

# Music Classification Using Kolmogorov Distance

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**Abstract.** We evaluate the music composer classification using an approximation of the Kolmogorov distance between different music pieces. The distance approximation has recently been suggested by Vitanyi and his colleagues. They use a clustering method to evaluate the distance metric. However the clustering is too slow for large (>60) data sets. We suggest using the distance metric together with a k-nearest neighbor classifier. We measure the performance of the distance metric based on the test classification accuracy of the classifier. A classification accuracy of 79% is achieved for a training data set of 57 midi files from three different classical composers. We find out that the classification accuracy increases with training set size. The performance of the metric seems to also depend on different pre-processing methods, hence domain knowledge and input representation could make a difference on how the distance metric performs.

## 1 Introduction

Recently Vitanyi and his colleagues (Cilibrasi and Vitanyi, Cilibrasi et.al., Li et. al.) have suggested using an approximation to Kolmogorov distance between two musical pieces as a means to compute clusters of music. They first process the MIDI representation ([www.midi.org](http://www.midi.org)) of a music piece to turn it into a string from a finite alphabet. Then they compute the distance between two music pieces using their Normalized Compression Distance (NCD). NCD uses the compressed length of a string as an approximation to its Kolmogorov Complexity.

Although the Kolmogorov Complexity of a string is not computable, the compressed length approximation seems to have given good results for musical genre and composer clustering in (Cilibrasi et.al.) and other data sets (Keogh et.al.). (Cilibrasi et.al.) note that the clustering performance decreases as the data size increases. In this paper, we investigate how the performance of the distance metric changes with data set size. In order to be able to quantify our results better, instead of clustering, we use classification. We classify the composer of a new music piece based on a set of training data from different composers. We use k-nearest neighbor (Bishop 57) as the classifier, since it only requires the distance between feature vectors.

Like Vitanyi and colleagues, we also work on midi (see [www.midi.org](http://www.midi.org)) files. Although there is loss of quality and information from mp3 or wav to midi format and midi has its other limitations, this format takes a lot less space, is widely accepted and allows for better comparison between music pieces played on different instruments. In this paper we use different pre-processing methods of midi files and also report how pre-processing affects the performance of the classifier. Polyphonic to monophonic conversions at different time two intervals and using the difference between notes at consecutive time intervals versus normalized notes with respect to the mathematical mode of the notes in the piece are the four different pre-processing methods that we investigate.

In our data set, we use midi music pieces from 3 different classical composers (Bach, Chopin, Debussy). The midi data we use was gathered from the internet.

## 2 Normalized Compression Distance (NCD)

For completeness of the paper, we repeat the derivation of the NCD (Cilibrasi et.al.) or K-metric (Ming and Sleep). Please see the references for more information.

Given a string  $x$  from a finite alphabet,  $K(x)$ , the Kolmogorov Complexity of  $x$ , is the length of the shortest program that can output  $x$  and halt (Cover 147).  $K(x)$  can also be considered the length of the shortest compressed binary version from which  $x$  can be fully reproduced or the amount of information, number of bits in  $x$  (Cilibrasi et.al.).  $K(x|y)$  can be considered the minimum number of bits to produce  $x$  from string  $y$ . We approximate  $K(x)$  by the compressed length of  $x$ . For  $K(x|y)$  we use the approximation  $K(x|y) \approx K(xy) - K(x)$  where  $xy$  is the concatenation of strings  $x$  and  $y$ .

We approximate the distance between strings  $x$  and  $y$  using the Kolmogorov distance approximation as follows:

$$d(x,y) = \frac{\max\{K(x|y), K(y|x)\}}{\max\{K(x), K(y)\}} \quad (1)$$

This distance metric approximates the distance between  $x$  and  $y$  well in the sense that  $d(x,y) \leq f(x,y) + O(\log(k)/k)$  where  $k = \max\{K(x), K(y)\}$ .

We should note that, even though this distance approximation seems to work well in practice (Keogh et.al), it needs to be used carefully. Because, although the compressed length of  $x$  is an upper bound on  $K(x)$ , due to the subtraction and division operations,  $d(x,y)$  may over or underestimate the distance between  $x$  and  $y$ . It should also be noted that as the string  $x$  becomes less complicated the error term  $O(\log(k)/k)$  becomes more pronounced. Hence

this distance approximation may work better for more dimensional/more complicated inputs  $x$  and worse for less dimensional/less complicated inputs.

