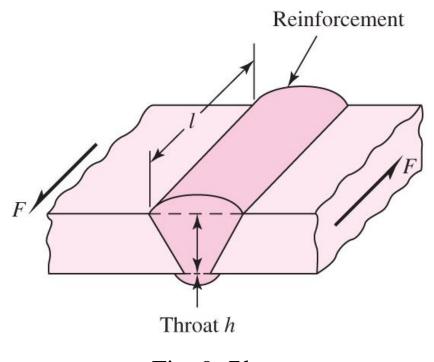
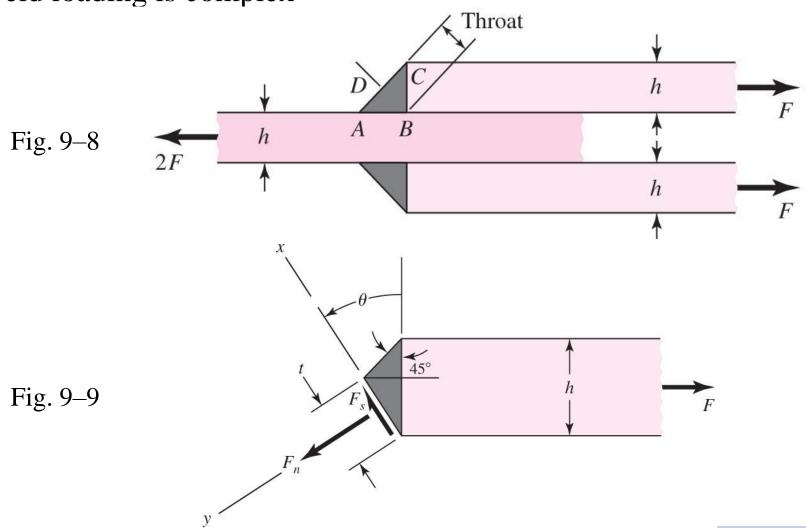


Fig. 9–7*b*

- Joint loaded in tension
- Weld loading is complex



Summation of forces

$$F_s = F \sin \theta$$
$$F_n = F \cos \theta$$

Law of sines

$$\frac{t}{\sin 45^{\circ}} = \frac{h}{\sin(180^{\circ} - 45^{\circ} - \theta)} = \frac{h}{\sin(135^{\circ} - \theta)} = \frac{\sqrt{2}h}{\cos \theta + \sin \theta}$$

• Solving for throat thickness t

$$t = \frac{h}{\cos \theta + \sin \theta}$$

$$t = \frac{h}{\cos \theta + \sin \theta}$$
Fig. 9–9

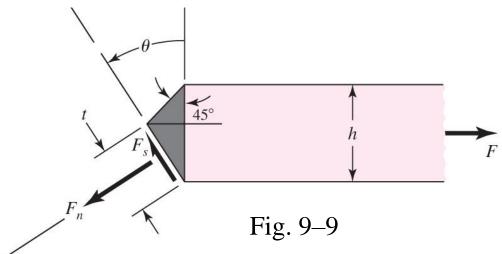
• Nominal stresses at angle θ

$$\tau = \frac{F_s}{A} = \frac{F \sin \theta (\cos \theta + \sin \theta)}{hl} = \frac{F}{hl} (\sin \theta \cos \theta + \sin^2 \theta)$$

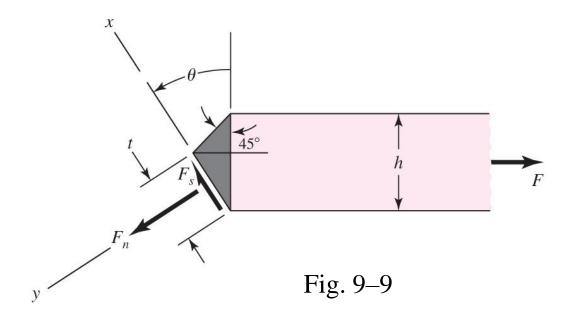
$$\sigma = \frac{F_n}{A} = \frac{F\cos\theta(\cos\theta + \sin\theta)}{hl} = \frac{F}{hl}(\cos^2\theta + \sin\theta\cos\theta)$$

• Von Mises Stress at angle θ

$$\sigma' = (\sigma^2 + 3\tau^2)^{1/2} = \frac{F}{hl} [(\cos^2 \theta + \sin \theta \cos \theta)^2 + 3(\sin^2 \theta + \sin \theta \cos \theta)^2]^{1/2}$$



- Largest von Mises stress occurs at $\theta = 62.5^{\circ}$ with value of $\sigma' = 2.16 F/(hl)$
- Maximum shear stress occurs at θ = 67.5° with value of $\tau_{\rm max}$ = 1.207F/(hl)



Experimental Stresses in Transverse Fillet Weld

• Experimental results are more complex

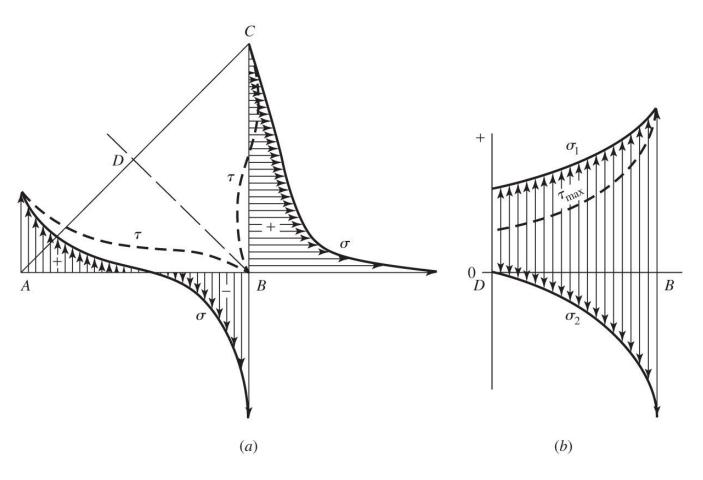


Fig. 9–10

Transverse Fillet Weld Simplified Model

- No analytical approach accurately predicts the experimentally measured stresses.
- Standard practice is to use a simple and conservative model
- Assume the external load is carried entirely by shear forces on the minimum throat area.

$$\tau = \frac{F}{0.707hl} = \frac{1.414F}{hl} \tag{9-3}$$

- By ignoring normal stress on throat, the shearing stresses are inflated sufficiently to render the model conservative.
- By comparison with previous maximum shear stress model, this inflates estimated shear stress by factor of 1.414/1.207 = 1.17.

