

TABLE: SELECTED DIMENSIONAL EQUIVALENTS

Length	<p>1 m = 3.280 ft 0.39,37 in 1 cm = 10^{-2} m = 0.394 in = 0.038 ft 1 mm = 10^{-3} m 1 micron (m) = 10^{-10} m 1 Angstrom (°A) 10^{-6} m</p>
Time	<p>1 hr = 3600 sec = 60 min 1 milisecc = 10^{-3} sec 1 microsec (µsec) = 10^{-6} sec 1 nanosec (nsec) = 10^{-9} sec</p>
Mass	<p>1 kg = 1000 gr = 2.2046 lbm = 6.8521×10^{-3} slugs 1 slugs = 1 lbf.sec⁻²/ft = 32.174 lbm 1 amu = 1.66×10^{-27} kg</p>
Force	<p>1 newton = 1 kg.m/sec² 1 dyne = 1 gr.cm/sec² 1 lbf = 4.448×10^5 dyne = 4.448 newtons</p>
Energy	<p>1 joule = 1 kg.m²/sec² = 0.239 cal = 0.738 ft.lb = 2.78×10^{-7} kwh 1 joule = 10^7 erg 1 Btu = 778.18 ft.lb = 1.055×10^{15} erg = 252 cal 1 cal = 4.186 joule 1 erg = 1 gr.cm²/sec² 1 eV = 1.602×10^{-19} joules = 160×10^{-12} erg</p>
Power	<p>1 Watt = 1 kg.m²/sec³ = 1 joule/sec 1 hp = 550 ft.lbf/sec 1 hp = 2545 Btu/hr = 746 Watts 1 kWatt = 1000 Watts = 3413 Btu/hr</p>
Pressure	<p>1 atm = 14.696 lbf/in² = 760 torr 1 mmHg = 0.01931 lbf/in² = 1 torr 1 dyne/cm² = 145.04×10^{-7} 1 bar = 14.504 lbf/in² = 10^6 dynes/cm² 1 micron (µ) = 10^{-6} mmHg = 10^{-3} mmHg 1 pascal (Pa) = 1 N/m² = 1 kg/(m·s²) 1 hPa = 1 mb 1 hPa = 100 Pa</p>
Volume	<p>1 gal = 0.13368 ft³ 1 liter = 1000.028 cm³</p>
Temperature	<p>1 °K = 1 °C = 1.8 °F = 1.8 °R 0 °C corresponds to 32 °F, 273.16 °K, and 491.69 °R 1 eV = 11600 °K</p>
Magnetic Quantities	<p>1 Gauss = 1 g^{1/2}/cm^{1/2}.sec 1 Gauss = 10^3 coul/m.sec for M 1 Gauss = $(1/4\pi) \times 10^3$ coul/m.sec for H 1 Gauss = 10^{-4} Tesla for B 1 Tesla = 1 kg/coul.sec 1 Tesla = 1 kg/A.sec² 1 nT = 10^{-9} Tesla 1 nT = 10^{-5} Gauss 1 gamma = 1 g = 1 nT</p> <p>Magnetic Flux: $\phi_B = \int B \cdot dA$, 1 Weber = 1 kg.m²/coul.sec</p> <p>$\vec{B} = \text{kg/sec.coul}$</p>
Electrical Quantities	<p>E-potential: $\mathcal{E}, d\mathcal{E} = \vec{E} \cdot d\vec{l}$ E, 1 volt = 1 kg.m²/coul.sec²</p> <p>$\vec{E} = \text{kg.m/coul.sec}$</p> <p>Current Density: coul/m².sec Current: coul/sec Resistance (R): 1 ohm = 1 kg.m²/coul².sec</p>