### 3 Details of the Experiments

#### 3.1 Midi Data

In order to compare our results with the original paper (Cilibrasi and Vitanyi), we included their 12 classical pieces in our data set: J.S. Bach's "Wohltemperierte Klavier II: Preludes and Fugues 1,2", Chopin's "Préludes op. 28: 1, 15, 22, 24 and Debussy's "Suite Bergamasque," four movements. In order to be able to compare the performance of the classification algorithm as the data set size changes, we added 16 more pieces by each of the three composers into our data set. Thus we experimented with a total of 60 midi files. The midi data we use was gathered from the internet.

#### 3.2 Midi Pre-Processing

We first discard information about the instruments, composer, song name etc. from the midi file. Like (Cilibrasi et.al.) we sample the music at 5 ms intervals. We also use 1 ms sampling intervals. Unlike them, though, we do a polyphonic to monophonic music conversion and take the tempo variations into account. At each time interval, we examine all the tracks and channels and determine which notes are on within that interval. Then, we use the note with the maximum pitch as the note to represent that time interval (Doraisamy and Rürger, Uitdenbogerd and Zobel). We convert each note to an integer. When there is no note in a certain time interval we denote that with a special integer. After this, we output the string  $x$  to represent the musical piece in two different ways:

- 1) Determine the (mathematical) mode (i.e. the note that sounds most often) among the monophonic notes for the whole piece. Subtract the mode from each note. Output the mode followed by the normalized notes, using one byte per note in binary.
- 2) Use the difference between the notes at each consecutive time intervals. Output the first note, followed by the note differences. Again we use one byte per note and the output is a binary string.

### 3.3 Distance Matrix Computation

We used the publicly available software by Vitanyi and colleagues at [complearn.sourceforge.net](https://complearn.sourceforge.net) to compute the distances between note strings. We used the default bzip2 as the compression algorithm.

### 3.4 Classification

Since  $d(x,y)$  is a distance metric, it is possible to construct a nearest neighbour classifier using it. We use k-nearest neighbour with

- 1)  $k=1$ ,
- 2)  $k=3$ .

A k-nearest neighbour classifier stores the available training data. When a new data point needs to be classified, it computes the distance between the new data point and the training data. It chooses the k closest training data and chooses the label (in our case the composer) that occurs most frequent among those k training data points.

We evaluate how good a particular midi pre-processing method or classifier performs using the following version of leave one out cross validation: Among all data points, we randomly choose one data point per class as the test data. From the remaining data we choose the training data according to the training set size. We compute the classification accuracy for this partition as the ratio of points in test data that are classified correctly. In order to get error bars on the classification accuracy, for each pre-processing method and classification algorithm, we repeat the partitioning and testing process for 200 times.

## 4 Results

Table 1 shows the composer classification accuracy for training set of size 57 for different pre-processing methods (columns) and classification methods (rows). Using 1 nearest neighbor classifier and pre-processing at 1 ms and taking the difference between consecutive monophonic notes seem to give the best result, an accuracy of 79%. Table 2 shows the confusion matrices for two different pre-processing methods and classifiers and 200 different training-test set partitionings. The training set was of size 57 and test set was of size 3. While Bach and Debussy are less confused with the others, Chopin's works seem to have more similarities to other two composers'.

**Table 1.** Composer classification test accuracy for different pre-processing and classification methods. Training set size is 57 and test set size is 3