Parallel Fillet Welds

• Same equation also applies for simpler case of simple shear loading in fillet weld

$$\tau = \frac{F}{0.707hl} = \frac{1.414F}{hl} \tag{9-3}$$

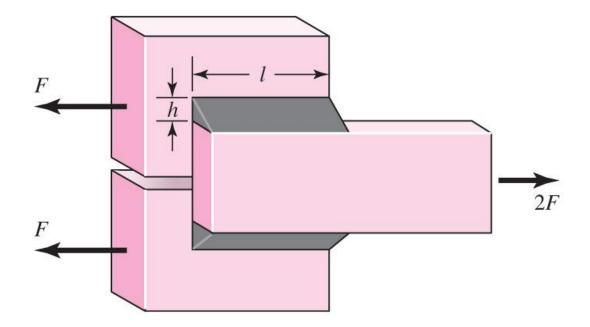


Fig. 9–11

Fillet Welds Loaded in Torsion

- Fillet welds carrying both direct shear *V* and moment *M*
- Primary shear

$$\tau' = \frac{V}{A}$$

Secondary shear

$$\tau'' = \frac{Mr}{J}$$

- A is the throat area of all welds
- r is distance from centroid of weld group to point of interest
- *J* is second polar moment of area of weld group about centroid of group

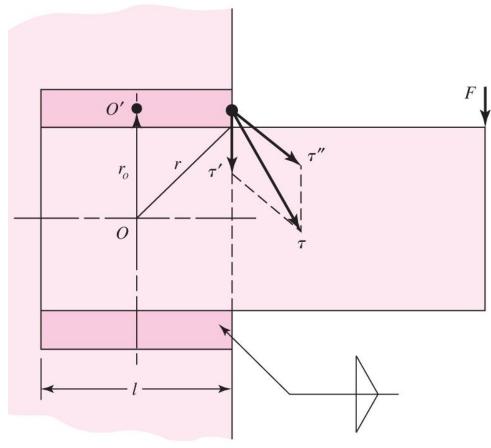


Fig. 9–12

Example of Finding A and J

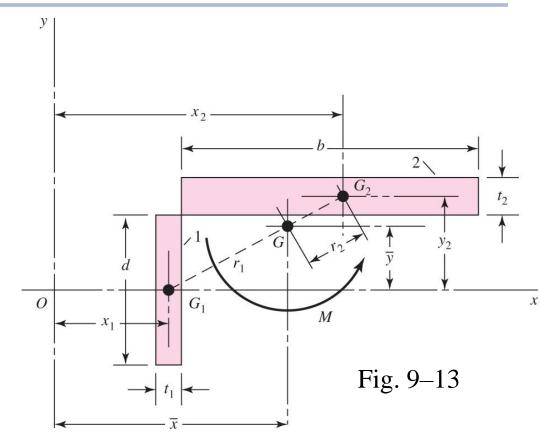
• Rectangles represent throat areas. t = 0.707 h

$$A = A_1 + A_2 = t_1d + t_2b$$

$$I_x = \frac{t_1 d^3}{12} \qquad I_y = \frac{dt_1^3}{12}$$

$$J_{G1} = I_x + I_y = \frac{t_1 d^3}{12} + \frac{dt_1^3}{12}$$

$$J_{G2} = \frac{bt_2^3}{12} + \frac{t_2b^3}{12}$$



$$\bar{x} = \frac{A_1 x_1 + A_2 x_2}{A}$$
 $\bar{y} = \frac{A_1 y_1 + A_2 y_2}{A}$

$$r_1 = [(\bar{x} - x_1)^2 + \bar{y}^2]^{1/2}$$
 $r_2 = [(y_2 - \bar{y})^2 + (x_2 - \bar{x})^2]^{1/2}$

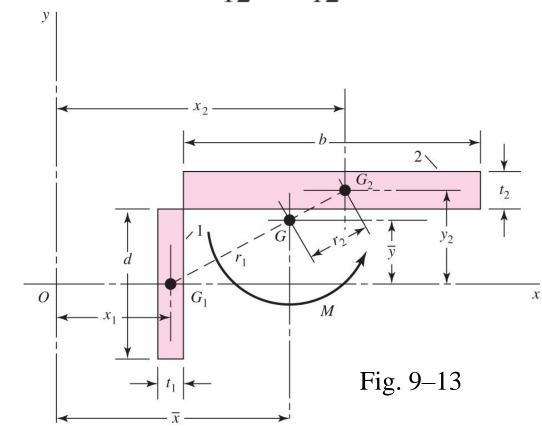
$$J = (J_{G1} + A_1 r_1^2) + (J_{G2} + A_2 r_2^2)$$

Example of Finding A and J

- Note that t^3 terms will be very small compared to b^3 and d^3
- Usually neglected
- Leaves J_{G1} and J_{G2} linear in weld width
- Can normalize by treating each weld as a line with unit thickness *t*
- Results in unit second polar moment of area, J_u
- Since t = 0.707h,

$$J = 0.707hJ_u$$

$$J_{G1} = I_x + I_y = \frac{t_1 d^3}{12} + \frac{dt_1^3}{12}$$
$$J_{G2} = \frac{bt_2^3}{12} + \frac{t_2 b^3}{12}$$



Common Torsional Properties of Fillet Welds (Table 9–1)