PHYSICAL CONSTANTS

Avogadro's Number	$N = 6.025 \times 10^{23} / \text{g.mole}$
Bolzman's Constant	$k = 1.38 \times 10^{-23} \text{ joule /}^\circ\text{K}$
Stefan Boltzmann Constant	$\sigma = 5.7 \times 10^{-5} \text{ erg/cm}^2 \cdot \text{sec.}^\circ\text{K}^4$ $\sigma = 5.67 \times 10^{-8} \text{ joule/m}^2 \cdot \text{sec.}^\circ\text{K}^4$
Gas Constant	$R = 1545.33 \text{ ft.lbf/lb.mole.}^\circ\text{R}$ $R = 8.317 \text{ joule/g-mole.}^\circ\text{K}$ $R = 8317 \text{ joule/kg-mole.}^\circ\text{K}$ $R = 1.986 \text{ Btu/lb.mole.}^\circ\text{R}$ $R = 1.986 \text{ cal/g.mole.}^\circ\text{K}$
Planck's Constant	$h = 6.625 \times 10^{-34} \text{ joule.sec}$
Biot-Savart Constant	$1/4\pi\epsilon_0 = 8.987 \times 10^9 \text{ kg.m}^3/\text{coul}^2 \cdot \text{sec}^2$ $\mu_0/4\pi = 1.000 \times 10^{-7} \text{ kg.m/coul}^2$
Electronic Charge	$e = -1.6021 \times 10^{-19} \text{ coul}$
Proton Mass	$m_p = 1.67 \times 10^{-27} \text{ kg}$
Electron Mass	$m_e = 9.1 \times 10^{-31} \text{ kg}$
Speed of Light	$c = 2.998 \times 10^8 \text{ m/sec}$
Newton's Constant	$g_c = 32.174 \text{ ft.lbm/lbf.sec}^2$
Gravitational Constant	$k_G = 6.67 \times 10^{-11} \text{ m}^3/\text{kg.sec}^2$
Wienn's Constant	$c = 0.28 \text{ cm.}^\circ\text{K}$
Sun-Earth Distance	$1 \text{ AU} = 1.5 \times 10^8 \text{ km}$
Solar Constant for Earth	$I_o = 1.94 \text{ cal/cm}^2 \cdot \text{min}$ $I_o = 1370 \text{ Watt/m}^2$
Sun's Radius	$R_{\text{sun}} = 7 \times 10^5 \text{ km}$
Sun's Mass	$M_{\text{sun}} = 2 \times 10^{30} \text{ kg}$
Sun's Surface Temperature	$T = 6000 \text{ }^\circ\text{K}$
Sun's Luminosity	$L = 4 \times 10^{26} \text{ Watt}$
Earth's Radius	$R_{\text{Earth}} = 6378 \text{ km}$
Earth's Albedo	$A \text{ or } \alpha = \% 33 \text{ or } 0.33$
Magnetic Field at the Earth's Equator	$B_o = 0.36 \text{ Gauss (CGS)}$ $B_o = 0.3 \times 10^{-4} \text{ Tesla (MKS)}$
μ_o	$\mu_o = 4\pi \times 10^{-7} \text{ (MKS, Henry/m, or kg.m/coul}^2, \text{ Henry} = \text{kg.m}^2/\text{coul}^2)$
<p>R : Universal Gas Constant R^* : Specific Gas Constant $R^* = (R \times 10^3) / M$, $M = 29 \text{ amu for Air}$ $R^* = (8.317 \times 10^3) / 29 = 286 \text{ (MKS)}$ $P = \rho R^* T \text{ or } PV = RT$</p>	

Symbol	MKS (SI)	CGS (Gaussian System)
Length	1 m	10^2 cm
Mass	1 kg	10^3 g
Time	1 s, 1 sec	1 s, 1 sec
Force	1 N	10^5 dynes
Work or Energy	1 J	10^7 erg
Power	1 W	10^7 ergs/s
Charge	1 C	3×10^9 statcoul
Current	1 A	3×10^9 statamp
Electric Field Strength	1 V/m	$(1/3) \times 10^{-4}$ statvolt/cm
Electric Potential	1 V	(1/300) statvolt
Electric Polarization	1 C/m ²	3×10^5 statcoul/cm ²
Electric Displacement	1 C/m ²	$12\pi \times 10^5$ statvolt/cm ²
Resistance	1 Ω	$(1/9) \times 10^{-11}$ s/cm
Capacitance	1 F	9×10^{11} cm
Magnetic Flux	1 Wb	10^8 Maxwells
Magnetic Induction	1 T	10^4 Gauss
Magnetic Field Strength	1 A-turn/m	$4\pi \times 10^3$ Gauss