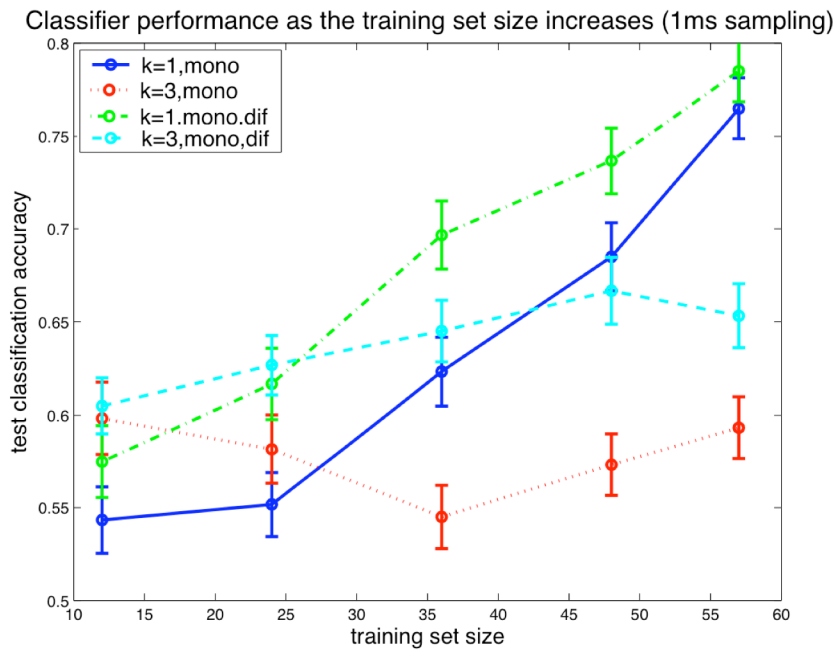
	Pre-process at 1 ms		Pre-process at 5ms	
	No difference	Difference	No difference	Difference
1-nearest neighbor	$0.77 \pm 0.02$	<b><math>0.79 \pm 0.02</math></b>	<b><math>0.70 \pm 0.02</math></b>	$0.68 \pm 0.02$
3-nearest neighbor	$0.59 \pm 0.02$	$0.65 \pm 0.02$	$0.64 \pm 0.02$	$0.69 \pm 0.02$

**Table 2.** The confusion matrices for two different classifiers highlighted in table 1

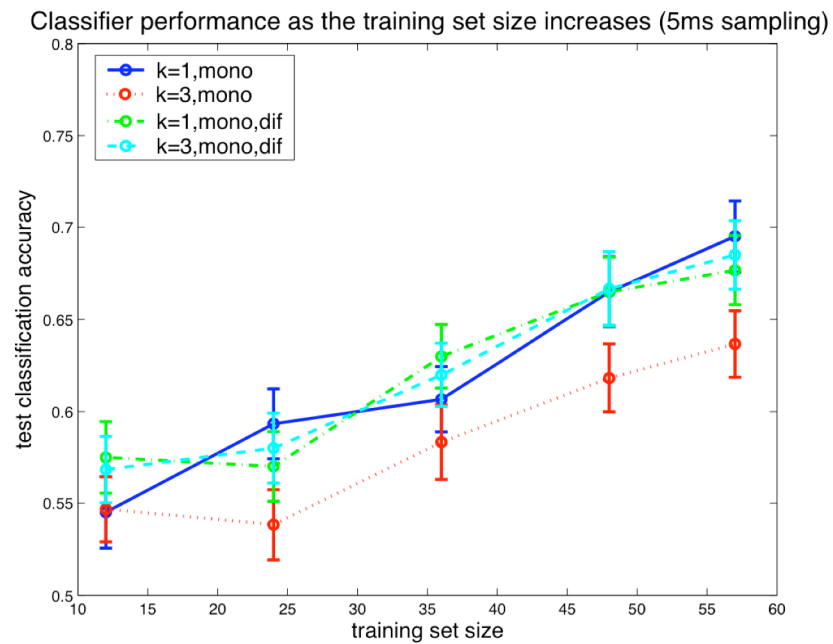
		Predicted					
		1ms, dif, 1-nearest neighbor			5ms, no difference, 1-nearest neighbor		
		Bach	Chopin	Debussy	Bach	Chopin	Debussy
Actual	Bach	171	16	13	137	26	37
	Chopin	26	122	52	19	132	49
	Debussy	8	26	166	7	45	148

Figures 1 and 2 show the classifier performance as the training set size increases. The classifiers perform better as more training data is available. This contradicts the finding that as more data is available clustering gets worse (Cilibrasi and Vitanyi). Our interpretation is, as the data set size increases some pieces are clustered wrong, however their ratio to the total number of data points gets less as more data becomes available.