Weld	Throat Area	Location of <i>G</i>	Unit Second Polar Moment of Area
1. $\frac{G}{\overline{y}}$ $\frac{1}{\sqrt{\frac{d}{y}}}$	$A = 0.707 \ hd$	$\bar{x} = 0$ $\bar{y} = d/2$	$J_u = d^3/12$
$ \begin{array}{c c} \hline 2. & $	$A = 1.414 \ hd$	$\bar{x} = b/2$ $\bar{y} = d/2$	$J_u = \frac{d(3b^2 + d^2)}{6}$
3. b d	A = 0.707h(b+d)	$\bar{x} = \frac{b^2}{2(b+d)}$ $\bar{y} = \frac{d^2}{2(b+d)}$	$J_u = \frac{(b+d)^4 - 6b^2d^2}{12(b+d)}$

Common Torsional Properties of Fillet Welds (Table 9–1)

4.
$$| \leftarrow b \rightarrow |$$
 $| \leftarrow b \rightarrow |$ $| \leftarrow b \rightarrow |$ $| \rightarrow | \overline{x} |$

$$A = 0.707h(2b + d)$$

$$\bar{x} = \frac{b^2}{2b+d}$$

$$\bar{y} = d/2$$

$$J_u = \frac{8b^3 + 6bd^2 + d^3}{12} - \frac{b^4}{2b+d}$$

5.
$$b \rightarrow G$$
 d

$$A = 1.414h(b+d)$$

$$\bar{x} = b/2$$
$$\bar{y} = d/2$$

$$J_u = \frac{(b+d)^3}{6}$$

$$A = 1.414 \,\pi hr$$

$$J_u = 2\pi r^3$$

*G is centroid of weld group; h is weld size; plane of torque couple is in the plane of the paper; all welds are of unit width.

A 50-kN load is transferred from a welded fitting into a 200-mm steel channel as illustrated in Fig. 9–14. Estimate the maximum stress in the weld.

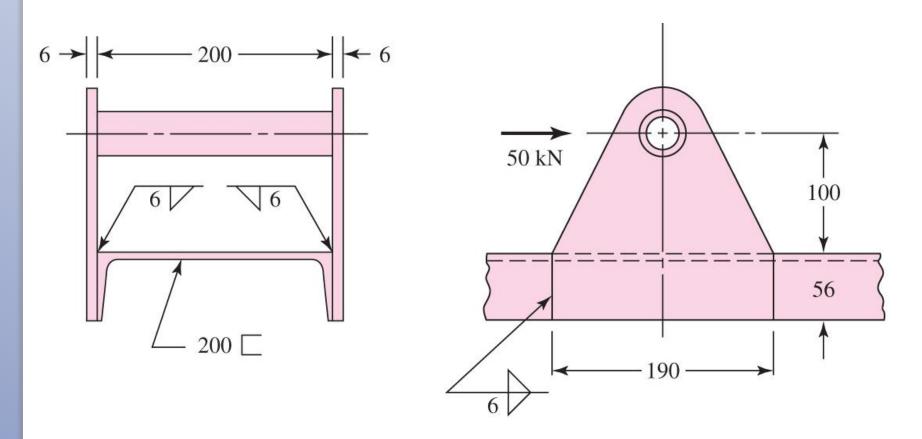
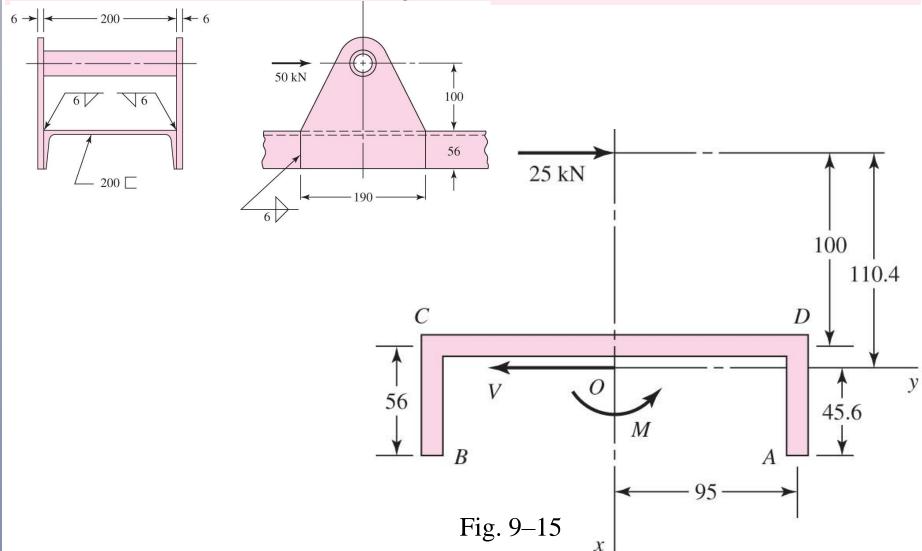


Fig. 9–14

(a) Label the ends and corners of each weld by letter. See Fig. 9–15. Sometimes it is desirable to label each weld of a set by number.

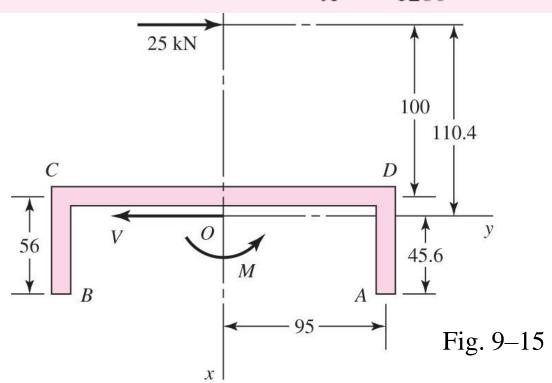


(b) Estimate the primary shear stress τ' . As shown in Fig. 9–14, each plate is welded to the channel by means of three 6-mm fillet welds. Figure 9–15 shows that we have divided the load in half and are considering only a single plate. From case 4 of Table 9–1 we find the throat area as

$$A = 0.707(6)[2(56) + 190] = 1280 \text{ mm}^2$$

Then the primary shear stress is

$$\tau' = \frac{V}{A} = \frac{25(10)^3}{1280} = 19.5 \text{ MPa}$$



- (c) Draw the τ' stress, to scale, at each lettered corner or end. See Fig. 9–16.
- (d) Locate the centroid of the weld pattern. Using case 4 of Table 9–1, we find