To convert to	Multiply by
kilo	10^3
mega	10^6
giga	10^9
centri	10^{-2}
mili	10^{-3}
micro	10^{-6}
nano	10^{-9}
pico	10^{-12}
ppmv = one per million	10^{-6}
ppbv = one per billion	10^{-9}
pptv = one per trillion	10^{-12}

LENGTH

- 1 kilometer (km) = 1000 meters (m)
= 3281 feet (ft)
= 0.62 mile (mi)
- 1 mile (mi) = 5280 feet (ft)
= 1609 meters (m)
= 1.61 kilometers (km)
- 1 centimeter (cm) = 0.39 inch (in.)
= 0.01 meter (m)
- 1 inch (in.) = 2.54 cm
= 0.08 ft
- 1 meter (m) = 100 cm
= 3.28 ft
= 39.37 in.
- 1 micrometer (μm) = 0.0001 cm
= 0.000001 m

AREA

- 1 square centimeter (cm^2) = 0.15 in.²
1 square inch (in.²) = 6.45 cm²
1 square meter (m^2) = 10.76 ft²
1 square foot (ft²) = 0.09 m²

VOLUME

- 1 cubic centimeter (cm^3) = 0.06 in.³
1 cubic inch (in.³) = 16.39 cm³
1 liter (l) = 1000 cm³

SPEED

- 1 knot = 1.15 mph
= 0.51 mps
= 1.85 kph
- 1 mile per hour (mph) = 0.87 knot
= 0.45 mps
= 1.61 kph
- 1 kilometer per hour (kph) = 0.54 knot
= 0.62 mph
= 0.28 mps
- 1 meter per second (mps) = 1.9 knots
= 2.2 mph
= 3.6 kph

A

UNITS, CONVERSIONS, AND ABBREVIATIONS

MASS

- 1 gram (g) = 0.035 ounce
= 0.002 lb
- 1 kilogram (kg) = 1000 g
= 2.2 lb

ENERGY

- 1 joule (J) = 0.239 cal
1 calorie (cal) = 4.187 J

PRESSURE

- 1 millibar (mb) = 1000 dynes/cm²
= 0.75 millimeter of mercury
= 0.03 inch of mercury
= 0.01 pound per square
inch (psi)
= 100 pascals (Pa)
- 1 standard atmosphere = 1013.25 mb
= 760 millimeters of
mercury
= 29.92 inches of
mercury
= 14.7 psi

Appendix A

Conversion to SI Units

Physical quantity	Unit	SI (MKS) equivalent
Length	ft	0.305 m
	μm	10^{-6} m
	nm	10^{-9} m
Time	day	8.64×10^4 s
Mass	lb	0.454 kg
Temperature	$^{\circ}\text{F}$	$273 + (^{\circ}\text{F} - 32)/1.8$ K
Volume	liter	10^{-3} m ³
Velocity	mph	0.447 m s^{-1}
	knots	0.515 m s^{-1}
	km hr^{-1}	0.278 m s^{-1}
	fps	0.305 m s^{-1}
Force	kg m s^{-2}	1 N
	lb	0.138 N
	dyne	10^{-5} N
Pressure	N m^{-2}	1 Pa
	bar	10^5 Pa
	mb	$10^2 \text{ Pa} = 1 \text{ hPa}$
Energy	$\text{kg m}^2 \text{ s}^{-2}$	1 J
	Nm	1 J
	erg	10^{-7} J
	cal	4.187 J
Power	$\text{kg m}^{-2} \text{ s}^{-3}$	1 W
	J s^{-1}	1 W
	Langley day^{-1}	$4.84 \times 10^{-1} \text{ W m}^{-2}$
Specific heat	cal gm^{-1}	$4.184 \times 10^3 \text{ J kg}^{-1}$
Energy flux	$\text{cal cm}^{-2} \text{ min}^{-1}$	$6.97 \times 10^2 \text{ W m}^{-2}$