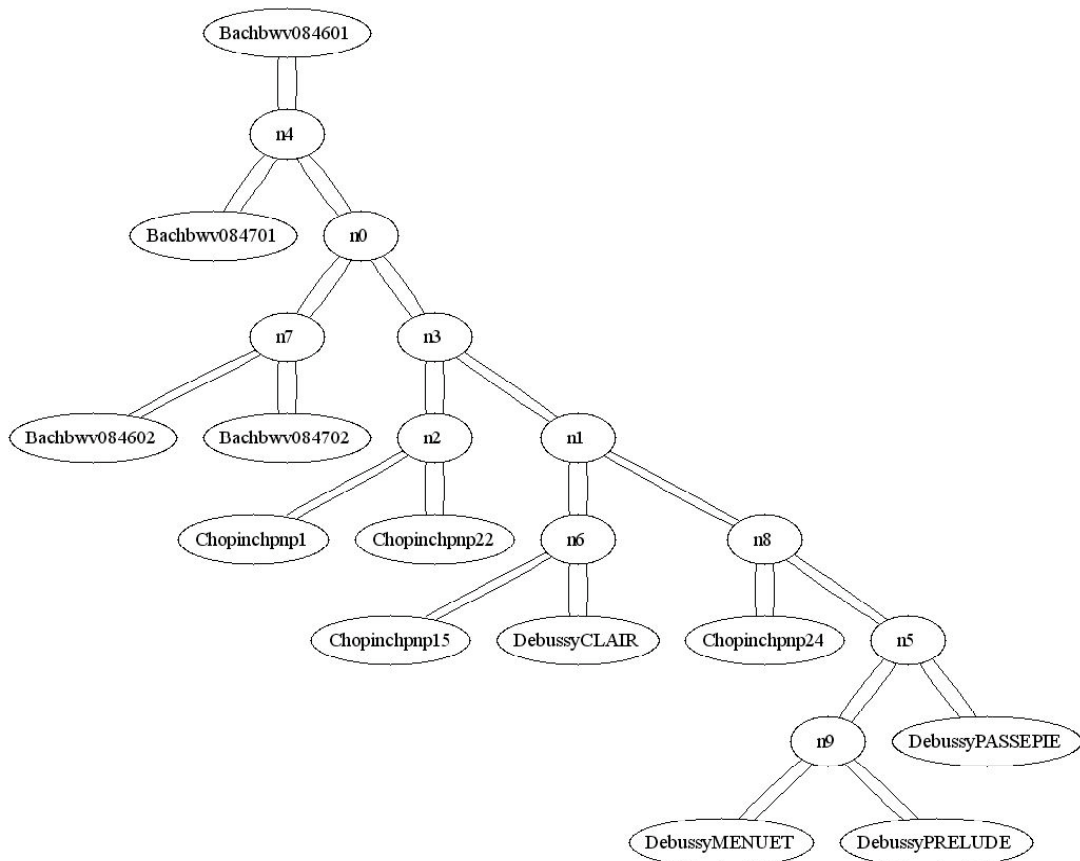
In figure 3 we show the clusters found by the complearn program using one of our four different midi pre-processing methods. This verifies that our monophonic conversion works as well as the polyphonic pre-processing used by (Cilibrasi and Vitanyi). We could not produce the cluster graph for size 60 data set even after 10 hours of processing time on a P4 1.8 GHz laptop.



**Fig. 1.** The test classification accuracy for classical 60 data set at 1ms sampling. The classification accuracy increases as the training set size increases. Using 1 nearest neighbor with difference pre-processing algorithm performs best.



**Fig. 2.** The test classification accuracy for classical 60 data set at 5ms sampling. Again, the classification accuracy increases as the training set size increases. Using 1 nearest neighbor with difference pre-processing algorithm still performs quite well. However the accuracy level is less than that of 1ms for all methods.



**Fig. 3.** The cluster produced by the complearn (complearn.sourceforge.net) program for the size 12 classical data set using monophonic conversion and difference between time slices of 5ms.

## 5 Conclusion

In this paper we showed how the Kolmogorov distance measure and k-nearest neighbour classifier performs for composer classification of midi files. We found out that the distance measure works better as more training data is available. We also found out that, the distance metric may perform different with different input data pre-processing methods.

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