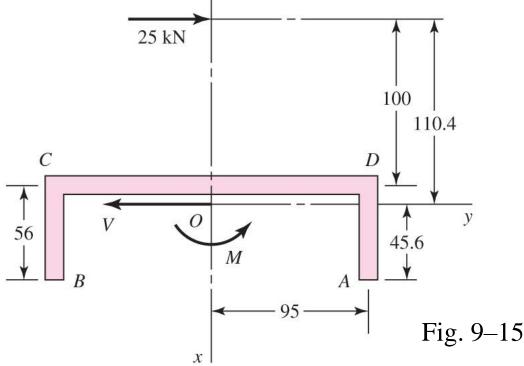
$$\bar{x} = \frac{(56)^2}{2(56) + 190} = 10.4 \text{ mm}$$

This is shown as point O on Figs. 9–15 and 9–16.

(e) Find the distances r_i (see Fig. 9–16):

$$r_A = r_B = [(190/2)^2 + (56 - 10.4)^2]^{1/2} = 105 \text{ mm}$$

 $r_C = r_D = [(190/2)^2 + (10.4)^2]^{1/2} = 95.6 \text{ mm}$



(f) Find J. Using case 4 of Table 9–1 again, with Eq. (9-6), we get

$$J = 0.707(6) \left[\frac{8(56)^3 + 6(56)(190)^2 + (190)^3}{12} - \frac{(56)^4}{2(56) + 190} \right]$$
$$= 7.07(10)^6 \text{ mm}^4$$

(*g*) Find *M*:

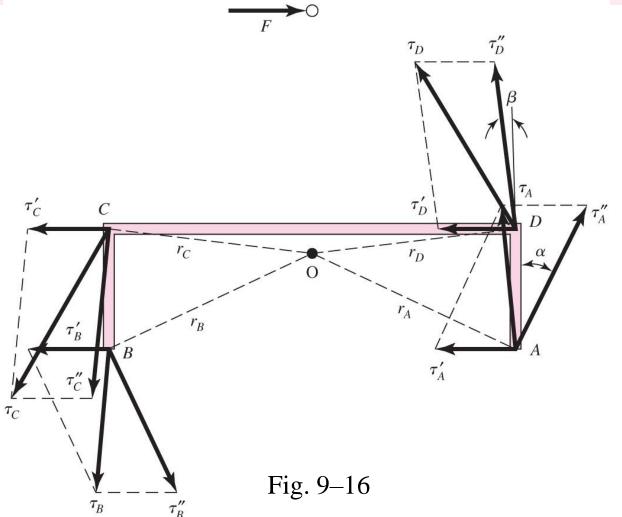
$$M = Fl = 25(100 + 10.4) = 2760 \text{ N} \cdot \text{m}$$

(h) Estimate the secondary shear stresses τ'' at each lettered end or corner:

$$\tau_A'' = \tau_B'' = \frac{Mr}{J} = \frac{2760(10)^3(105)}{7.07(10)^6} = 41.0 \text{ MPa}$$

$$\tau_C'' = \tau_D'' = \frac{2760(10)^3(95.6)}{7.07(10)^6} = 37.3 \text{ MPa}$$

(i) Draw the τ'' stress at each corner and end. See Fig. 9–16. Note that this is a free-body diagram of one of the side plates, and therefore the τ' and τ'' stresses represent what the channel is doing to the plate (through the welds) to hold the plate in equilibrium.



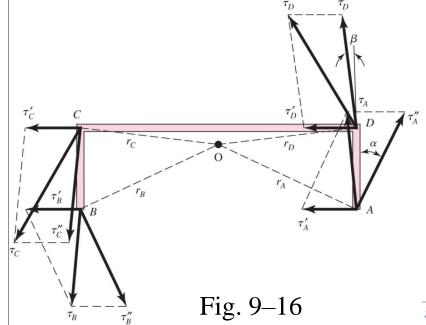
(j) At each point labeled, combine the two stress components as vectors (since they apply to the same area). At point A, the angle that τ_A'' makes with the vertical, α , is also the angle r_A makes with the horizontal, which is $\alpha = \tan^{-1}(45.6/95) = 25.64^{\circ}$. This angle also applies to point B. Thus

$$\tau_A = \tau_B = \sqrt{(19.5 - 41.0 \sin 25.64^\circ)^2 + (41.0 \cos 25.64^\circ)^2} = 37.0 \text{ MPa}$$

Similarly, for *C* and *D*, $\beta = \tan^{-1}(10.4/95) = 6.25^{\circ}$. Thus

$$\tau_C = \tau_D = \sqrt{(19.5 + 37.3 \sin 6.25^\circ)^2 + (37.3 \cos 6.25^\circ)^2} = 43.9 \text{ MPa}$$