Appendix B

Thermodynamic Properties of Air and Water

Dry Air

Mean molecular weight	$M_d = 28.96 \text{ g mol}^{-1}$
Specific gas constant	$R = 287.05 \text{ J kg}^{-1} \text{ K}^{-1}$
Density	$\rho = 1.293 \text{ kg m}^{-3}$ (at STP*)
Number density (Loschmidt number)	$n = 2.687 \times 10^{25} \text{ m}^{-3}$ (at STP)
Isobaric specific heat capacity	$c_p = 1.005 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Isochoric specific heat capacity	$c_v = 7.19 \times 10^2 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Ratio of specific heats	$\gamma = c_p/c_v = 1.4$
	$\kappa = (\gamma - 1)/\gamma = R/c_p = 0.286$
Coefficient of viscosity	$\mu = 1.73 \times 10^{-5} \text{ kg m}^{-1} \text{ s}^{-1}$ (at STP)
Kinematic viscosity	$\nu = 1.34 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$ (at STP)
Coefficient of thermal conductivity	$k = 2.40 \times 10^{-2} \text{ W m}^{-1} \text{ K}^{-1}$ (at STP)
Sound speed	$c_s = 331 \text{ m s}^{-1}$ (at 273 K)

Water

Mean molecular weight	$M_v = 18.015 \text{ g mol}^{-1}$
	$\epsilon = M_v/M_d = 0.622$
Specific gas constant	$R = 461.51 \text{ J kg}^{-1} \text{ K}^{-1}$
Density (liquid water)	$\rho = 10^3 \text{ kg m}^{-3}$ (at STP)
Density (ice)	$\rho = 9.17 \times 10^2 \text{ kg m}^{-3}$ (at STP)
Isobaric specific heat capacity (vapor)	$c_p = 1.85 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Isochoric specific heat capacity (vapor)	$c_v = 1.39 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Ratio of specific heats (vapor)	$\gamma = c_p/c_v = 1.33$
Specific heat capacity (liquid water)	$c = 4.218 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Specific heat capacity (ice)	$c = 2.106 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$ (at 273 K)
Specific latent heat of fusion	$l_f = 3.34 \times 10^5 \text{ J kg}^{-1}$
Specific latent heat of vaporization	$l_v = 2.50 \times 10^6 \text{ J kg}^{-1}$
Specific latent heat of sublimation	$l_s = l_f + l_v$

*Standard temperature and pressure (STP) = 1013 mb and 273 K.

Appendix C

Physical Constants

Avogadro's number	$N_A = 6.022 \times 10^{26} \text{ mol}^{-1}$
Universal gas constant	$R^* = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$
Boltzmann constant	$k = 1.381 \times 10^{-23} \text{ J K}^{-1}$
Planck constant	$h = 6.6261 \times 10^{-34} \text{ J s}^{-1}$
Stefan-Boltzmann constant	$\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$
Speed of light	$c = 2.998 \times 10^8 \text{ m s}^{-1}$
Solar constant	$F_s = 1.372 \times 10^3 \text{ W m}^{-2}$
Radius of the earth	$a = 6.371 \times 10^3 \text{ km}$
Standard gravity	$g_0 = 9.806 \text{ m s}^{-2}$
Earth's angular velocity	$\Omega = 7.292 \times 10^{-5} \text{ s}^{-1}$