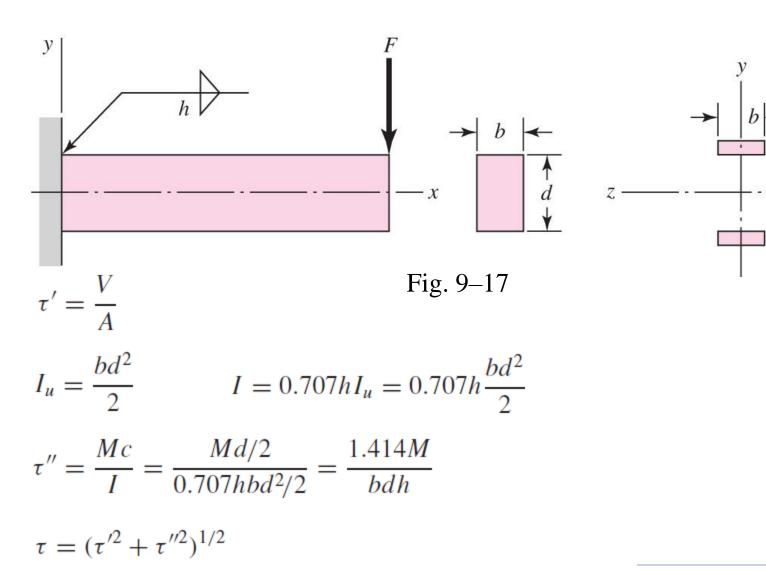
(k) Identify the most highly stressed point: $\tau_{\text{max}} = \tau_C = \tau_D = 43.9 \text{ MPa}$



Shigley's Mechanical Engineering Design

Fillet Welds Loaded in Bending

Fillet welds carry both shear V and moment M



Bending Properties of Fillet Welds (Table 9–2)

Weld	Throat Area	Location of G	Unit Second Moment of Area
1. \overline{y}	A = 0.707hd	$\bar{x} = 0$ $\bar{y} = d/2$	$I_u = \frac{d^3}{12}$
$ \begin{array}{c c} \hline 2. & $	A = 1.414hd	$\bar{x} = b/2$ $\bar{y} = d/2$	$I_u = \frac{d^3}{6}$
3. $ \leftarrow b \rightarrow $ $ \leftarrow b \rightarrow $ $ \leftarrow b \rightarrow $ $ \rightarrow $ $ \overline{x} \leftarrow$	A = 1.414hb	$\bar{x} = b/2$ $\bar{y} = d/2$	$I_u = \frac{bd^2}{2}$
$ \begin{array}{c c} \hline 4. & \leftarrow b \rightarrow \\ \hline \bar{y} \downarrow & \bar{x} \downarrow \\ \hline \rightarrow \bar{x} \downarrow \\ \hline \end{array} $	A = 0.707h(2b + d)	$\bar{x} = \frac{b^2}{2b+d}$ $\bar{y} = d/2$	$I_u = \frac{d^2}{12}(6b+d)$

Bending Properties of Fillet Welds (Table 9–2)

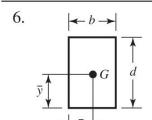
5.
$$\frac{1}{\overline{y}} \xrightarrow{G} G$$

$$A = 0.707h(b + 2d)$$

$$\bar{x} = b/2$$

$$\bar{y} = \frac{d^2}{b+2d}$$

$$I_u = \frac{2d^3}{3} - 2d^2\bar{y} + (b+2d)\bar{y}^2$$



$$A = 1.414h(b+d)$$

$$\bar{x} = b/2$$

$$\bar{y} = d/2$$

$$I_u = \frac{d^2}{6}(3b+d)$$

7.
$$|-b-|$$
 $\overline{y} \updownarrow \uparrow$ $|-\overline{g} \downarrow \uparrow$

$$A = 0.707h(b + 2d)$$

$$\bar{x} = b/2$$

$$\bar{y} = \frac{d^2}{b + 2d}$$

$$I_u = \frac{2d^3}{3} - 2d^2\bar{y} + (b+2d)\bar{y}^2$$

8.
$$G \xrightarrow{g} G \xrightarrow{d} G$$

$$A = 1.414h(b+d)$$

$$\bar{x} = b/2$$
$$\bar{y} = d/2$$

$$I_u = \frac{d^2}{6}(3b+d)$$



$$A = 1.414\pi hr$$

$$l_u = \pi r^3$$

Strength of Welded Joints

- Must check for failure in parent material and in weld
- Weld strength is dependent on choice of electrode material
- Weld material is often stronger than parent material
- Parent material experiences heat treatment near weld
- Cold drawn parent material may become more like hot rolled in vicinity of weld
- Often welded joints are designed by following codes rather than designing by the conventional factor of safety method

Minimum Weld-Metal Properties (Table 9–3)

AWS Electrode Number*	Tensile Strength kpsi (MPa)	Yield Strength, kpsi (MPa)	Percent Elongation
E60xx	62 (427)	50 (345)	17–25
E70xx	70 (482)	57 (393)	22
E80xx	80 (551)	67 (462)	19
E90xx	90 (620)	77 (531)	14–17
E100xx	100 (689)	87 (600)	13–16
E120xx	120 (827)	107 (737)	14

^{*}The American Welding Society (AWS) specification code numbering system for electrodes. This system uses an E prefixed to a four- or five-digit numbering system in which the first two or three digits designate the approximate tensile strength. The last digit includes variables in the welding technique, such as current supply. The next-to-last digit indicates the welding position, as, for example, flat, or vertical, or overhead. The complete set of specifications may be obtained from the AWS upon request.

Stresses Permitted by the AISC Code for Weld Metal

Table 9–4

Type of Loading	Type of Weld	Permissible Stress	n*
Tension	Butt	$0.60S_{y}$	1.67
Bearing	Butt	$0.90S_y$	1.11
Bending	Butt	$0.60-0.66S_y$	1.52-1.67
Simple compression	Butt	$0.60S_y$	1.67
Shear	Butt or fillet	$0.30S_{ut}^{\dagger}$	

^{*}The factor of safety n has been computed by using the distortion-energy theory.

 $^{^{\}dagger}$ Shear stress on base metal should not exceed $0.40S_y$ of base metal.