Appendix D

Vector Identities

$$\mathbf{A} \times (\mathbf{B} \times \mathbf{C}) = (\mathbf{A} \cdot \mathbf{C})\mathbf{B} - (\mathbf{A} \cdot \mathbf{B})\mathbf{C} \quad (\text{D.1})$$

$$\mathbf{A} \cdot (\mathbf{B} \times \mathbf{C}) = (\mathbf{A} \times \mathbf{B}) \cdot \mathbf{C} = \mathbf{B} \cdot (\mathbf{C} \times \mathbf{A}) \quad (\text{D.2})$$

$$(\mathbf{A} \times \mathbf{B}) \cdot (\mathbf{C} \times \mathbf{D}) = (\mathbf{A} \cdot \mathbf{C})(\mathbf{B} \cdot \mathbf{D}) - (\mathbf{A} \cdot \mathbf{D})(\mathbf{B} \cdot \mathbf{C}) \quad (\text{D.3})$$

$$\nabla(fg) = f\nabla g + g\nabla f \quad (\text{D.4})$$

$$\nabla \cdot (f\mathbf{A}) = \nabla f \cdot \mathbf{A} + f\nabla \cdot \mathbf{A} \quad (\text{D.5})$$

$$\nabla \times (f\mathbf{A}) = \nabla f \times \mathbf{A} + f\nabla \times \mathbf{A} \quad (\text{D.6})$$

$$\nabla \cdot (\mathbf{A} \times \mathbf{B}) = \mathbf{B} \cdot (\nabla \times \mathbf{A}) - \mathbf{A} \cdot (\nabla \times \mathbf{B}) \quad (\text{D.7})$$

$$\nabla \cdot \nabla \times \mathbf{A} = 0 \quad (\text{D.8})$$

$$\nabla \times \nabla f = 0 \quad (\text{D.9})$$

$$\nabla \cdot \nabla f = \nabla^2 f \quad (\text{D.10})$$

$$\nabla \times \nabla \times f = \nabla(\nabla \cdot f) - \nabla^2 f \quad (\text{D.11})$$

$$\nabla(\mathbf{A} \cdot \mathbf{B}) = \mathbf{A} \cdot \nabla \mathbf{B} + \mathbf{B} \cdot \nabla \mathbf{A} + \mathbf{A} \times \nabla \mathbf{B} + \mathbf{B} \times \nabla \times \mathbf{A} \quad (\text{D.12})$$

$$\nabla(\mathbf{A} \times \mathbf{B}) = \mathbf{B} \cdot \nabla \mathbf{A} - \mathbf{A} \cdot \nabla \mathbf{B} + \mathbf{A}(\nabla \cdot \mathbf{B}) - \mathbf{B}(\nabla \cdot \mathbf{A}) \quad (\text{D.13})$$

$$\mathbf{A} \cdot \nabla \mathbf{A} = \frac{1}{2} \nabla(\mathbf{A} \cdot \mathbf{A}) - \mathbf{A} \times (\nabla \times \mathbf{A}) \quad (\text{D.14})$$

Appendix E

Curvilinear Coordinates

Spherical Coordinates (λ, ϕ, r)

$$\nabla\psi = \frac{1}{r \cos \phi} \frac{\partial\psi}{\partial\lambda} \mathbf{e}_\lambda + \frac{1}{r} \frac{\partial\psi}{\partial\phi} \mathbf{e}_\phi + \frac{\partial\psi}{\partial r} \mathbf{e}_r$$

$$\nabla \cdot \mathbf{A} = \frac{1}{r \cos \phi} \frac{\partial A_\lambda}{\partial \lambda} + \frac{1}{r \cos \phi} \frac{\partial}{\partial \phi} (\cos \phi A_\phi) + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 A_r)$$

$$\begin{aligned} \nabla \times \mathbf{A} = & \frac{1}{(r^2 \cos \phi)} \left\{ r \cos \phi \left[\frac{\partial A_r}{\partial \phi} - \frac{\partial (r A_\phi)}{\partial r} \right] \mathbf{e}_\lambda \right. \\ & + r \left[\frac{\partial}{\partial r} (r \cos \phi A_\lambda) - \frac{\partial A_r}{\partial \lambda} \right] \mathbf{e}_\phi \\ & \left. + \left[\frac{\partial (r A_\phi)}{\partial \lambda} - \frac{\partial}{\partial \phi} (r \cos \phi A_\lambda) \right] \mathbf{e}_r \right\} \end{aligned}$$