Fatigue Stress-Concentration Factors

- K_{fs} appropriate for application to shear stresses
- Use for parent metal and for weld metal

Table 9-5

Fatigue Stress-Concentration Factors, K_{fs}

Type of Weld	Kfs
Reinforced butt weld	1.2
Toe of transverse fillet weld	1.5
End of parallel fillet weld	2.7
T-butt joint with sharp corners	2.0

Allowable Load or Various Sizes of Fillet Welds (Table 9–6)

Strength Level of Weld Metal (EXX)										
	60*	70*	80	90*	100	110*	120			
Allowable shear stress on throat, ksi (1000 psi) of fillet weld or partial penetration groove weld										
$\tau =$	18.0	21.0	24.0	27.0	30.0	33.0	36.0			
Allowable Unit Force on Fillet Weld, kip/linear in										
$^{\dagger}f =$	12.73h	14.85 <i>h</i>	16.97 <i>h</i>	19.09 <i>h</i>	21.21 <i>h</i>	23.33h	25.45h			
Leg Size <i>h</i> , in	Allowable Unit Force for Various Sizes of Fillet Welds kip/linear in									
1	12.73	14.85	16.97	19.09	21.21	23.33	25.45			
7/8	11.14	12.99	14.85	16.70	18.57	20.41	22.27			
3/4	9.55	11.14	12.73	14.32	15.92	17.50	19.09			
5/8	7.96	9.28	10.61	11.93	13.27	14.58	15.91			
1/2	6.37	7.42	8.48	9.54	10.61	11.67	12.73			
7/16	5.57	6.50	7.42	8.35	9.28	10.21	11.14			
3/8	4.77	5.57	6.36	7.16	7.95	8.75	9.54			
5/16	3.98	4.64	5.30	5.97	6.63	7.29	7.95			
1/4	3.18	3.71	4.24	4.77	5.30	5.83	6.36			
3/16	2.39	2.78	3.18	3.58	3.98	4.38	4.77			
1/8	1.59	1.86	2.12	2.39	2.65	2.92	3.18			
1/16	0.795	0.930	1.06	1.19	1.33	1.46	1.59			

^{*}Fillet welds actually tested by the joint AISC-AWS Task Committee.

 $^{^{\}dagger} f = 0.707 h \, \tau_{\rm all}.$

Minimum Fillet Weld Size, h (Table 9–6)

Material Thic Thicker Part		Weld Size, in
*To $\frac{1}{4}$ incl.		$\frac{1}{8}$
Over $\frac{1}{4}$	To $\frac{1}{2}$	$\frac{3}{16}$
Over $\frac{1}{2}$	To $\frac{3}{4}$	$\frac{1}{4}$
†Over $\frac{3}{4}$	To 1½	5 16
Over $1\frac{1}{2}$	To $2\frac{1}{4}$	$\frac{3}{8}$
Over $2\frac{1}{4}$	То 6	$\frac{1}{2}$
Over 6		$\frac{5}{8}$

Not to exceed the thickness of the thinner part.

^{*}Minimum size for bridge application does not go below $\frac{3}{16}$ in.

[†]For minimum fillet weld size, schedule does not go above $\frac{5}{16}$ in fillet weld for every $\frac{3}{4}$ in material.

Resistance Welding

- Welding by passing an electric current through parts that are pressed together
- Common forms are spot welding and seam welding
- Failure by shear of weld or tearing of member
- Avoid loading joint in tension to avoid tearing

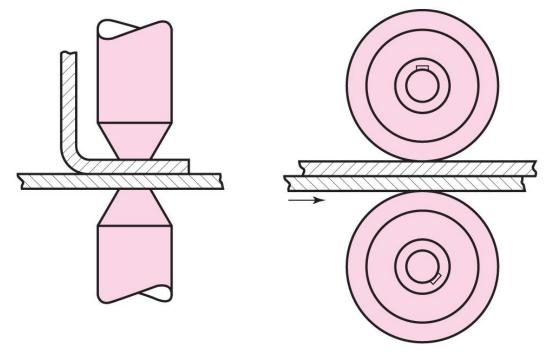
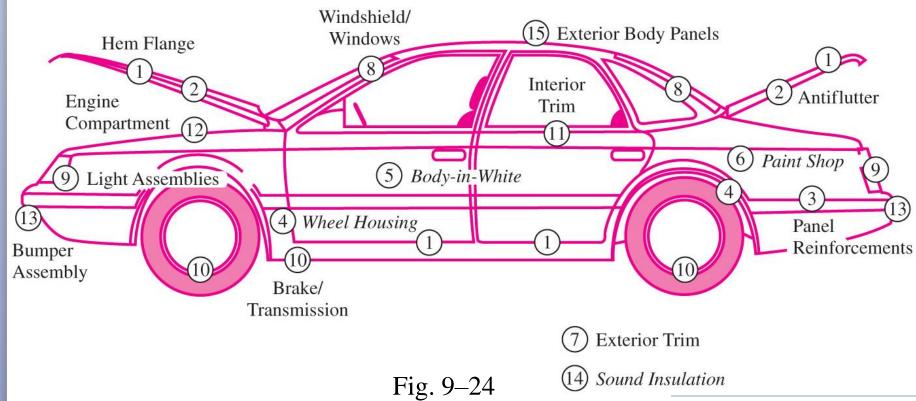


Fig. 9–23

(b)

Adhesive Bonding

- Adhesive bonding has unique advantages
- Reduced weight, sealing capabilities, reduced part count, reduced assembly time, improved fatigue and corrosion resistance, reduced stress concentration associated with bolt holes



Types of Adhesives

- May be classified by
 - Chemistry
 - Epoxies, polyurethanes, polyimides
 - Form
 - Paste, liquid, film, pellets, tape
 - Type
 - Hot melt, reactive hot melt, thermosetting, pressure sensitive, contact
 - Load-carrying capability
 - Structural, semi-structural, non-structural

Mechanical Performance of Various Types of Adhesives

Adhesive Chemistry or Type	Lap-Shed	mperature ır Strength, a (psi)	Peel Strength per Unit Width, kN/m (lbf/in)		
Pressure-sensitive	0.01-0.07	(2–10)	0.18-0.88 (1–5)	
Starch-based	0.07 - 0.7	(10–100)	0.18-0.88	1–5)	
Cellosics	0.35-3.5	(50–500)	0.18–1.8	1–10)	
Rubber-based	0.35-3.5	(50–500)	1.8–7	10–40)	
Formulated hot melt	0.35-4.8	(50–700)	0.88–3.5	5–20)	
Synthetically designed hot melt	0.7-6.9	(100-1000)	0.88–3.5	5–20)	
PVAc emulsion (white glue)	1.4-6.9	(200–1000)	0.88–1.8	5–10)	
Cyanoacrylate	6.9–13.8	(1000-2000)	0.18–3.5	1–20)	
Protein-based	6.9–13.8	(1000–2000)	0.18–1.8	1–10)	
Anaerobic acrylic	6.9–13.8	(1000–2000)	0.18–1.8	1–10)	
Urethane	6.9–17.2	(1000–2500)	1.8-8.8	10–50)	
Rubber-modified acrylic	13.8–24.1	(2000–3500)	1.8–8.8	10–50)	
Modified phenolic	13.8–27.6	(2000–4000)	3.6–7	20–40)	
Unmodified epoxy	10.3–27.6	(1500–4000)	0.35–1.8	2–10)	
Bis-maleimide	13.8–27.6	(2000–4000)	0.18–3.5	1–20)	
Polyimide	13.8–27.6	(2000–4000)	0.18-0.88	1–5)	
Rubber-modified epoxy	20.7-41.4	(3000–6000)	4.4–14 (2	25–80)	

Table 9–7

Stress Distributions

- Adhesive joints are much stronger in shear loading than tensile loading
- Lap-shear joints are important for test specimens and for practical designs
- Simplest analysis assumes uniform stress distribution over bonded area
- Most joints actually experience significant peaks of stress

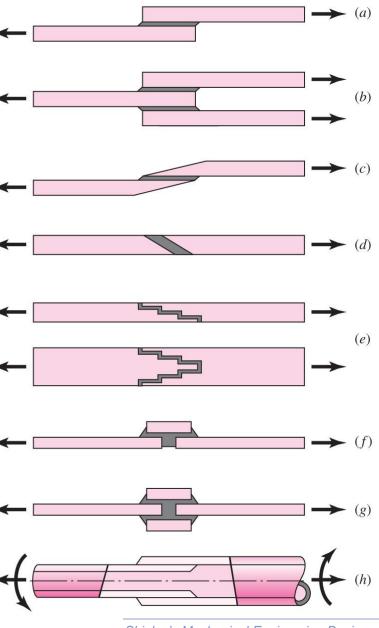
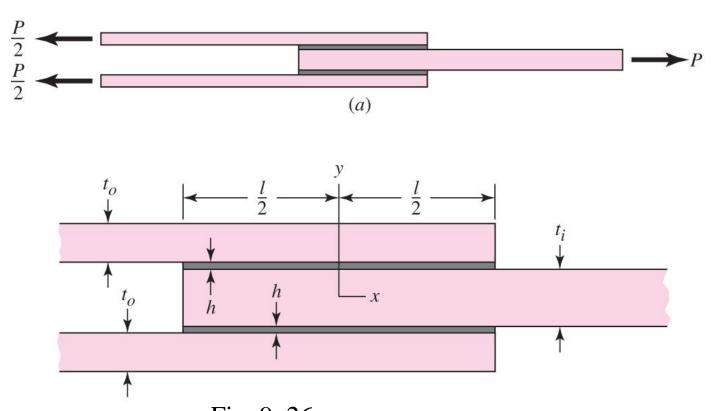


Fig. 9–25

Shigley's Mechanical Engineering Design

Double-lap Joint

- Classic analysis of double-lap joint known as shear-lag model
- Double joint eliminates complication of bending from eccentricity

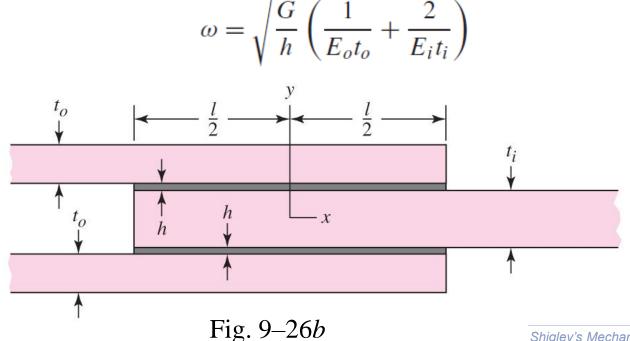


Double-lap Joint

Shear-stress distribution is given by

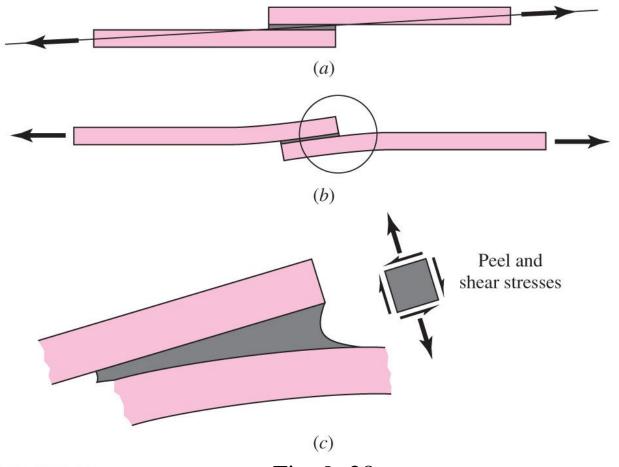
$$\tau(x) = \frac{P\omega}{4b \sinh(\omega l/2)} \cosh(\omega x) + \left[\frac{P\omega}{4b \cosh(\omega l/2)} \left(\frac{2E_o t_o - E_i t_i}{2E_o t_o + E_i t_i} \right) + \frac{(\alpha_i - \alpha_o) \Delta T\omega}{(1/E_o t_o + 2/E_i t_i) \cosh(\omega l/2)} \right] \sinh(\omega x)$$
(9-7)