$$\nabla^2 \psi = \frac{1}{r^2 \cos^2 \phi} \frac{\partial^2 \psi}{\partial \lambda^2} + \frac{1}{r^2 \cos \phi} \frac{\partial}{\partial \phi} \left(\cos \phi \frac{\partial \psi}{\partial \phi} \right) + \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial \psi}{\partial r} \right)$$

$$\begin{aligned} \nabla^2 \mathbf{A} = & \left[\nabla^2 A_\lambda - \frac{A_\lambda}{r^2 \cos^2 \phi} + \frac{2}{r^2 \cos \phi} \frac{\partial A_r}{\partial \lambda} + \frac{2 \sin \phi}{r^2 \cos^2 \phi} \frac{\partial A_\phi}{\partial \lambda} \right] \mathbf{e}_\lambda \\ & + \left[\nabla^2 A_\phi - \frac{A_\phi}{r^2 \cos^2 \phi} + \frac{2}{r^2} \frac{\partial A_r}{\partial \phi} - \frac{2 \sin \phi}{r^2 \cos^2 \phi} \frac{\partial A_\lambda}{\partial \lambda} \right] \mathbf{e}_\phi \\ & + \left[\nabla^2 A_r - \frac{2}{r^2} A_r - \frac{2}{r^2 \cos \phi} \frac{\partial}{\partial \phi} (\sin \phi A_\phi) - \frac{2}{r^2 \cos \phi} \frac{\partial A_\lambda}{\partial \lambda} \right] \mathbf{e}_r \end{aligned}$$

Cylindrical Coordinates (r, ϕ, z)

$$\nabla\psi = \frac{\partial\psi}{\partial r}\mathbf{e}_r + \frac{1}{r}\frac{\partial\psi}{\partial\phi}\mathbf{e}_\phi + \frac{\partial\psi}{\partial z}\mathbf{e}_z \quad (\text{E.6})$$

$$\nabla \cdot \mathbf{A} = \frac{1}{r}\frac{\partial}{\partial r}(rA_r) + \frac{1}{r}\frac{\partial A_\phi}{\partial\phi} + \frac{\partial A_z}{\partial z} \quad (\text{E.7})$$

$$\begin{aligned} \nabla \times \mathbf{A} = & \left[\frac{1}{r}\frac{\partial A_z}{\partial\phi} - \frac{\partial A_\phi}{\partial z} \right] \mathbf{e}_r + \left[\frac{\partial A_r}{\partial z} - \frac{\partial A_z}{\partial r} \right] \mathbf{e}_\phi \\ & + \left[\frac{1}{r}\frac{\partial(rA_\phi)}{\partial r} - \frac{1}{r}\frac{\partial A_r}{\partial\phi} \right] \mathbf{e}_z \end{aligned} \quad (\text{E.8})$$

$$\nabla^2\psi = \frac{1}{r}\frac{\partial}{\partial r}\left(r\frac{\partial\psi}{\partial r}\right) + \frac{1}{r^2}\frac{\partial^2\psi}{\partial\phi^2} + \frac{\partial^2\psi}{\partial z^2} \quad (\text{E.9})$$

$$\begin{aligned} \nabla^2\mathbf{A} = & \left[\nabla^2 A_r - \frac{A_r}{r^2} - \frac{2}{r^2}\frac{\partial A_\phi}{\partial\phi} \right] \mathbf{e}_r + \left[\nabla^2 A_\phi - \frac{A_\phi}{r^2} + \frac{2}{r^2}\frac{\partial A_r}{\partial\phi} \right] \mathbf{e}_\phi \\ & + \nabla^2 A_z \mathbf{e}_z \end{aligned} \quad (\text{E.10})$$