where



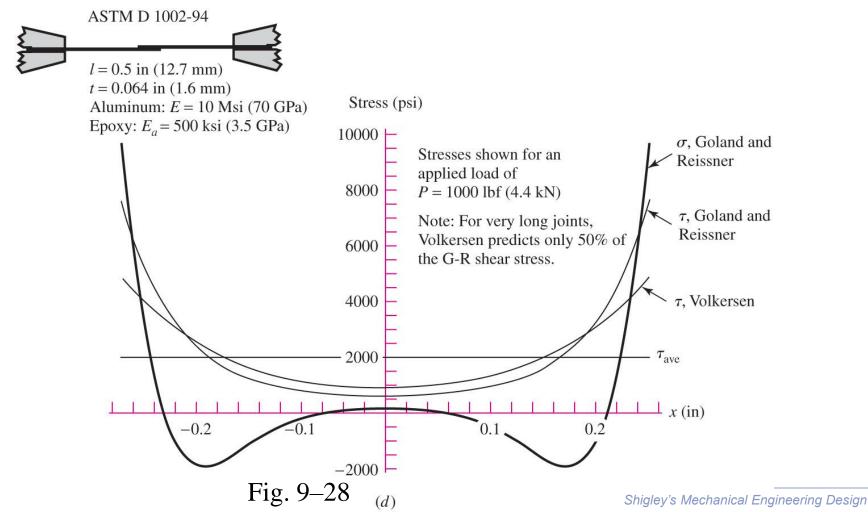
Single-lap Joint

- Eccentricity introduces bending
- Bending can as much as double the resulting shear stresses
- Near ends of joint peel stresses can be large, causing joint failure



Single-lap Joint

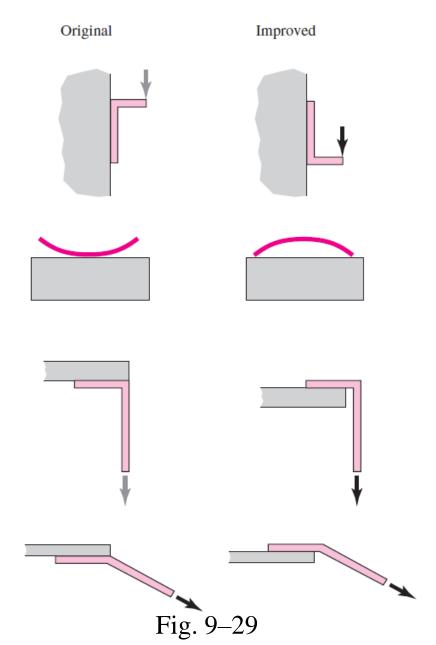
- Shear and peal stresses in single-lap joint, as calculated by Goland and Reissner
- Volkersen curve is for double-lap joint



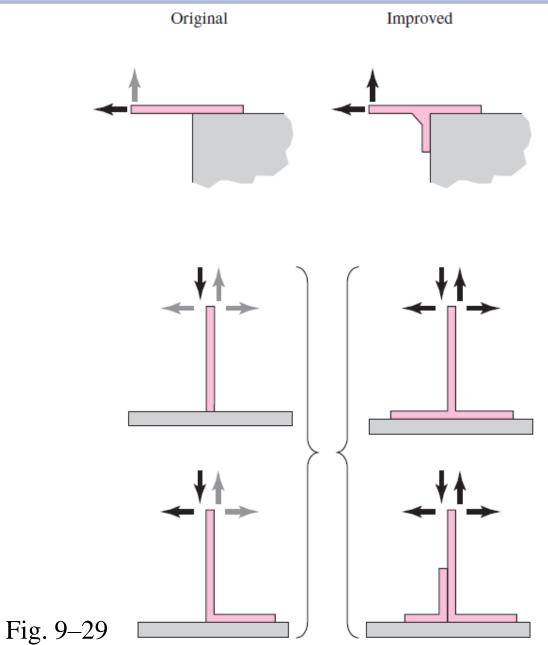
Adhesive Joint Design Guidelines

- Design to place bondline in shear, not peel.
- Use adhesives with adequate ductility to reduce stress concentrations and increase toughness to resist debond propagation.
- Recognize environmental limitations of adhesives and surface preparation.
- Design to facilitate inspection.
- Allow sufficient bond area to tolerate some debonding before becoming critical.
- Attempt to bond to multiple surfaces to support loads in any direction.
- Consider using adhesives in conjunction with spot welds, rivets, or bolts.

Design Ideas for Improved Bonding



Design Ideas for Improved Bonding



Design Ideas for Improved Bonding

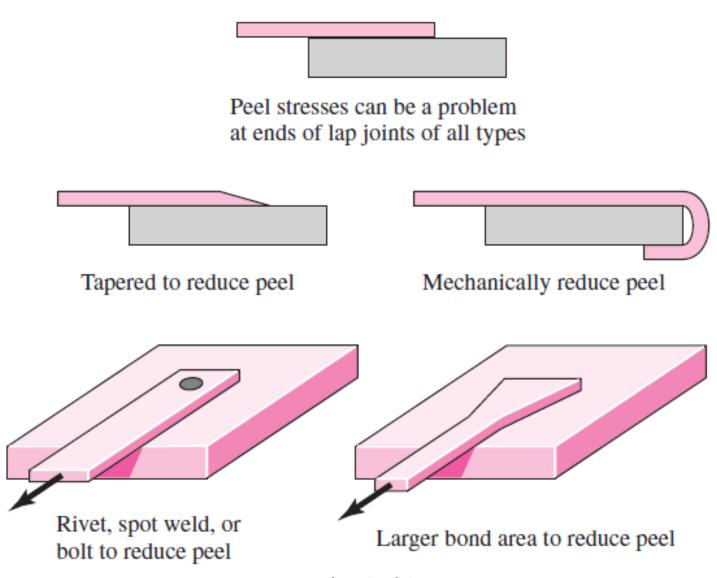


Fig. 9–29